

RKNN Using Clipping Methodologies

¹ M.Vinothkumar, ²Dr.K.Selvam

¹Research Scholar, ²Professor

Dept of Computer Applications

Dr.MGR Educational & Research Institute, Chennai, Tamil Nadu, India.

Abstract -Reverse k Nearest Neighbor (RKNN) query is proposed based on the k Nearest Neighbor (KNN) query, which can be used to evaluate the influence of the query objects. At present RKNN query algorithms are mostly based on static or continuous objects, The algorithms for efficiently answering queries about large populations of moving objects are gaining interest. Given a group of nearby space objects as the query input, the authors propose the continuously monitoring RKNN algorithms based on the half-space pruning, compute the minimum bounding rectangles (MBRs) containing the query objects and consider the objects in the rectangles as a whole. Then, In order to get the query's final RKNN results.

Keywords:- Half-space, Dominance, Metric Based, Probabilistic, Prune.

INTRODUCTION

The clipping for RNN query processing in spatial databases has been well studied it is non-trivial to devise clipping strategies for RNN query processing on uncertain data. For example, if we naively use every instance of a Filtering Object to perform bi-sector clipping, it will a huge computation cost due to large number of instances in each uncertain object. Instead, we devise non-trivial generalization of bisector bisector clipping for minimum bounding rectangles (MBRs) of uncertain objects based on a novel notion of normalized half space. Verification is extremely expensive in probabilistic RNN query processing because, in order to verify an object as probabilistic RNN, we need to take into consideration not only the instances of this object but also the instances of query object and other nearby objects. Hence it is important to devise efficient clipping rules to reduce the number of objects that need verification.

Types of clipping

In this, we present several clipping rules from the following orthogonal perspectives:

- Half space based clipping that exploits geometrical properties
- Dominance based clipping that exploits topological properties
- Metric based clipping
- Probabilistic clipping that exploits the probability threshold

We remark that the first three of the above clipping techniques are the same as those presented. The only deference is that, in this chapter, we present generalized versions of these clipping rules that can be applied on multidimensional space (and not only on 2d space).

Half Space Clipping

Consider a query point q and a filtering object U that has n instances $\{u_1, u_2, \dots, u_n\}$. Let $H_{u_i}:q$ be the half space between q and u_i . Any instance $u \in U$ that lies in $\bigcap_{i=1}^n H_{u_i}:q$ has zero probability to be the RNN of q because by the property of $H_{u_i}:q$, u is closer to every u_i than to q . where the bisectors between q_1 and the instances of A are drawn and the half spaces $H_{a_1}:q_1$ and $H_{a_2}:q_1$ are shown. Intersection of the two half spaces is shown shaded and any point that lies in the shaded area is closer to both a_1 and a_2 than q_1 . For this reason, b_2 cannot be the RNN of q_1 in any possible world. This clipping is very expensive because we need to compute intersection of all half spaces $H_{u_i}:q$ for every $u_i \in U$. Below we present our clipping rules that utilize the MBR of the entire filtering object, R_{fil} , to prune the candidate object with respect to a query instance q or the MBR of uncertain query object Q .

Clipping using R_{fil} and an instance q

First we present the intuition. Consider the example of Fig. 5.3 where we know that the point p lies on a line MN but we do not know the exact location of p on this line. The bisectors between q and the end points of the line (M and N) can be used to prune the area safely.

In other words, any point that lies in the intersection of half spaces $H_M : q$ and $H_N : q$ (grey area) can never be the RNN of q . It can be proved that whatever be the location of point p on the line MN , the half space $H_p : q$ always contains $H_M : q \cap H_N : q$. Hence any point p' that lies in $H_M : q \cap H_N : q$ would always be closer to p than to q and for this reason cannot be the RNN of q .

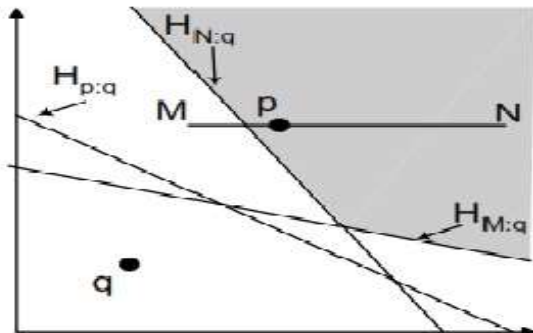


Fig 1: - The exact location of the Point p on line MN is not known

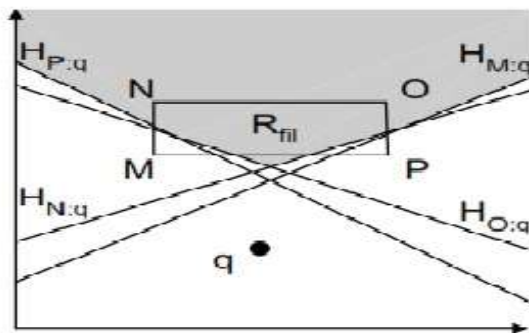


Fig 2: - Any point in shaded area can not be RNN of q in any possible world

Based on the above observation, below we present a clipping rule for the case when the exact location of a point p is unknown within some hyper-rectangle R_{fil} .

Clipping Rule 5.3.2 : Let R_{fil} be a hyper-rectangle and q be a query point. For any point p that lies in $T2d_{i=1} H_{C_i} : q$ (C_i is the i th corner of R_{fil}), $dist(p, q) > maxdist(p, R_{fil})$ and thus p cannot be the RNN of q .

Note that this clipping rule is a generalized version of the clipping rule 3.3.4 presented in Chapter 3. The proof is similar to the proof of clipping rule 3.3.4 and is omitted. Consider the example of Fig. 2. Any point that lies in shaded area is closer to every point in rectangle R_{fil} than to q . Note that if R_{fil} is a hyper rectangle that encloses all instances of the filtering object U_i then any instance $u \in U_{j,j=i}$ that lies in $T2H_{C_i} : q$ can never be the RNN of q in any possible world.

Clipping using R_{fil} and RQ

Clipping rule 5.3.2 prunes the area such that any point lying in it can never be the RNN of some instance q . However, the points in the pruned area may still be the RNNs of other instances of the query. Now, we present a clipping rule that prunes the area using R_{fil} and RQ such that any point that lies in the pruned area cannot be the RNN of any instance of Q .

Consider the example of Fig. 5.5 where the exact location of the query point q on line MN is not known. Unfortunately, in contrast to the previous case of Fig. 1, the bisectors between p and the end points of the line MN do not define the area that can be pruned. If we prune the area $H_p : M \cap H_p : N$ (the grey area), we may miss some point p' that is the RNN of q . Fig. 3 shows a point p' that is the RNN of q but lies in the shaded area. This is because the half space $H_p : q$ does not contain $H_p : M \cap H_p : N$. This makes the clipping using R_{fil} and RQ challenging.

Note that if $H_p : N$ is moved such that it passes through the point where $H_p : q$ intersects $H_p : M$ then $H_p : M \cap H_p : N$ would be contained by $H_p : q$. We note that in the worst case when p lies infinitesimally close to point M , $H_p : q$ and $H_p : M$ intersect each other at point c which is the centre of line joining p and M . Hence, in order to safely prune the area, the half space $H_p : N$ should be moved such that it passes through the point c . The point c is shown in Fig 3.

A half space that is moved to the point c is called a normalized half space and a half space $H_p : N$ that is normalized is denoted as $H' : p : N$. Fig. 3 shows $H' : p : N$ in broken line and $H_p : N \cap H_p : M$ (the dotted shaded area) can be safely pruned.

Before we present our clipping rule for the general case that uses 2d half spaces to prune the area using hyper-rectangles RQ and R_{fil} , we define the following concepts:

Antipodal Corners: Let C be a corner of rectangle R_1 and C' be a corner in R_2 , the two corners are called antipodal corners² if for every dimension i where $C[i] = R_1L[i]$ then $C'[i] = R_2H[i]$ and for every dimension j where $C[j] = R_1H[j]$ then $C'[j] = R_2L[j]$. Fig. 5.6 shows two rectangles R_1 and R_2 . The corners D and O are antipodal corners. Similarly, other pairs of antipodal corners are (B, M) , (C, N) and (A, P) .

Antipodal half space: A half space that is defined by the bisector between two antipodal corners is called antipodal half space. Fig. 4. shows two antipodal half spaces $H_{M:B}$ (resp. $H_{P:A}$) is the lowest (resp. highest) coordinate of a hyper-rectangle R in i th dimension $HM :B$ and $HP :A$.

Normalized half space: Let B and M be two points in hyper-rectangles R_1 and R_2 , respectively. The normalized half space H' is a space defined by the bisector between M and B that passes through a point c such that $c[i] = (R_1L[i] + R_2L[i])/2$ for all dimensions i for which $B[i] > M[i]$ and $c[j] = (R_1H[j] + R_2H[j])/2$ for all dimensions j for which $B[j] \leq M[j]$. Fig.6 shows two normalized (antipodal) half spaces H' and H' . The point c for each half space is also shown. The inequalities 1 and 2 define the half space $HM :B$ and its normalized half space H' respectively.

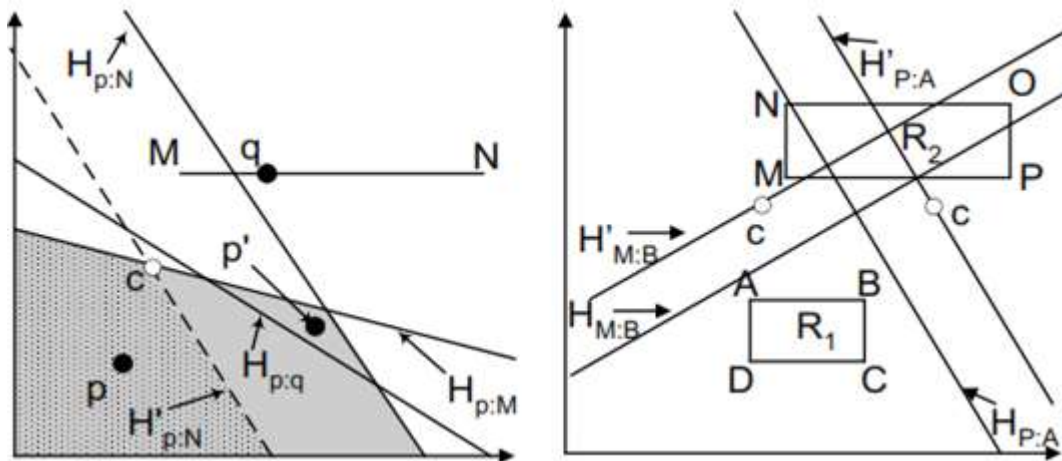


Fig 3: - Any point in dotted area can never be RNN of q

Fig 4: - Antipodal corners and normalized half spaces

Clipping Rule 5.3.3 : Let R_Q and R_{fil} be two hyper-rectangles. For any point p that lies $d_i = H'$, $mindist(p, R_Q) > maxdist(p, R_{fil})$ where H' is normalized half space between C (the i th corner of the rectangle R_{fil}) and its antipodal corner C' in R_Q .

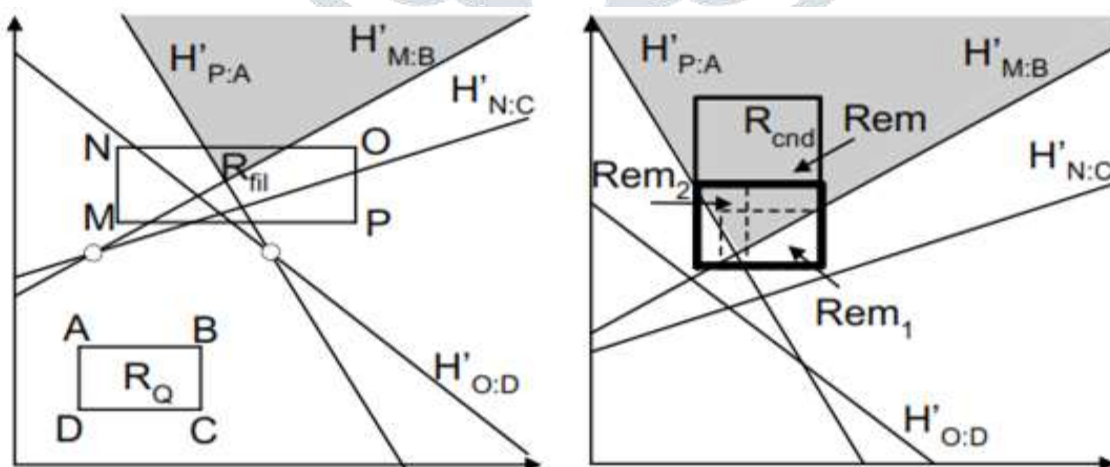


Fig 5: - Any point in Shaded area can never be RNN of $q \in Q$

Fig 6: - Clipping part of the candidate object R_{cnd} that cannot be pruned

Consider the example of Fig. 5 where the normalized antipodal half spaces are drawn and their intersection is shown shaded. Any point that lies in the shaded area is closer to every point in rectangle R_{fil} than every point in rectangle R_Q . Note that if R_{fil} and R_Q are the MBRs enclosing all instances of an uncertain object U_i and query object Q , respectively, any instance $u \in U_j, j=i$ that lies in the pruned region, $T_2 H'$, cannot be RNN of any instance of $q \in Q$ in any possible world. Even if the clipping region

partially overlaps with R_{fil} , we can still trim the part of any other hyper-rectangle that falls in the pruned region.

It is known that exact trimming becomes inefficient in high dimensional space, therefore, we adopt the loose trimming of R_{cnd} proposed.

The overall half space clipping algorithm that integrates clipping rules 5.3.2 and 5.3.3 is illustrated in Algorithm 7. For each half space, we use the clipping algorithm in [013] to find a remnant rectangle $Rem_i \subseteq R_{cnd}$ that cannot be pruned (lines 4 and 7).

Algorithm 1 : hspace-clipping (Q, R_{fil} , R_{cnd})

Input: Q: an MBR containing instances of Q ; R_{fil} : the MBR to be used for trimming

R_{cnd} : the candidate MBR to be trimmed

Description:

```

1: Rem =  $\emptyset$  /* Remnant rectangle */
2: for each corner  $C_i$  of  $R_{fil}$  do
3:   if Q is a point then
4:      $Rem_i = \text{clip}(R_{cnd}, H_{C_i}:Q)$  /* clipping algorithm [013] */
5:   else if Q is a hyper-rectangle then
6:      $C' =$  antipodal corner of  $C_i$  in Q
7:      $Rem_i = \text{clip}(R_{cnd}, H'_{i'})$  /* clipping algorithm [013] */
8:   enlarge Rem to enclose  $Rem_i$ 
9:   if Rem =  $R_{cnd}$  then
10:    return  $R_{cnd}$ 
11: return Rem

```

After all the half spaces have been used for clipping, we calculate the MBR $Rem \subseteq R_{cnd}$ as the minimum bounding hyper rectangle covering every Rem_i . As such, we trim the original R_{cnd} to Rem . For better illustration we zoom Fig. 5 and show the clipping of a hyper-rectangle R_{cnd} in Fig. 6.

The algorithm returns Rem_1, Rem_2 (rectangles shown with broken lines) when H' and H'' are parameters to the clipping algorithm, respectively. For the half spaces H' and H'' the whole hyper-rectangle R_{cnd} can be pruned so the algorithm returns \emptyset . The remnant hyper-rectangle Rem is an MBR that encloses Rem_1 and Rem_2 . Note that at any stage if the remnant rectangle Rem becomes equal to R_{cnd} , the clipping by other bisectors is not needed so R_{cnd} is returned without further clipping (line 10).

Dominance Clipping

We first give the intuition behind this clipping rule. The clipping by using clipping rule 5.3.3 in two dimensional spaces. The normalized half spaces are defined such that if R_{fil} is fully dominated by RQ in all dimensions then all the normalized antipodal half spaces meet at point F_p . We also observe that for the case when R_{fil} is fully dominated by RQ , the angle between the half spaces that define the pruned area (shown in grey) is always greater than 90° . Based on these observations, it can be verified that the space dominated by F_p (the dotted-shaded area) can be pruned.

Let RQ be the MBR containing instances of Q. We can obtain the 2d regions. RU_i be an MBR of a filtering object R_{fil} that lies completely in one of the 2d regions. Let f be the furthest corner of RU from RQ and n be the nearest corner of RQ from f . The frontier point F_p lies at the centre of line joining f and n .

Clipping Rule 5.3.4

Any instance $u \in U_j$ that is dominated by the frontier point F_p of a filtering object cannot be RNN of any $q \in Q$ in any possible world.

The dominance clipping (one in each region). In each partition the shaded area is dominated by F_p and can be pruned. Note that if R_{fil} is not fully dominated by R_Q , we cannot use this clipping rule because the normalized antipodal half spaces in this case do not meet at the same point.

For example, the four normalized antipodal half spaces intersect at two points in Fig. 5. In general, the clipping power of this rule is less than that of the half space clipping. The area pruned by the half space clipping (shaded area) and dominance clipping (dotted area). The main advantage of this clipping rule is that the clipping procedure is computationally more efficient than the half space clipping, as checking the dominance relationship and trimming the hyper-rectangles is easier.

Metric Based Clipping

Clipping Rule 5.3.5 An uncertain object R_{cnd} can be pruned if $\max\text{dist}(R_{cnd}, R_{fil}) < \min\text{dist}(R_{cnd}, R_Q)$. This clipping approach is the least expensive. Note that it cannot prune part of R_{cnd} , i.e., it either invalidates all the instances of R_{cnd} or does nothing.

Probabilistic Clipping

Note that we did not discuss probability threshold while presenting previous clipping rules. In this section, we present a clipping rule that exploits the probability threshold and embeds it in all previous clipping rules to increase their clipping powers.

A simple exploitation of the probability threshold is to trim the candidate object using previous clipping rules and then prune the object if the accumulative appearance probability of instances within its remnant rectangle is less than the threshold.

Next, we present a more powerful clipping rule that is based on estimating an upper bound of the RNN probability of candidate objects. In previous clipping rules, we prune some area using MBR of a query object R_Q and a filtering object R_{fil} .

We observe that the area pruned by using R' and R_{fil} always contains the area pruned by R_Q and R_{fil} where $R' \subseteq R_Q$ and $R' \subseteq R_{fil}$. The shaded area is pruned when R' and R_{fil} are used for clipping and the dotted shaded area is pruned when R_Q and R_{fil} are used. Note that this observation also holds for the dominance clipping.

We can use the observation presented above to prune the objects that cannot have RNN probability greater than the threshold. First, we give a formal description of this clipping rule and then we give an example.

Clipping Rule 5.3.6: Let the instances of Q be divided into n disjoint sets $\{Q_1, Q_2, \dots, Q_n\}$ and R_{Qi} be the minimum bounding rectangle enclosing all instances in Q_i . Let $\{R_{cnd1}, R_{cnd2}, \dots, R_{cndn}\}$ be the set of bounding rectangles such that each R_{cndi} contains the instances of the candidate object that cannot be pruned for Q_i using any of the clipping rules. Let PR_{Qi} and PR_{cndi} be the total appearance probabilities of instances in Q_i and R_{cndi} , respectively. If $P_n(PR_{cndi} \cdot PR_{Qi})$, the candidate object can be pruned.

Clipping rule 5.3.6: Computes an upper bound of the RNN probability of the candidate object by assuming that all instances in R_{cndi} are RNNs of all instances in Q_i . The candidate object can be safely pruned if this upper bound is still less than the threshold.

Example 5.3.7 : MBRs of the query object R_Q and a candidate object R_{cnd} along with their instances (q_1 to q_5 and u_1 to u_4). Assume that all instances within an object have equal appearance probabilities (e.g: $p_{qi} = 0.2$ for every q_i and $p_{ui} = 0.25$ for every u_i). Suppose that no part of R_{cnd} can be pruned using R_Q and any filtering object R_{fil} (for better illustration, filtering object is not shown).

We prune R_{cnd} using the rectangle R_{Q1} that is contained by R_Q . This trims R_{cnd} and the remnant rectangle R_1 is obtained. Similarly, R_2 is the remnant rectangle when clipping rules are applied for R_{Q2} . Note that only the instances in R_1 (u_1 and u_2) can be the RNN of instances in R_{Q1} (q_3, q_4 and q_5). Similarly, no instance can be the RNNs of any instance in R_{Q2} because R_2 is empty. So the maximum RNN probability of R_{cnd} is $(0.6 \times 0.5) + (0.4 \times 0) = 0.3$. If the probability threshold is greater than 0.3, we can prune R_{cnd} . Otherwise, we can continue to trim R_{cnd} by using the smaller rectangles contained in R_{Q1} .

In our implementation, we build an R-tree on query object and the clipping rule is applied iteratively using MBRs of children. For more details, please see Algorithm 11. Although the smaller rectangles R' contained in R_{fil} can also be used, we do not use them because unlike query object there may be many filtering objects.

Hence, using the smaller rectangles for each of the filtering objects would make this clipping rule very expensive in practice (more expensive than the efficient verification presented).

Integrating the clipping rules

Algorithm 8 is the implementation of clipping rules 5.3.2 to 5.3.5. Specifically, we apply clipping rules in increasing order of their computational costs (i.e., from clipping rule 5.3.5 to 5.3.2). While simple clipping rules are not as restricting as more expensive ones, they can quickly discard many non-promising candidate objects and save the overall computational time.

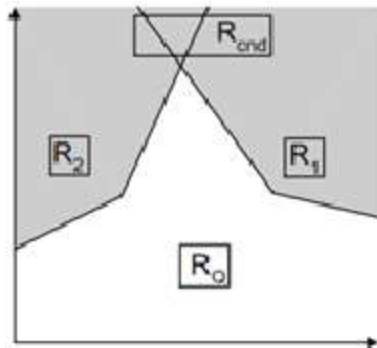


Fig 7 :- R_{end} can be pruned by R_1 and R_2

It is important to use all the filtering objects to filter a candidate objects. R_{end} cannot be pruned by either R_1 or R_2 , but will be pruned by considering both of them. Two subtle optimizations in the algorithm are:

- If $\text{mindist}(R_{end}, R_{fil}) > \text{maxdist}(RQ, R_{end})$ for a given MBR R_{fil} , then R_{fil} cannot prune any part of R_{end} . Hence such R_{fil} is not considered for dominance and half space clipping (lines 4-5). However, R_{fil} may still prune some other candidate objects, so we remove such R_{fil} only from a local set of filtering object, S_{fil} . This optimization reduces the cost of dominance and half space clipping.
- If the frontier point $Fp1$ of a filtering object R_{fil1} is dominated by the frontier point $Fp2$ of another filtering object R_{fil2} , then $Fp1$ can be removed from S_{fil} because the area pruned by $Fp1$ can also be pruned by $Fp2$. However, note that a frontier point cannot be used to prune its own rectangle. Therefore, before deleting $Fp1$, we use it to prune rectangle belonging to $Fp2$. This optimization reduces the cost of dominance clipping.

Algorithm 8 : Prune(Q, S_{fil}, R_{end})

Input: RQ : an MBR containing instances of Q ; S_{fil} : a set of MBRs to be used for trimming R_{end} : the candidate MBR to be trimmed

Description:

- 1: for each R_{fil} in S_{fil} do
- 2: if $\text{maxdist}(R_{end}, R_{fil}) < \text{mindist}(RQ, R_{end})$ then /* Clipping rule 5.3.5 */
- 3: return
- 4: if $\text{mindist}(R_{end}, R_{fil}) > \text{maxdist}(RQ, R_{end})$ then
- 5: $S_{fil} = S_{fil} - R_{fil}$ /* R_{fil} cannot prune R_{end} */ $Rem = R_{end}$
- 6: for each R_{fil} in S_{fil} do
- 7: if R_{fil} is fully dominated by RQ in a partition p then /* Clipping rule 5.3.4 */
- 8: if some part of Rem lies in the partition p then
- 9: $Rem =$ the part of Rem not dominated by Fp
- 10: if ($Rem =$) then return
- 11: for each R_{fil} in S_{fil} do
- 12: $Rem = \text{hspace clipping}(RQ, R_{fil}, Rem)$ /* Clipping Rules 5.3.2 and 5.3.3 */

13: if (Rem =) then return

14: return Rem

CONCLUSION

We formalize probabilistic reverse nearest neighbor query that is to retrieve the objects from the uncertain data that have higher probability than a given threshold to be the RNN of an uncertain query object. We develop an efficient algorithm based on various novel clipping approaches that solves the probabilistic RNN queries on multidimensional uncertain data. The experimental results demonstrate that our algorithm is even more efficient than a sampling-based approximate algorithm for most of the cases and is highly scalable and performance of algorithm is tested by employing real data set. With a group of neighboring space objects as inquire point set, the experiment result shows that the proposed algorithm's efficiency is better than direct algorithm. This algorithm also has practical application value, could be used to evaluate the set object influence. Future work will focus on improving algorithm, researching RKNN and high-dimensional RKNN.

REFERENCES

- [1] Tao Yu-fei, Papadias D, Lian X, et al. Multidimensional reverse kNN search. The VLDB Journal The International Journal on Very Large Data Bases[J]. 2007, PP293-415
- [2] Wu Wei, Yang Fei, Chan Yong, Tan Kian-Lee. FINCH: Evaluating reverse k nearest neighbor queries on location data. Proceedings of the Very Large Data bases[J]. 2008, PP1056-1067
- [3] Wang Wei, Wang Wenping. An algorithm for finding the smallest circle containing all points in a given point set. Journal of Software[J]. 2000, PP1237-1240
- [4] Kyriakos Mouratidis, Dimitris Papadias, Spiridon Bakiras and Yufei Tao. A Threshold-Based Algorithm for Continuous Monitoring of k Nearest Neighbors. TKDE, pages 1451–1464, 2005.
- [5] Yufei Tao, Reynold Cheng, Xiaokui Xiao, Wang Kay Ngai, Ben Kao and Sunil Prabhakar. Indexing Multi-Dimensional Uncertain Data with Arbitrary Probability Density Functions. In VLDB, pages 922–933, 2005.
- [6] Korn F, Muthukrishnan S. Influence sets based on reverse nearest neighbor queries. Special Interest Group of Data[J]. 2000, PP201-212
- [7] Wu Wei, Chee Fei Yang, Chan Yong, Tan Kian-Lee. Continuous reverse k nearest neighbor monitoring. Proceedings of the 9th International Conference on Mobile Data Management[J]. 2008, PP132-139.