



FUZZY rh-SUPER IRRESOLUTE MAPPING

¹Dr.P.Thamil selvi, ²G.M.Kohila Gowri, ³P.Kavitha

^{1&2 &3}Assistant professor, Department of Mathematics

^{1 &2 &3} Parvathy's Arts and science College, Madurai kamaraj university
Dindigul-624002, Tamil Nadu, India.

Abstract: In this paper the concept of fuzzy rh -super irresolute mappings have been introduced and explore some of its basic properties in fuzzy Topological Space.

Keywords: fuzzy topology, fuzzy super closure, Fuzzy Super Interior fuzzy rh - super closed sets and fuzzy rh - super open sets, fuzzy rh -super continuous and fuzzy rh -super irresolute mappings

I.INTRODUCTION

Let Y be a non empty set and $I = [0,1]$. A fuzzy set on Y is a mapping from Y in to I . The null fuzzy set 0 is the mapping from X in to I which assumes only the value is 0 and whole fuzzy sets 1 is a mapping from Y on to I which takes the values 1 only. The union (resp. intersection) of a family $\{A_\alpha: \alpha \in \Lambda\}$ of fuzzy sets of X is defined by to be the mapping $\sup P_\alpha$ (resp. $\inf P_\alpha$). A fuzzy set P of Y is contained in a fuzzy set R of Y if $P(y) \leq Q(y)$ for each $x \neq y$. A fuzzy point y_α in Y is a fuzzy set defined by $x_\beta(x) = \alpha$ for $y = x$ and $y(x) = 0$ for $x \neq y$, $\alpha \in [0,1]$ and $x \in y$. A fuzzy point y_α is said to be quasi-coincident with the fuzzy set P denoted by $x_{\alpha q}P$ if and only if $\alpha + P(y) > 1$. A fuzzy set P is quasi coincident with a fuzzy set R denoted by P_qR if and only if there exists a point $y \in Y$ such that $P(y) + R(y) > 1$. $P \leq R$ if and only if (P_qR^c) . A family τ of fuzzy sets of y is called a fuzzy topology [2] on Y if $0,1$ belongs to τ and τ is super closed with respect to arbitrary union and finite intersection. The members of τ are called fuzzy super open sets and their complement are fuzzy super closed sets. For any fuzzy set P of Y the closure of P (denoted by $cl(P)$) is the intersection of all the fuzzy super closed super sets of P and the interior of P (denoted by $int(P)$) is the union of all fuzzy super open subsets of P .

Definition 1.1 [5,10,11,12]: Let (Y, τ) fuzzy topological space and $P \leq Y$ then

1. Fuzzy Super closure $scl(P) = \{y \in Y: cl(U) \cap P \neq \emptyset\}$
2. Fuzzy Super interior $sint(P) = \{y \in Y: cl(U) \leq P \neq \emptyset\}$

Definition 1.2[5, 10,11,12]: A fuzzy set P of a fuzzy topological space (Y, τ) is called:

- (a) Fuzzy super closed if $scl(P) \leq P$.
- (b) Fuzzy super open if $1-P$ is fuzzy super closed $sint(P) = P$

Remark 1.1[5, 10,11,12]: Every fuzzy closed set is fuzzy super closed but the converses may not be true. **Remark 1.2[5, 10,11,12]:** Let P and Q are two fuzzy super closed sets in a fuzzy topological space (Y, \mathfrak{T}) , then $P \cup Q$ is fuzzy super closed.

Remark 1.3[5]: The intersection of two fuzzy super closed sets in a fuzzy topological space (Y, \mathfrak{T}) may not be fuzzy super closed.

Definition 1.3: A fuzzy set P of an fuzzy topological space (Y, \mathfrak{T}) is said to be :-

- (a) fuzzy regular super open if $P = int(cl(P))$ [7].
- (b) fuzzy h-super closed if $cl(P) \leq O$ whenever $P \leq O$ and O is an fuzzy super open set.[14]
- (c) fuzzy h-super open if P^c is fuzzy g-closed.[14]
- (d) fuzzy rh-super closed if $cl(P) \leq O$ whenever $P \leq O$ and O is an fuzzy regular super open set.[16]
- (e) fuzzy rh-super open if P^c is fuzzy mg-closed.[16]

Remark 1.3: Every fuzzy super closed set is fuzzy h-super closed and every fuzzy h-super closed set is fuzzy rh-super closed but the converse may not be true.[14,16]

Definition 1.4: A mapping $f: (Y, \mathfrak{T}) \rightarrow (X, \mu)$ is said to be :

1. Fuzzy h-super continuous if the pre image of every fuzzy super closed set of X is fuzzy h-super closed in Y . [15].
2. Fuzzy rh-super continuous if the pre image of every fuzzy super closed set of X is fuzzy rh-super closed in Y . [17]

Remark 1.4: Every fuzzy super continuous mapping is fuzzy h-super continuous and every fuzzy h-super continuous mapping is fuzzy rh-super continuous but the converse may not be true.[17]

Definition 1.5: A collection $\{F_\beta: \beta \in \Lambda\}$ of fuzzy mg-super open sets in a fuzzy topological space (Y, \mathfrak{T}) is called a fuzzy rh-super open cover of a fuzzy set P of Y if $P \leq \cup\{F_\beta: \beta \in \Lambda\}$. [16]

Definition 1.6: A fuzzy topological space (Y, \mathfrak{T}) is said to be fuzzy rh - super compact if every fuzzy rh-super open cover of Y has a finite subcover. [16]

Definition 1.7: A fuzzy set A of a fuzzy topological space (Y, \mathfrak{T}) is said to be fuzzy rh- super compact relative to Y if every collection $\{F_\beta: \beta \in \Lambda\}$ of fuzzy rh-super open subsets of Y such that $P \leq \cup\{F_\beta: \beta \in \Lambda\}$ there exists a finite subset Λ_0 such that $A \leq \cup\{F_\beta: \beta \in \Lambda_0\}$. [16]

Definition 1.8: A fuzzy topological space Y is fuzzy rh-connected if there is no proper fuzzy set of Y which is both fuzzy rh-super open and fuzzy mg-closed. [17]

II. FUZZY RH -SUPER IRRESOLUTE MAPPINGS

Definition 2.1: A mapping f from a fuzzy topological space (Y, \mathfrak{T}) to another fuzzy topological space (X, μ) is said to be fuzzy rh -super irresolute if the pre image of every fuzzy rh-super closed set of X is fuzzy rh -super closed in Y .

Theorem 2.1: A mapping $f : (Y, \mathfrak{T}) \rightarrow (X, \mu)$ is fuzzy rh -super irresolute if and only if the pre image of every fuzzy rh -super open set in X is fuzzy rh -super open in Y .

Proof: It is obvious because $f^{-1}(U^c) = (f^{-1}(U))^c$, for every fuzzy set U of Y .

Remark 2.1: Every fuzzy h-super closed set is fuzzy rh -super closed it is clear that every fuzzy rh -super irresolute mapping is fuzzy rh -super continuous but the converse may not be true.

Definition 2.2: A mapping $f : (Y, \mathfrak{T}) \rightarrow (X, \mu)$ is said to be fuzzy regular super open if the image of every fuzzy regular super open set of X is fuzzy regular super open set in Y .

Theorem 2.2: Let $f : (Y, \mathfrak{T}) \rightarrow (X, \mu)$ be bijective fuzzy regular super open and fuzzy rh-super continuous then f is fuzzy rh -super irresolute.

Proof: Let P be a fuzzy mg-super closed set in X and let $f^{-1}(P) \leq F$ where F is fuzzy regular super open set in Y . Then $P \leq f(F)$. Since f is fuzzy regular super open and P is fuzzy rh-super closed in X , $cl(P) \leq f(F)$ and $f^{-1}(cl(P)) \leq F$. Since f is fuzzy mg-super continuous and $cl(P)$ is fuzzy super closed in X , $cl(f^{-1}(cl(P))) \leq F$. And so $cl(f^{-1}(P)) \leq F$. Therefore $f^{-1}(P)$ is fuzzy rh-super closed in Y . Hence f is fuzzy rh -irresolute.

Theorem 2.3: Let $f : (Y, \mathfrak{T}) \rightarrow (X, \mu)$ and $g : (X, \mu) \rightarrow (Z, \eta)$ be two fuzzy rh -super irresolute mappings, then $g \circ f : (Y, \mathfrak{T}) \rightarrow (Z, \eta)$ is fuzzy rh -super irresolute.

Proof: Obvious.

Theorem 2.4: Let $f : (Y, \mathfrak{T}) \rightarrow (X, \mu)$ is fuzzy rh -super irresolute mapping, and if Q is fuzzy rh- super compact relative to Y , then the image $f(Q)$ is fuzzy rh -super compact relative to X .

Proof: Let $\{P_i: i \in \Lambda\}$ be any collection of fuzzy rh-super open set of X such that $f(Q) \leq \cup\{P_i: i \in \Lambda\}$. Then $Q \leq \cup\{f^{-1}(P_i): i \in \Lambda\}$. By using the assumption, there exists a finite subset Λ_0 of Λ such that $Q \leq \cup\{f^{-1}(P_i): i \in \Lambda_0\}$. Therefore, $f(Q) \leq \cup\{P_i: i \in \Lambda_0\}$. Which shows that $f(Q)$ is fuzzy rh- super compact relative to X .

Theorem 2.5: A fuzzy rh-super irresolute image of a fuzzy rh- super compact space is fuzzy rh-compact.

Proof: Obvious.

Theorem 2.6: If the product space $(Y \times X, \mathfrak{T} \times \mu)$ of two non- empty fuzzy topological spaces (Y, \mathfrak{T}) and (X, μ) is fuzzy rh -super compact, then each factor space is fuzzy rh- super compact.

Proof: Obvious.

Theorem 2.7: Let $f : (Y, \mathfrak{T}) \rightarrow (X, \mu)$ is a fuzzy rh -super irresolute surjection and (Y, \mathfrak{T}) is fuzzy rh -super connected, then (X, μ) is fuzzy rh -super connected.

Proof: Suppose Y is not fuzzy rh -connected then there exists a proper fuzzy set G of Y which is both fuzzy rh -super open and fuzzy rh -closed, therefore $f^{-1}(G)$ is a proper fuzzy set of X , which is both fuzzy rh -super open and fuzzy rh -closed, because f is fuzzy rh -super continuous surjection. Therefore X is not fuzzy rh -connected, which is a contradiction. Hence Y is fuzzy rh -super connected.

III. REFERENCES

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