

# Dedicated multiplication hardware on FPGA with low Power

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**Abstract :** This paper proposes a basic and effective Montgomery augmentation calculation with the end goal that the minimal effort and elite Montgomery measured multiplier possibly actualized. The furthered multiplier gets and yields data with twofold depiction and uses only a solitary level CSA to avoid the convey proliferation at each development activity. This CSA is bestow to perform operand pre-computation and arrangement change from convey spare association to twofold depiction provoking a lower hardware cost and basic way concede costs consummating one particular duplication. To beat this issue, a configurable CSA (CCSA), which have one full viper or two semi half adders, is exerted to decrease the extra clock cycles and setup change extensively. Additionally, a framework that perhaps recognize and skirt the pointless convey spare extension activity in the one-level CCSA plan while keeping up the short basic way delay is created. In this manner, the extra clock cycles for operand pre estimation and game plan change possibly covered up and high throughput possibly procured. Test result shows that the furthered Montgomery Modular Multiplication perhaps accomplish higher execution and critical area–time item upgrade when deviate with past plans.

**Keyword:** CCSA, Montgomery, Low power, multiplication.

## I. Introduction

In several crypto systems, modular multiplication (MM) with expansive whole numbers is the utmost classical operation. In this manner, various calculations and equipment execution have been introduced to complete the MM[1] all the ample rapidly, and Montgomery's calculation is a standout amongst the utmost understood MM calculations.

A few variations of FFT strategy have been furthered pointing at the evasion zero-cushioning. Phatak and Goff's strategy plays out the

Montgomery measured decrease by one straight convolution and one cyclic convolution. Their strategy could incompletely keep distant from the zero-cushioning issue, since just cyclic convolution conceivably registered without zero-cushioning[3].

It [4] depicts the plan and usage of low power particular multiplier of RSA and equalizations its zone and speed. By enhancing Montgomery particular duplication calculation, advancing basic way and utilizing a few low power techniques, this paper accomplishes low power and additionally fast execution. The outline is actualized utilizing SMIC 0.13um CMOS process, the normal power utilization is 106uW at 13.56MHZ when executing 1024-piece operations, the zone is around 0.17mm<sup>2</sup> and an opportunity to complete particular increase are 1412 clock cycles, such fantastic property make it appropriate for RSA operation.

It [5] Montgomery multipliers of carry save snake (CSA) design require a full expansion to change over the carry save portrayal of outcome into a regular frame. In this paper, we reuse the CSA engineering to play out the outcome arrange change, which prompts little zone and quick speed. The aftereffects of execution on FPGAs demonstrate akin the new Montgomery multiplier is around 113.4 M<sub>bit</sub>/s for 1024-piece operands at a clock of 114.2 MHz

Montgomery[6] confined increment is one of real tasks exerted as a piece of cryptographic estimations, for instance, RSA and Elliptic Curve Cryptosystems. At CHES 1999, Tenca and Koc, furthered the Multiple-Word Radix-2 Montgomery Multiplication (MWR2MM) figuring and introduced a now-commendable outline for consummating Montgomery duplication in gear. With parameters updated for minimum inaction, this plan plays out a singular Montgomery increment in approximately 2n clock cycles, where n is the range of operands in bits. In this paper, we propose two new hardware structures that perhaps play out a comparable activity in generally n clock

cycles with outmost a comparative clock period. These two plans rely upon pre preparing midway results using two possible doubts concerning the utmost basic bit of past word. These two models defeat the primary building of Tenca and Koc, to extent the thing dormancy times locale by 23 and 50 percent, independently, for a couple of utmost ordinary operand sizes exerted as a piece of cryptography.

## II. Methodology

Around there, we propose another SCS-based Montgomery MM figuring to lessen the fundamental route deferral of Montgomery multiplier. Likewise, the drawback of ample clock cycles for consummating one duplication is also improved while keeping up the upsides of short fundamental way delay and low gear versatile quality.

### A. Critical Path Delay Reduction

The essential path deferral of SCS-based multiplier possibly diminished by joining the advantages of FCS-MM-2 and SCS-MM-2. That is, we perhapspre register  $D=B+N$  and reuse the one-level CSA building to perform  $B+N$  and the setup change. Fig. 1 exhibits the modified SCS-based Montgomery increment (MSCS-MM) figuring and one possible gear outline, exclusively. The Zero\_D circuit in Fig. 1 is exerted to recognize whether SC is equal to zero, which possibly master using one NOR activity. The Q\_L circuit picks the  $q_i$  regard according to stage 7 of algorithm stated below. The extension tasks of  $B+N$  and the setup change are performed by the one-level CSA designing of MSCS-MM multiplier through over and again executing the convey spare development  $(SS, SC) = SS+SC+0$  until  $SC=0$ .

In addition, we furtheramplepre process  $A_i$  and  $q_i$  in cycle  $i-1$  (this will be cleared up ample doubtlessly in Section III-C) so they possibly exerted to rapidly pick the pinned for information operand from 0, N, B, and D through the multiplexer M3 in accentuation I. Forth these lines, the essential route delay of MSCS-MM multiplier possibly diminished into  $TMUX4+TFA$ . Regardless, despite playing out the three-input convey spare additions [i.e., stage 12 of algorithm stated below]  $k+2$  times, various extra clock cycles are endorsed to perform  $B+N$  and the arrangement change through the one-level CSA

designing since they ought to be performed once in every MM.

### Algorithm for MM

Inputs: A,B,N(modulus)

Output: SS[k+2]

1.  $(SS,SC)$
  2.  $=(B+N+0);$  While( $SC!=0$ )
  3.  $(SS,SC)=(SS+SC+0);$
  4.  $D=SS;$
  5.  $SS[0]=0;$
  6. for  $i=0$  to  $k-$
  7.  $1 \{$   $q_i=(SS[i]o$
  8.  $+ SC[i]o + A_i*B_o)mod2;$  if( $A_i=0$  and
  9.  $q_i=0) x=0;$  if( $A_i=0$  and
  10.  $q_i=1) x=N;$  if( $A_i=1$  and
  11.  $q_i=0) x=B;$  if( $A_i=1$  and
  12.  $q_i=1) x=D;$
  13.  $(SS[i+1],SC[i+1])=(SS[i]+SC[i]+x)/2;$
  14.  $(SC[k+2] != 0)$  } While
  15.  $(SS[k+2],SC[k+2])=$
  16.  $SC[k+2]+0);$   $(SS[k+2]+$
- return SS[k+2];

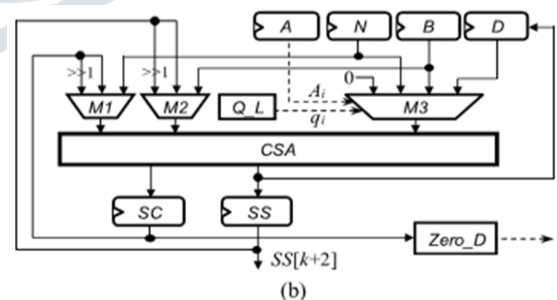


Fig 1. MSCS- MM Multiplier.

### B. Clock Cycle Number Reduction

To decrease the clock cycle number, a CCSA outline which perhaps perform one three-input convey spare development or two serial two-input convey spare increases is furthered to substitute for one-level CSA designing in Fig.1. Fig. 2(a) shows two cells of one-level CSA outline in Fig. 1, each cell is one general FA which

perhaps play out the three-input convey spare development. Fig. 2(b) exhibits two cells of furthered configurable FA (CFA) circuit. In case  $\alpha = 1$ , CFA is one FA and perhaps perform one three-input convey spare development (implied as 1F\_CSA). Else, it is two half-adders (HAs) and perhaps perform two serial two-input convey spare builds (meant as 2H\_CSA), as showed up in Fig. 2(c). For this circumstance, G1 of CFA<sub>j</sub> and G2 of CFA<sub>j+1</sub> in Fig. 2(b) will go about as HA1<sub>j</sub> in Fig. 2(c), and G3, G4, and G5 of CFA<sub>j</sub> in Fig. 2(b) will bear on as HA2<sub>j</sub> in Fig. 2(c). Furtherample, we modify the 4-to-1 multiplexer M3 in Fig. 1 into an unraveled multiplier SM3 as showed up in Fig. 2(d) in light of reality that one of its wellsprings of data is zero, where  $\sim$  means the INVERT activity. Note that M3 has been supplanted by SM3 in the furthered one-level CCSA designing showed up in Fig. 2(b) According to concede extent showed up in Table II, TSM3 (i.e.,  $0.68 \times TFA$ ) is vague to TMUX3 (i.e.,  $0.63 \times TFA$ ) and TMUX12 (i.e.,  $0.23 \times TFA$ ) is ample diminutive than TXOR2 (i.e.,  $0.34 \times TFA$ ). Thusly, the essential path deferment of furthered one-level CCSA outline in Fig. 2(b) is estimated to that of one-level CSA designing in Fig. 2(a).

isolated by 2) when  $A_i = q_i = 0$  and  $SS[i]_0 = SC[i]_0 = 0$ . Likewise, the banner  $skip_{i+1}$  exerted as a piece of the  $i$ th cycle to exhibit whether the convey spare extension in the  $(I + 1)$  accentuation will be skipped possibly imparted as

$$skip_{i+1} = \sim (A_{i+1} \vee q_{i+1} \vee SS[i + 1]_0)$$

Where,  $\vee$  speaks to OR task. If  $skip_{i+1}$  created in  $i$ th cycle is 0, the convey spare extension of  $(I + 1)$ th accentuation won't be skipped. For this circumstance,  $q_{i+1}$  and  $A_{i+1}$  conveyed in  $i$ th accentuation possibly set distant in FFs and after that bestow to speedy pick the estimation of  $x$  in the  $(i+1)$ th cycle.

### C. Quotient Pre computation

As said above  $A_{i+1}$ ,  $A_{i+2}$ ,  $q_{i+1}$ , and  $q_{i+2}$  must be known in  $i$ th emphasis for avoiding the superfluous operation in the  $(i+1)$ th cycle. It is anything but difficult to obtain  $A_{i+1}$  and  $A_{i+2}$  in  $i$ th cycle. The remainder  $q_{i+1}$  conceivably figured in  $i$ th emphasis like stride 7 of Fig. 3.1(a) as takes after

$$q_{i+1} = (SS[i + 1]_0 + SC[i + 1]_0 + A_{i+1} \times B_0) \bmod 2. \quad (3)$$

Be that as it may,  $SS_{[i+1]0}$  and  $SC_{[i+1]0}$  are inaccessible until (1) is finished, as appeared in Fig. 3. Subsequently, the basic way of Montgomery multiplier in Fig. 3.1(b) will be generally stretched if (3) is straightforwardly employed to create  $q_{i+1}$  in  $i$ th cycle. To keep distant from this situation,  $N$ ,  $B$ , and  $D$  are adjusted as takes after with the goal that  $SS_{[i+1]0}$ ,  $SC_{[i+1]0}$ ,  $q_{i+1}$ , and  $q_{i+2}$  conceivably immediately originated in  $i$ th cycle. Since modulus  $N$  is an odd number and is comprehended the  $i$ th cycle just when  $q_i$  is equivalent to one, it is discovered that no less than a proliferated convey 1 is originated since  $N_0$  is equivalent to one. Forth these lines, we perhaps straightforwardly utilize the incentive as appeared in (4) rather than  $N$  to fulfill the procedure of Montgomery MM. A short time later: 0 must be equivalent to zero.

$$\hat{N} = \begin{cases} N + 1, & \text{if } N_{1:0} = 11 \\ 3N + 1, & \text{if } N_{1:0} = 01. \end{cases} \quad (4)$$

In addition, we employ  $\hat{B} = 8$  instead of  $B$  to guarantee that  $2:0$  is equivalent to zero so  $A_{i+1} \times B_0$  in (3) conceivably disposed of and the calculation of  $q_{i+2}$  perhaps likewise be disentangled. Note that

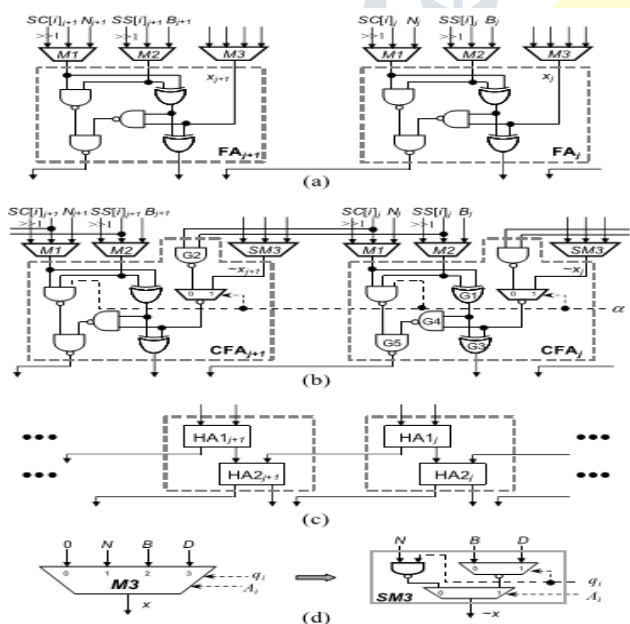
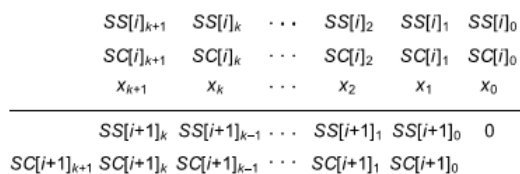


Fig.2. (a) Conventional FA circuit (b) Furthered CFA circuit. (c) Two serial HAs. (d) Simplified multiplexer SM3

Therefore, the computation of (1) in cycle  $I$  possibly skipped if we direct right move the yields of one-level CSA outline in the  $(I - 1)$ th accentuation by useful in vain positions (i.e., discognate by 4) instead of one piece position (i.e.,

three additional time cycles toward the finish of MM for figuring division by two are important to keep up the rightness of Montgomery MM since Bis supplanted with 8B.If N and B are supplanted by and the created 1:0( = + )must be equivalent to zero. After N, B, and D are supplanted andwe perhaps guarantee that the two LSBs of variable x(i.e., x1:0)in (1) must be equivalent to zero. Accordingly, the convey esteem SC[i+1]0in Fig. 3 is equivalent to SS[i]0ASC[i]0since x0=0



**Figure. 3. Three-to-two carry-save addition at the i<sub>th</sub> iteration of Fig. 1.**

**D. Furthered Algorithm and Hardware Architecture**

On the bases of basic way postpone lessening, clock cycle number decrease, and remainder precomputation specified over, another SCS-based Montgomery MM calculation (i.e., SCS-MM-New calculation appeared in Fig. 4) utilizing one-level CCSA engineering is furthered to fundamentally decrease the prescribed clock cycles for finishing one MM. As appeared in SCS-MM-New calculation, steps 1– 5 for creating and are first performed. Note that in light of fact that q<sub>i+1</sub> and q<sub>i+2</sub> must be created in ithemphasis, the iterative file I of Montgomery MM will begin from -1 rather than 0 and the relating starting estimations of and must be set to 0.

NEW	FURTHERED	SCS-BASED
<b>MONTGOMERY MM ALGORITHM:</b>		
Inputs :A,B,N(modulus)		
Output:SS[k+5]		
1.	A=0;^q=0;skipi+1=0;	^B=B<<3;^
2.	_CSA ^B+^N+0);	(SS,SC)=(if
3.	0)	While(SC!=
4.	(SS,SC)=2H_CSA(SS,SC);	
5.		^D=SS;
6.	1]=0;. SC[-1]=0;	i=-1,SS[-
7.	(i<=k+4) {	while
8.	and ^qi=0) x=0;	if(^Ai=0
9.	and ^qi=1) x=^N;	if(^Ai=0
10.	and ^qi=0) x=^B;	if(^Ai=1
11.	and ^qi=1) x=^D;	if(^Ai=1
12.	(SS[i+1],SC[i+1])=IF_CSA(SS[i]+SC[i]+x)>>1;	
13.	qi+1,qi+2,skipi+1 by (5),(7) and(8);	compute
14.	1){	If(skipi+1 =
15.	SS[i+2]=SS[i+1]>>1;(SC[i+2]=SC[i+1]>>1;	
16.	=Ai+2,i=i+2;	^q=qi+2;^A
17.		{
18.		else {
19.	=Ai+1,i=i+1;	^q=qi+1;^A
20.		}
21.		}
22.		^q=0;^A=0;



```

23.           While
      (SC[k+5]!=0)

24.           (SS[k+5]=S
      C[k+5])=2H_(SS[k+5]+ SC[k+5]);

25.           return
      SS[k+5];
    
```

### III. Experimental results

The schematic flow of the proposed system is as shown below fig 5.

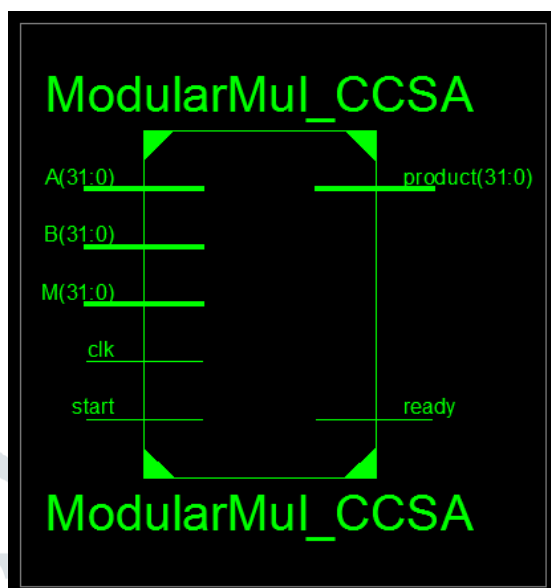


Fig 5. Schematic view of proposed system.

The RTL schematic view is as shown in below fig 6.

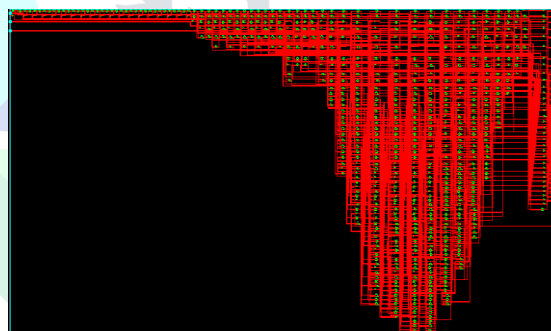


Fig 6. RTL view schematic

The simulation shows the multiplication of two operands of 32 bit in length. The simulation results shows that the power consumed by the proposed system is less.

The results are shown in Fig 7.

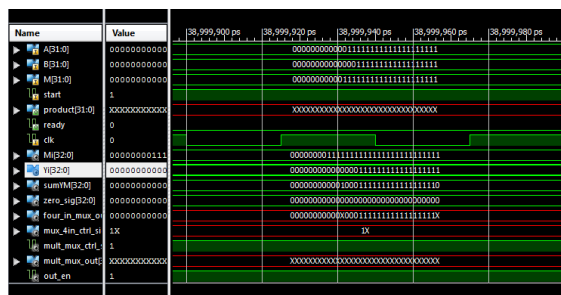


Fig 7. Simulation of multiplication of two operands.

Fig. 4(a). SCS-MM-New algorithm

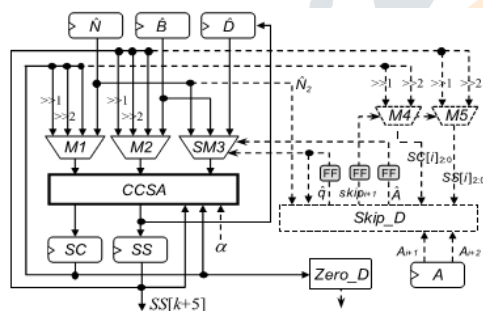


Fig.4 (b).SCS-MM-New multiplier.

Toward the start of Montgomery duplication, the FFs put distant skip<sub>i+1</sub>, are first reset to 0 as appeared in step 1 of SCS-MM-New calculation with the goal that = + conceivably registered by means of one-level CCSA design. When playing out the while circle, the skip detectorSkip<sub>D</sub>showninFig.3.6is employed to create skip<sub>i+1</sub>,and .The Skip<sub>D</sub> is made out of four XOR gates, three AND gates, one NOR gate, and two 2-to-1 multiplexers. It initially creates the q<sub>i+1</sub>, q<sub>i+2</sub>and skip<sub>i+1</sub>signal in thei<sup>th</sup> emphasis as indicated by (5), (7), and (8), individually, and after that chooses the right ^ qand as per skip<sub>i+1</sub>. Toward the finish of the ith emphasis and skip<sub>i+1</sub>must be put distant to FFs.

The device utilization by the device is as shown in the Fig 8. The fig 9 shows the total delay generated from the device which is 10.08 nano seconds

Device Utilization Summary (estimated values)			
Logic Utilization	Used	Available	Utilization
Number of Slices	286	4656	6%
Number of Slice Flip Flops	75	9312	0%
Number of 4 input LUTs	539	9312	5%
Number of bonded IOBs	131	190	68%
Number of GCLs	1	24	4%

Fig 8. Device utilization by hardware

MUXCY:CI->O	32	0.399	1.225	Mcompa_product_sig_cmp_lt0000
LUT3:I0->O	1	0.612	0.357	product_sig<9>1 (product_9_OBUF
OBUF:I->O			3.169	product_9_OBUF (product<9>)
-----				
Total		10.088ns	(7.899ns logic, 2.189ns route)	
			(78.3% logic, 21.7% route)	

Fig 9. Delay generated by the proposed system.

## IV. Conclusion

FCS-based multipliers keep up the data and yield operands of Montgomery MM in the convey spare design to escape from the association change, provoking less clock cycles yet greater range than SCS-based multiplier. To redesign the execution of Montgomery MM while keeping up the low gear diserse quality, this venture has changed the SCS-based Montgomery increment figuring and furthered a negligible exertion and predominant Montgomery specific multiplier. The furthered multiplier exerted one-level CCSA outline and maintained a strategic distance from the trivial convey spare development tasks, all things studios, diminish the essential way delay and recommended clock cycles for consummating one MM activity. Test comes to fruition showed akin the furthered approaches are point of fact prepared for enhancing the execution of radix-2 CSA-based Montgomery multiplier while keeping up low hardware multifaceted nature.

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