

Intuitionistic Fuzzy Quasi γ Generalized Continuous Mappings

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Abstract: In this paper, I am introduce intuitionistic fuzzy quasi γ generalized continuous mappings and investigate some of their properties. I am provide the relation between intuitionistic fuzzy quasi γ generalized continuous mappings and some of the already existing intuitionistic fuzzy continuous mappings.

Keywords: Intuitionistic fuzzy topology, intuitionistic fuzzy continuous mappings, intuitionistic fuzzy quasi γ generalized continuous mappings.

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1. Introduction

Atanassov [1] introduced the idea of intuitionistic fuzzy sets. Coker [2] introduced intuitionistic fuzzy topological spaces using the notion of intuitionistic fuzzy sets. Prema, S and Jayanthi, D[5] introduced intuitionistic fuzzy γ generalized closed sets. In this paper, I am introduce the notion of intuitionistic fuzzy quasi γ generalized continuous mappings in intuitionistic fuzzy topological spaces. I am provide some characterizations of intuitionistic fuzzy quasi γ generalized continuous mappings and establish the relationships with other classes of early defined forms of intuitionistic fuzzy continuous mappings.

2. Preliminaries

Definition 2.1: [1] An intuitionistic fuzzy set (IFS for short) A is an object having the form

$$A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle : x \in X \}$$

where the functions $\mu_A : X \rightarrow [0,1]$ and $\nu_A : X \rightarrow [0,1]$ denote the degree of membership (namely $\mu_A(x)$) and the degree of non-membership (namely $\nu_A(x)$) of each element $x \in X$ to the set A respectively, and $0 \leq \mu_A(x) + \nu_A(x) \leq 1$ for each $x \in X$. Denote by IFS (X), the set of all intuitionistic fuzzy sets in X . An intuitionistic fuzzy set A in X is simply denoted by $A = \langle x, \mu_A, \nu_A \rangle$ instead of denoting $A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle : x \in X \}$.

Definition 2.2: [1] Let A and B be two IFSs of the form $A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle : x \in X \}$ and $B = \{ \langle x, \mu_B(x), \nu_B(x) \rangle : x \in X \}$. Then,

(a) $A \subseteq B$ if and only if $\mu_A(x) \leq \mu_B(x)$ and $\nu_A(x) \geq \nu_B(x)$ for all $x \in X$,

(b) $A = B$ if and only if $A \subseteq B$ and $A \supseteq B$,

$$(c) A^c = \{ \langle x, \nu_A(x), \mu_A(x) \rangle : x \in X \},$$

$$(d) A \cup B = \{ \langle x, \mu_A(x) \vee \mu_B(x), \nu_A(x) \wedge \nu_B(x) \rangle : x \in X \},$$

$$(e) A \cap B = \{ \langle x, \mu_A(x) \wedge \mu_B(x), \nu_A(x) \vee \nu_B(x) \rangle : x \in X \}.$$

The intuitionistic fuzzy sets $0_{\sim} = \langle x, 0, 1 \rangle$ and $1_{\sim} = \langle x, 1, 0 \rangle$ are respectively the empty set and the whole set of X .

Definition 2.3: [2] An intuitionistic fuzzy topology (IFT) on X is a family τ of IFSs in X satisfying the following axioms:

- (i) $0_{\sim}, 1_{\sim} \in \tau$,
- (ii) $G_1 \cap G_2 \in \tau$ for any $G_1, G_2 \in \tau$,
- (iii) $\cup G_i \in \tau$ for any family $\{G_i: i \in J\} \subseteq \tau$.

In this case the pair (X, τ) is called the intuitionistic fuzzy topological space (IFTS) and any IFS in τ is known as an intuitionistic fuzzy open set (IFOS) in X . The complement A^c of an IFOS A in an IFTS (X, τ) is called an intuitionistic fuzzy closed set (IFCS) in X .

Definition 2.4: [5] An IFS A in an IFTS (X, τ) is said to be an intuitionistic fuzzy γ generalized closed set (IF γ GCS) if $\gamma \text{cl}(A) \subseteq U$ whenever $A \subseteq U$ and U is an IF γ OS in (X, τ) .

The complement A^c of an IF γ GCS A in an IFTS (X, τ) is called an intuitionistic fuzzy γ generalized open set (IF γ GOS) in X .

Definition 2.5: [6] A mapping $f: (X, \tau) \rightarrow (Y, \sigma)$ is called an intuitionistic fuzzy γ generalized α continuous (IF γ G continuous) mapping if $f^{-1}(V)$ is an IF γ GCS in (X, τ) for every IFCS V of (Y, σ) .

Definition 2.6: [5] An IFTS (X, τ) is an intuitionistic fuzzy $\gamma_{\gamma} T_{1/2}$ (IF $\gamma_{\gamma} T_{1/2}$) space if every IF γ GCS is an IF γ CS in X .

Definition 2.7: [6] A mapping $f: X \rightarrow Y$ is called an intuitionistic fuzzy γ generalized irresolute mapping if $f^{-1}(A)$ is an IF γ GCS in X for each IF γ GCS A in Y .

Definition 2.8: [7] A mapping $f: X \rightarrow Y$ is called an intuitionistic fuzzy almost γ generalized continuous mapping if $f^{-1}(A)$ is an IF γ GCS in X for each IF γ CS A in Y .

Corollary 2.9: [3] Let $A, A_i (i \in J)$ be intuitionistic fuzzy sets in X and $B, B_j (j \in K)$ be intuitionistic fuzzy sets in Y and $f: X \rightarrow Y$ be a mapping. Then

- a) $A_1 \subseteq A_2 \Rightarrow f(A_1) \subseteq f(A_2)$
- b) $B_1 \subseteq B_2 \Rightarrow f^{-1}(B_1) \subseteq f^{-1}(B_2)$
- c) $A \subseteq f^{-1}(f(A))$ [If f is injective, then $A = f^{-1}(f(A))$]
- d) $f(f^{-1}(B)) \subseteq B$ [If f is surjective, then $B = f(f^{-1}(B))$]
- e) $f^{-1}(\cup B_j) = \cup f^{-1}(B_j)$
- f) $f^{-1}(\cap B_j) = \cap f^{-1}(B_j)$
- g) $f^{-1}(0_{\sim}) = 0_{\sim}$
- h) $f^{-1}(1_{\sim}) = 1_{\sim}$
- i) $f^{-1}(B^c) = (f^{-1}(B))^c$

Definition 2.10: [4] Let (X, τ) be an IFTS and $A = \langle x, \mu_A, \nu_A \rangle$ be an IFS in X . Then the intuitionistic fuzzy γ interior and intuitionistic fuzzy γ closure are defined by

$$\begin{aligned} \gamma \text{int}(A) &= \cup \{ G / G \text{ is an IF}\gamma\text{OS in } X \text{ and } G \subseteq A \}, \\ \gamma \text{cl}(A) &= \cap \{ K / K \text{ is an IF}\gamma\text{CS in } X \text{ and } A \subseteq K \}. \end{aligned}$$

Note that for any IFS A in (X, τ) , we have $\gamma \text{cl}(A^c) = (\gamma \text{int}(A))^c$ and $\gamma \text{int}(A^c) = (\gamma \text{cl}(A))^c$.

Definition 2.12: [3] Let f be a mapping from an IFTS (X, τ) into an IFTS (Y, σ) . Then f is said to be an

- (i) intuitionistic fuzzy semi continuous mapping if $f^{-1}(B) \in \text{IFSO}(X)$ for every $B \in \sigma$
- (ii) intuitionistic fuzzy α - continuous mapping if $f^{-1}(B) \in \text{IF}\alpha\text{O}(X)$ for every $B \in \sigma$
- (iii) intuitionistic fuzzy pre continuous mapping if $f^{-1}(B) \in \text{IFPO}(X)$ for every $B \in \sigma$

Definition 2.13: [4] Let f be a mapping from an IFTS (X, τ) into an IFTS (Y, σ) . Then f is said to be an intuitionistic fuzzy γ continuous mapping if $f^{-1}(B) \in \text{IFPO}(X)$ for every $B \in \sigma$.

3. Intuitionistic Fuzzy Quasi γ Generalized Continuous Mappings

In this section we introduce intuitionistic fuzzy quasi γ generalized continuous mappings and study some of their properties.

Definition 3.1: A mapping $f: (X, \tau) \rightarrow (Y, \sigma)$ is called an intuitionistic fuzzy quasi γ generalized α continuous mapping (IF quasi γ G continuous mapping) if $f^{-1}(V)$ is an IFCS in X for every IF γ GCS V of Y .

Theorem 3.2: Every IF quasi γ G continuous mapping is an IF continuous mapping but not conversely in general.

Proof: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IF quasi γ G continuous mapping. Let A be an IFCS in Y . Since every IFCS is an IF γ GCS in Y , A is an IF γ GCS in Y . Then by hypothesis $f^{-1}(A)$ is an IFCS in X . Hence f is an IF continuous mapping.

Example 3.3: Let $X = \{a, b\}$, $Y = \{u, v\}$ and $G_1 = \langle x, (0.5_a, 0.6_b), (0.5_a, 0.4_b) \rangle$, $G_2 = \langle x, (0.4_a, 0.3_b), (0.6_a, 0.7_b) \rangle$, $G_3 = \langle y, (0.5_u, 0.6_v), (0.5_u, 0.4_v) \rangle$ and $G_4 = \langle y, (0.4_u, 0.3_v), (0.6_u, 0.7_v) \rangle$. Then $\tau = \{0_{\sim}, G_1, G_2, 1_{\sim}\}$ and $\sigma = \{0_{\sim}, G_3, G_4, 1_{\sim}\}$ are IFTs on X and Y respectively. Define a mapping $f: (X, \tau) \rightarrow (Y, \sigma)$ by $f(a) = u$ and $f(b) = v$.

IF γ O(X) = $\{0_{\sim}, 1_{\sim}, \mu_a \in [0,1], \mu_b \in [0,1], \nu_a \in [0,1], \nu_b \in [0,1] / \text{either } \nu_a < 0.4 \text{ or } \nu_b < 0.3, \nu_a \geq 0.5 \text{ whenever } \nu_b < 0.6, 0.4 \leq \nu_a \leq 0.5 \text{ whenever } \nu_b \leq 0.4, \mu_a \geq 0.5, \mu_b \geq 0.6, 0.5 \leq \nu_a < 0.6 \text{ whenever } \nu_b \geq 0.6, \mu_a \geq 0.4, \mu_b \geq 0.3 \text{ and } \nu_a \geq 0.6 \text{ whenever } \nu_b \geq 0.4, 0 \leq \mu_a + \nu_a \leq 1 \text{ and } 0 \leq \mu_b + \nu_b \leq 1\}$.

IF γ C(X) = $\{0_{\sim}, 1_{\sim}, \mu_a \in [0,1], \mu_b \in [0,1], \nu_a \in [0,1], \nu_b \in [0,1] / \text{either } \mu_a < 0.4 \text{ or } \mu_b < 0.3, \mu_a \geq 0.5 \text{ whenever } \mu_b < 0.6, 0.4 \leq \mu_a \leq 0.5 \text{ whenever } \mu_b \leq 0.4, \nu_a \geq 0.5, \nu_b \geq 0.6, 0.5 \leq \mu_a < 0.6 \text{ whenever } \mu_b \geq 0.6, \nu_a \geq 0.4, \nu_b \geq 0.3 \text{ and } \mu_a \geq 0.6 \text{ whenever } \mu_b \geq 0.4, 0 \leq \mu_a + \nu_a \leq 1 \text{ and } 0 \leq \mu_b + \nu_b \leq 1\}$.

IF γ O(Y) = $\{0_{\sim}, 1_{\sim}, \mu_a \in [0,1], \mu_b \in [0,1], \nu_a \in [0,1], \nu_b \in [0,1] / \text{either } \nu_a < 0.4 \text{ or } \nu_b < 0.3, \nu_a \geq 0.5 \text{ whenever } \nu_b < 0.6, 0.4 \leq \nu_a \leq 0.5 \text{ whenever } \nu_b \leq 0.4, \mu_a \geq 0.5, \mu_b \geq 0.6, 0.5 \leq \nu_a < 0.6 \text{ whenever } \nu_b \geq 0.6, \mu_a \geq 0.4, \mu_b \geq 0.3 \text{ and } \nu_a \geq 0.6 \text{ whenever } \nu_b \geq 0.4, 0 \leq \mu_a + \nu_a \leq 1 \text{ and } 0 \leq \mu_b + \nu_b \leq 1\}$.

IF γ C(Y) = $\{0_{\sim}, 1_{\sim}, \mu_a \in [0,1], \mu_b \in [0,1], \nu_a \in [0,1], \nu_b \in [0,1] / \text{either } \mu_a < 0.4 \text{ or } \mu_b < 0.3, \mu_a \geq 0.5 \text{ whenever } \mu_b < 0.6, 0.4 \leq \mu_a \leq 0.5 \text{ whenever } \mu_b \leq 0.4, \nu_a \geq 0.5, \nu_b \geq 0.6, 0.5 \leq \mu_a < 0.6 \text{ whenever } \mu_b \geq 0.6, \nu_a \geq 0.4, \nu_b \geq 0.3 \text{ and } \mu_a \geq 0.6 \text{ whenever } \mu_b \geq 0.4, 0 \leq \mu_a + \nu_a \leq 1 \text{ and } 0 \leq \mu_b + \nu_b \leq 1\}$.

Here f is an IF continuous mapping but not an IF quasi γ G continuous mapping. Since $G_3 = \langle y, (0.5_u, 0.6_v), (0.5_u, 0.4_v) \rangle$ is an IF γ GCS in Y but $f^{-1}(G_3)$ is not an IFCS in X .

Theorem 3.4: Every IF quasi γ G continuous mapping is an IF semi continuous mapping but not conversely in general.

Proof: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IF quasi γ G continuous mapping. Let A be an IFCS in Y . Since every IFCS is an IF γ GCS in Y , A is an IF γ GCS in Y . Then by hypothesis $f^{-1}(A)$ is an IFCS in X . Since every IFCS is an IFSCS, $f^{-1}(A)$ is an IFSCS in X . Hence f is an IF semi continuous mapping.

Example 3.5: In Example 3.3, f is an IF semi continuous mapping but not an IF quasi γ G continuous mapping.

Theorem 3.6: Every IF quasi γ G continuous mapping is an IF pre continuous mapping but not conversely in general.

Proof: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IF quasi γG continuous mapping. Let A be an IFCS in Y . Since every IFCS is an IF γ GCS in Y , A is an IF γ GCS in Y . Then by hypothesis $f^{-1}(A)$ is an IFCS in X . Since every IFCS is an IFPCS, $f^{-1}(A)$ is an IFPCS in X . Hence f is an IF pre continuous mapping.

Example 3.7: In Example 3.3, f is an IF pre continuous mapping but not an IF quasi γG continuous mapping.

Theorem 3.8: Every IF quasi γG continuous mapping is an IF α continuous mapping but not conversely in general.

Proof: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IF quasi γG continuous mapping. Let A be an IFCS in Y . Since every IFCS is an IF γ GCS in Y , A is an IF γ GCS in Y . Then by hypothesis $f^{-1}(A)$ is an IFCS in X . Since every IFCS is an IF α CS, $f^{-1}(A)$ is an IF α CS in X . Hence f is an IF α continuous mapping.

Example 3.9: In Example 3.3, f is an IF α continuous mapping but not an IF quasi γG continuous mapping.

Theorem 3.10: Every IF quasi γG continuous mapping is an IF γ continuous mapping but not conversely in general.

Proof: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IF quasi γG continuous mapping. Let A be an IFCS in Y . Since every IFCS is an IF γ GCS in Y , A is an IF γ GCS in Y . Then by hypothesis $f^{-1}(A)$ is an IFCS in X . Since every IFCS is an IF γ CS, $f^{-1}(A)$ is an IF γ CS in X . Hence f is an IF γ continuous mapping.

Example 3.11: In Example 3.3, f is an IF γ continuous mapping but not an IF quasi γG continuous mapping.

Theorem 3.12: Every IF quasi γG continuous mapping is an IF γG continuous mapping but not conversely in general.

Proof: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IF quasi γG continuous mapping. Let A be an IFCS in Y . Since every IFCS is an IF γ GCS in Y , A is an IF γ GCS in Y . Then by hypothesis $f^{-1}(A)$ is an IFCS in X . Since every IFCS is an IF γ GCS, $f^{-1}(A)$ is an IF γ GCS in X . Hence f is an IF γG continuous mapping.

Example 3.13: In Example 3.3, f is an IF γG continuous mapping but not an IF quasi γG continuous mapping.

Theorem 3.14: Every IF quasi γG continuous mapping is an IF γG continuous mapping but not conversely in general.

Proof: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IF quasi γG continuous mapping. Let A be an IFRC in Y . Since every IFRC is an IF γ GCS in Y , A is an IF γ GCS in Y . Then by hypothesis $f^{-1}(A)$ is an IFCS in X . Since every IFCS is an IF γ GCS, $f^{-1}(A)$ is an IF γ GCS in X . Hence f is an IF γG continuous mapping.

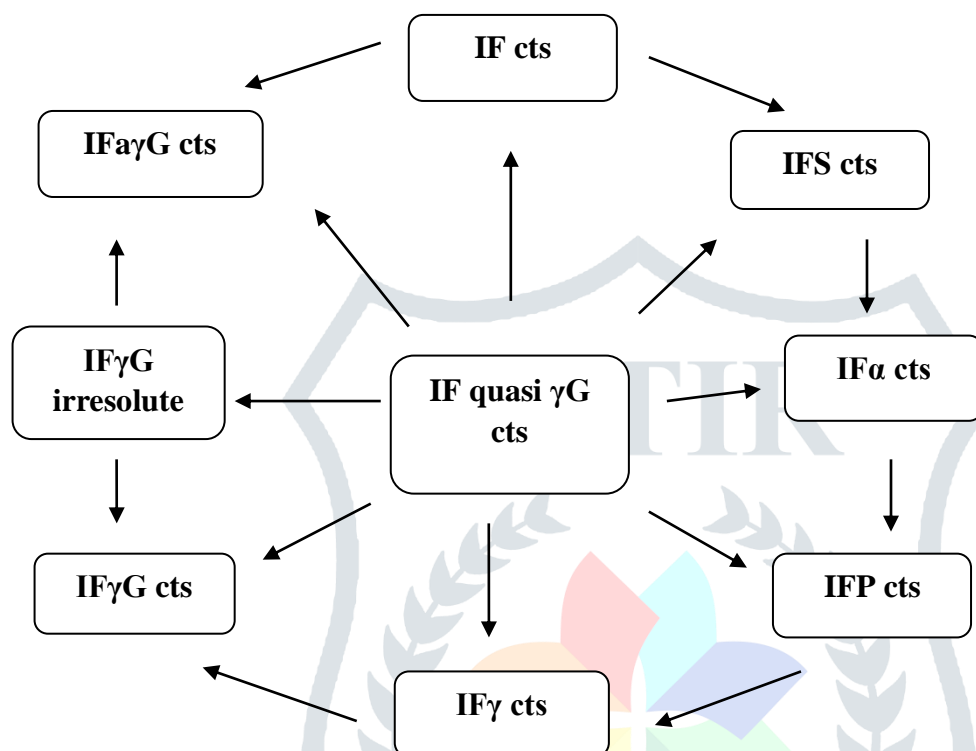
Example 3.15: In Example 3.3, f is an IF γG continuous mapping but not an IF quasi γG continuous mapping.

Theorem 3.16: Every IF quasi γG continuous mapping is an IF γG irresolute mapping but not conversely in general.

Proof: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IF quasi γG continuous mapping. Let A be an IF γ GCS in Y . Then $f^{-1}(A)$ is an IFCS in X by hypothesis. Since every IFCS is an IF γ GCS, $f^{-1}(A)$ is an IF γ GCS in X . Hence f is an IF γ G irresolute mapping.

Example 3.17: In Example 3.3, f is an IF γ G irresolute mapping but not an IF quasi γG continuous mapping.

The relation between various types of intuitionistic fuzzy continuous mapping is given in the following diagram. In this diagram 'cts' means continuous mappings.



The reverse implications are not true in general in the above diagram.

Theorem 3.18: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be a mapping. Then the following statements are equivalent:

- (i) f is an IF quasi γG continuous mapping.
- (ii) $f^{-1}(A)$ is an IFOS in X for every IF γ GOS A in Y .

Proof: Proof is obvious as $f^{-1}(A^c) = (f^{-1}(A))^c$

Theorem 3.19: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IF quasi γG continuous mapping then $f(\text{cl}(A)) \subseteq \gamma \text{cl}(f(A))$ for every IFS A in X .

Proof: Let A be an IFS in X . Then $\gamma \text{cl}(f(A))$ is an IF γ GCS in Y . Since f is an IF quasi γG continuous mapping, $f^{-1}(\gamma \text{cl}(f(A)))$ is an IFCS in X . Clearly $A \subseteq f^{-1}(f(A)) \subseteq f^{-1}(\gamma \text{cl}(f(A)))$. Therefore $\text{cl}(A) \subseteq \text{cl}(f^{-1}(\gamma \text{cl}(f(A)))) = f^{-1}(\gamma \text{cl}(f(A)))$. Hence $f(\text{cl}(A)) \subseteq f(f^{-1}(\gamma \text{cl}(f(A)))) \subseteq \gamma \text{cl}(f(A))$.

Theorem 3.20: If (Y, σ) is an IF $\gamma T_{1/2}$ space, then a mapping $f: (X, \tau) \rightarrow (Y, \sigma)$ is an IF quasi γG continuous mapping if and only if $f^{-1}(\gamma \text{int}(B)) \subseteq \text{int}(f^{-1}(B))$ for every IFS B of Y .

Proof: Let f be an IF quasi γG continuous mapping. Let $B \subseteq Y$ be an IFS. Then we have $\gamma \text{int}(B) \subseteq B$ and $f^{-1}(\gamma \text{int}(B)) \subseteq f^{-1}(B)$. Since $\gamma \text{int}(B)$ is an IF γ OS, it is an IF γ GOS. Then by hypothesis $f^{-1}(\gamma \text{int}(B))$ is an IFOS in X . Therefore $f^{-1}(\gamma \text{int}(B)) = \text{int}(f^{-1}(\gamma \text{int}(B))) \subseteq \text{int}(f^{-1}(B))$.

Conversely assume that B is an $IF_{\gamma}GOS$ in Y . Since Y is an $IF_{\gamma} T_{1/2}$ space, B is an $IF_{\gamma}OS$ in Y and then $f^{-1}(B) = f^{-1}(\gamma\text{int}(B)) \subseteq \text{int}(f^{-1}(B)) \subseteq f^{-1}(B)$. Therefore $f^{-1}(B)$ is an $IFOS$ in X . Hence f is an IF quasi γG continuous mapping.

Theorem 3.21: Let Y be an $IF_{\gamma} T_{1/2}$ space. If an bijective mapping $f: (X, \tau) \rightarrow (Y, \sigma)$ is an IF quasi γG continuous mapping, then $\gamma\text{int}(f(B)) \subseteq f(\text{int}(B))$, for every IFS B of X .

Proof: Let B be an IFS of X . Then $\gamma\text{int}(f(B))$ is an $IF_{\gamma}OS$ in Y and hence is an $IF_{\gamma}GOS$ in Y . By hypothesis $f^{-1}(\gamma\text{int}(f(B)))$ is an $IFOS$ in X . Hence $f^{-1}(\gamma\text{int}(f(B))) \subseteq \text{int}(f^{-1}(\gamma\text{int}(f(B)))) \subseteq \text{int}(f^{-1}(f(B))) = \text{int}(B)$. Now $\gamma\text{int}(f(B)) = f(f^{-1}(\gamma\text{int}(f(B)))) \subseteq f(\text{int}(B))$.

Theorem 3.22: The composition of two IF quasi γG continuous mapping is an IF quasi γG continuous mapping.

Proof: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IF quasi γG continuous mapping and $g: (Y, \sigma) \rightarrow (Z, \delta)$ an IF quasi γG continuous mapping. Let A be an $IF_{\gamma}GCS$ in Z . By hypothesis, $g^{-1}(A)$ is an $IFCS$ in Y and hence is an $IF_{\gamma}GCS$ in Y . Now $f^{-1}(g^{-1}(A)) = (g \circ f)^{-1}(A)$ is an $IFCS$ in X , by hypothesis. Hence $g \circ f$ is an IF quasi γG continuous mapping.

Theorem 3.23: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ and $g: (Y, \sigma) \rightarrow (Z, \delta)$ be any two mappings. Then the following statements hold

- (i) If $f: (X, \tau) \rightarrow (Y, \sigma)$ is an IF continuous mapping and $g: (Y, \sigma) \rightarrow (Z, \delta)$ is an IF quasi γG continuous mapping. Then $g \circ f: (X, \tau) \rightarrow (Z, \delta)$ is an IF quasi γG continuous mapping.
- (ii) If $f: (X, \tau) \rightarrow (Y, \sigma)$ is an IF quasi γG continuous mapping and $g: (Y, \sigma) \rightarrow (Z, \delta)$ is an IF continuous mapping. Then $g \circ f: (X, \tau) \rightarrow (Z, \delta)$ is an IF continuous mapping.
- (iii) If $f: (X, \tau) \rightarrow (Y, \sigma)$ is an IF quasi γG continuous mapping and $g: (Y, \sigma) \rightarrow (Z, \delta)$ is an IF γG continuous mapping. Then $g \circ f: (X, \tau) \rightarrow (Z, \delta)$ is an IF continuous mapping.

Proof: (i) Let A be an $IF_{\gamma}GCS$ in Z . By hypothesis, $g^{-1}(A)$ is an $IFCS$ in Y . Since f is an IF continuous mapping, $f^{-1}(g^{-1}(A)) = (g \circ f)^{-1}(A)$ is an $IFCS$ in X . Hence $g \circ f$ is an IF quasi γG continuous mapping.

(ii) Let A be an $IFCS$ in Z . By hypothesis, $g^{-1}(A)$ is an $IFCS$ in Y . Since every $IFCS$ is an $IF_{\gamma}GCS$, $g^{-1}(A)$ is an $IF_{\gamma}GCS$ in Y . Then $f^{-1}(g^{-1}(A)) = (g \circ f)^{-1}(A)$ is an $IFCS$ in X , by hypothesis. Hence $g \circ f$ is an IF continuous mapping.

(iii) Let A be an $IFCS$ in Z . By hypothesis, $g^{-1}(A)$ is an $IF_{\gamma}GCS$ in Y . Since f is an IF quasi γG continuous mapping, $f^{-1}(g^{-1}(A)) = (g \circ f)^{-1}(A)$ is an $IFCS$ in X . Hence $g \circ f$ is an IF continuous mapping.

Theorem 3.24: If $g: (Y, \sigma) \rightarrow (Z, \delta)$ is an IF γG irresolute mapping and $f: (X, \tau) \rightarrow (Y, \sigma)$ is an IF quasi γG continuous mapping, then $g \circ f: (X, \tau) \rightarrow (Z, \delta)$ is an IF quasi γG continuous mapping.

Proof: Let B be an $IF_{\gamma}GCS$ in Z . By hypothesis, $g^{-1}(A)$ is an $IF_{\gamma}GCS$ in Y . Since f is an IF quasi γG continuous mapping, $f^{-1}(g^{-1}(A)) = (g \circ f)^{-1}(A)$ is an IFCS in X . Hence $g \circ f$ is an IF quasi γG continuous mapping.

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