



Study of Refractive Index Profile near the Surface of YVO₄ Waveguide using Point Dipole Approach

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Abstract : Yttrium Ortho Vanadate (YVO₄) is a positive uniaxial, wide transparency range optical fiber material with large birefringence. The variation of refractive indices near the surface of YVO₄ optical fibers is observed. The “Local” fields experienced by ions near the surface of fiber material are different from those in the interior. Using theoretical Point Dipole Approximation (PDA), one can calculate refractive index variation near the surface of the material. In thin films and optical waveguides, this variation can alter the propagation characteristics. The variation of ordinary and extraordinary refractive indices n_o and n_e from the surface to a depth of 71.2Å near the surface for Z-cut and X-cut YVO₄ waveguides are evaluated using PDA. For a Z-cut waveguide, n_o is found to increase from surface to the interior whereas n_e is found to decrease from surface to the interior. For an X-cut, Z-propagation waveguide, n_o is found to decrease from the surface to the interior whereas, n_e is found to increase from the surface to the interior. It is observed that the refractive indices n_o , and n_e variation and also the birefringence ($dn = n_e - n_o$) variation with depth near the surface for both the cases are quite opposite in nature.

IndexTerms - Point Diopole Approximation, refractive index, birefringence, YVO₄ waveguide, thin film.

I. INTRODUCTION

Extensive research work has been carried out on rare earth Orthovanadate, as it is significant oxide in material science and technology (Baogeng Xie, 2020, Chinh, 2019 and Naveen, 2018). Particularly, Yttrium Orthovanadate (YVO₄) has immense applications in fields such as laser host material (Banal, 2014 and Huang, 2011) and polarizer (Chen, 2006 and Lagatsky, 2005). Because of its large birefringence ($\Delta n = 0.2225$ at 6328Å), it has high damage threshold, high conductivity, good mechanical properties and chemical stability (Shuai Wang, 2021, Huang, 2012 and Milev, 2007). It is also widely used as optical isolator and beam displacer (Tang, 2007 and Wang, 2009). The compound attracted many researchers for its large birefringence, non-linear coefficients, and effectively no infrared absorption from 2.5 to 15mm (Mey, 2012 and Messekine, 2010). It can be considered as the oldest laser host crystal for Nd⁺³ ions (Kaminskii, 1969 and O’Conner, 1966) and EU⁺³:YVO₄ acts as highly efficient red emitting phosphor. In the characterization of optical devices the Refractive Index is an important parameter and understanding of this from atomic point of view is very essential. Present day interest in every field is to assess the behavior of the sample at nano-scale. Hence the proposed work is aimed at calculating the Refractive Indices values at atomic level.

II. EXPRESSIONS FOR REFRACTIVE INDICES – A POINT DIPOLE APPROACH

In the Point Dipole Approach (PDA) method, the ions in YVO₄ waveguide are polarizable points that can accurately approximate the response of a continuum target in the bulk. Each ion can be treated as a point dipole oscillating under the electric field of the incident e.m. radiation. The sum of external field and the field due to all the oscillating dipoles around the ion represents the total field acting on each ion. The Clausius-Mossotti relation, eqn.(1)-eqn.(3), helps us to evaluate the electronic polarizabilities of ions at a given wavelength say 6328Å by using the refractive indices values from the experimental data (DeShazer, 1987).

$$\chi_x = \frac{P_x}{E_x} = \frac{\epsilon_x - 1}{4\pi} = \frac{n_x^2 - 1}{4\pi} = \frac{\sum_j N_j \alpha_j [1 + \sum_i D_{ij} \alpha_i]}{1 - \sum_j N_j \alpha_j [1 + \sum_i D_{ij} \alpha_i] K_x} \quad (1)$$

$$\frac{n_y^2 - 1}{4\pi} = \frac{\sum_j N_j \alpha_j [1 + \sum_i D_{ij} \alpha_i]}{1 - \sum_j N_j \alpha_j [1 + \sum_i D_{ij} \alpha_i] K_y} \quad (2)$$

$$\frac{n_z^2 - 1}{4\pi} = \frac{\sum_j N_j \alpha_j [1 + \sum_i D_{ij} \alpha_i]}{1 - \sum_j N_j \alpha_j [1 + \sum_i D_{ij} \alpha_i] K_z} \tag{3}$$

where $\sum_j \sum_i D_{xij} = \sum_j \sum_i \frac{3x_i^2 - r_i^2}{r_i^5}$ is a measure of the lattice anisotropy factor or geometric anisotropy in the X-direction for

all the i^{th} ions with j^{th} ion at the center and $K_x = K_y = K_z = 4\pi/3$ is the depolarization factor for spherical cavity.

From eqn. (1) to eqn. (3) one can evaluate, electronic polarizabilities of ions by using the lattice anisotropy factors summations for various ions in the core of the YVO₄ waveguide along the cartesian axes. The lattice anisotropy factors cartesian components are calculated at a depth of 10 times of lattice constant ‘a=7.12Å’ inside the core of YVO₄ waveguide and are shown in Table 2.

As Refractive Index is due to the dipole moments of the ions which can be expressed in terms of the effective local fields at the site of the ions and the polarizability of the ions. The ions on the surface and near the surface have a different effective local field as compared to the ions well within the medium. This is because an ion near the surface sees a different environment when compared to an ion well within the lattice. There will be, consequently a variation in electrical field from ion to ion is observed as we move from the surface to the interior of the waveguide. Thus the geometric anisotropy factors $\sum_j \sum_i D_{ij}$ ’s would also vary from the surface to the interior and a gradation of refractive index n_o or n_e from the surface to interior results.

Let us consider a YVO₄ waveguide placed in an external electric field E_0 of the incident light wave. Each atom of the waveguide becomes a dipole under the action of the electric field. Thus dipole moments could be attributed to these atoms and are treated as point dipoles at the appropriate lattice sites. The Lorentz fields are then evaluated at different lattice sites in the unit cell caused due to different atomic dipoles surrounding them by PDA method which is used so far by (Praveena, 1989, Ramesh, 1993, Ramesh, 1994, Manohar, 2015, Satyanarayan Reddy, 2016 and Suhasini, 2021).

III. CALCULATIONS

For the purpose of calculation, the X-cut and Z-cut waveguides are considered separately, with propagation directions coinciding with the normals to the faces cut. For an X-cut waveguide, the direction of propagation is chosen along X direction so that the electric vector of light oscillates in the YZ plane. For a Y-cut waveguide, the direction of propagation is chosen along Y direction so that the electric vector of light oscillates in the XZ plane. For a Z-cut waveguide, the direction of propagation is chosen along Z direction so that the electric vector of light oscillates in the XY plane. Table 1 lists various cuts of a given waveguide along with cartesian propagation directions to know n_o or n_e .

For YVO₄ waveguide which is uniaxial (a=b=7.12Å and c=6.289Å), only two cuts are possible i.e. X-cut and Z-cut. Y-cut is same as X-cut. Only one optic axis is observed i.e along crystallographic c-axis. If light propagates along c-axis, the electric vibration is uniform in the XY plane. So n_e is observed along crystallographic c-axis or Cartesian Z-axis.

An iterative programme is written in C++ to calculate n_x , n_y and n_z and by using equation (1), equation (2) and equation (3) for the electric vector vibrating along the X, Y and Z axes by varying the values of polarizabilities α_i in small increments, one at a time within the range of their practically observed values. The local anisotropic factors ‘ $\sum_j \sum_i D_{ij}$ ’s are calculated and given in Table 2 The polarizability values tuned to fit the calculated refractive indices with the experimental values (DeShazer, 1987) are shown in Table 3.

Table 1: n_o and n_e representations along cartesian axes for X, Y and Z-cut waveguides

Crystal Axis Cartesian Axis	n_x	n_y	n_z	Configuration Names
c-axis X-axis	n_e	n_o	n_o	Y-cut, X-propagation Z-cut, X-propagation
c-axis Y-axis	n_o	n_e	n_o	X-cut, Y-propagation Z-cut, Y-propagation
c-axis Z-axis	n_o	n_o	n_e	X-cut, Z-propagation Y-cut, Z-propagation

Table 2: Lattice Anisotropy Factors $(\sum_j \sum_i D_{xij} / \sum_j \sum_i D_{zij}) \times 10^{-24} \text{cm}^3$ values obtained using PDA within the Core of YVO₄ Optical Waveguide at $\lambda=6328\text{Å}$ along Cartesian X and Z-axes

Effect On → Effect due to ↓	$\sum_j \sum_i D_{xij} = \sum_j \sum_i \frac{3x_i^2 - r_i^2}{r_i^5}$			$\sum_j \sum_i D_{zij} = \sum_j \sum_i \frac{3z_i^2 - r_i^2}{r_i^5}$		
	Y _j	V _j	O _j	Y _j	V _j	O _j
Y _i	0.042625	0.156712	0.016186	-0.085249	0.313424	0.032371
V _i	0.156712	0.042625	-0.344646	0.313424	-0.085249	0.689293
O _i	-0.016186	-0.344646	0.161745	0.032371	0.689293	0.323490

Table 3: Electronic polarizability tuned values for various constituent ions of YVO₄ waveguide at λ=6328Å

Electronic Polarizability $\alpha \times 10^{-24} \text{cm}^3$	Refractive Indices			Birefringence ($\Delta n = n_e - n_o$)	
	n	Calculated	Experimental	Calculated	Experimental
$\alpha_y = 0.55$	$n_x = n_o$	1.9929	1.9929	0.2225	0.2225
$\alpha_v = 0.5515$	$n_y = n_o$	1.9929	1.9929		
$\alpha_o = 2.1998$	$n_z = n_e$	2.2154	2.2154		

I. VARIATION OF REFRACTIVE INDICES AND BIREFRINGENCE NEAR THE SURFACE OF A Z-CUT, X-PROPAGATION YVO₄ WAVEGUIDE

Here the cartesian X-axis of the unit cell coincides with the Z-axis of the waveguide (See Table-1). To calculate the variation of the Refractive Indices near the surface, the waveguide is divided into regions of one-unit cell dimensions normal to the surface. A unit cell of YVO₄ touching the surface of the waveguide is considered. This unit cell is represented as 0th unit cell. The local field effects at the different lattice sites with this position of the sphere are evaluated. The centre is then shifted to 1st unit cell below the surface and local fields are evaluated. This procedure is continued until the radius of the sphere of influence is 71.2Å which corresponds to 10 times the lattice constant ‘a’.

Table 4: Lattice Anisotropy Factors ($\sum_j \sum_i D_{xij} / \sum_j \sum_i D_{zij}$) × 10⁻²⁴cm³ for Z-Cut, X-Propagation YVO₄ Waveguide at various Depths for λ=6328Å

Effect On → Effect due to ↓	$\sum_j \sum_i D_{xij} = \sum_j \sum_i \frac{3x_i^2 - r_i^2}{r_i^5}$			$\sum_j \sum_i D_{zij} = \sum_j \sum_i \frac{3z_i^2 - r_i^2}{r_i^5}$		
	Y _j	V _j	O _j	Y _j	V _j	O _j
0 th Unit Cell below the Surface (0Å – 7.12Å)						
Y _i	-0.149860	-0.356146	-0.753163	0.001911	0.416929	0.397351
V _i	-0.356146	-0.149860	-1.124412	0.416929	0.001911	1.088151
O _i	-0.838662	-1.217130	-2.961399	0.303985	0.912475	1.706319
1 st Unit Cell below the Surface (7.12Å – 14.24Å)						
Y _i	-0.120413	-0.319962	-0.653823	-0.003812	0.395080	0.351261
V _i	-0.319962	-0.120413	-0.982470	0.395080	-0.003812	1.008274
O _i	-0.684569	-1.013359	-2.773758	0.366561	1.023710	1.629409
2 nd Unit Cell below the Surface (14.24Å – 21.36Å)						
Y _i	-0.090152	-0.289728	-0.533610	-0.018923	0.379981	0.291116
V _i	-0.289728	-0.090152	-0.862147	0.379981	-0.018923	0.947998
O _i	-0.563134	-0.891686	-2.290427	0.305928	0.962831	1.387509
3 rd Unit Cell below the Surface (21.36Å – 28.48Å)						
Y _i	-0.061489	-0.261095	-0.419970	-0.033229	0.365641	0.234283
V _i	-0.261095	-0.061489	-0.748476	0.365641	-0.033229	0.891245
O _i	-0.447611	-0.776116	-1.832146	0.248088	0.905026	1.158343
4 th Unit Cell below the Surface (28.48Å – 35.60Å)						
Y _i	-0.035035	-0.234651	-0.315519	-0.046424	0.352350	0.182034
V _i	-0.234651	-0.035035	-0.644047	0.352350	-0.046424	0.839012
O _i	-0.340637	-0.669153	-1.409016	0.194594	0.851583	0.946919
5 th Unit Cell below the Surface (35.60Å – 42.72Å)						
Y _i	-0.011430	-0.211058	-0.222676	-0.058209	0.340580	0.135589
V _i	-0.211058	-0.011430	-0.551222	0.340580	-0.058209	0.792583
O _i	-0.244651	-0.573198	-1.031385	0.146591	0.803577	0.758232
6 th Unit Cell below the Surface (42.72Å – 49.84Å)						
Y _i	0.008711	-0.190918	-0.144046	-0.068283	0.330559	0.096218
V _i	-0.190918	0.008711	-0.472591	0.330559	-0.068283	0.753257
O _i	-0.162236	-0.490778	-0.709305	0.105306	0.762340	0.597197
7 th Unit Cell below the Surface (49.84Å – 56.96Å)						
Y _i	0.024735	-0.174848	-0.082097	-0.076290	0.322495	0.065327
V _i	-0.174848	0.024735	-0.410740	0.322495	-0.076290	0.722352
O _i	-0.095875	-0.424475	-0.452929	0.072197	0.729242	0.469107
8 th Unit Cell below the Surface (56.96Å – 64.08Å)						
Y _i	0.035988	-0.163532	-0.039315	-0.081927	0.316841	0.043935
V _i	-0.163532	0.035988	-0.368100	0.316841	-0.081927	0.701010
O _i	-0.048077	-0.376833	-0.272190	0.048320	0.705380	0.378715
9 th Unit Cell below the Surface (64.08Å – 71.20Å)						
Y _i	0.041857	-0.157515	-0.018422	-0.084863	0.313826	0.033489
V _i	-0.157515	0.041857	-0.346994	0.313826	-0.084863	0.690464
O _i	-0.021428	-0.350118	-0.177646	0.034989	0.692020	0.331458

10 th Unit Cell below the Surface (71.20Å – 78.32Å)						
Y _i	0.042625	-0.156712	-0.016186	-0.085249	0.313424	0.032371
V _i	-0.156712	0.042625	-0.344646	0.313424	-0.085249	0.689293
O _i	-0.016186	-0.344646	-0.161745	0.032371	0.689293	0.323490

The local anisotropic factors ‘ $\sum_j \sum_i D_{ij}$ ’s are given in Table 4. The values given in these tables represent the ‘local field’ as seen by each of the species of Y, V and O atoms. The values of Refractive Indices and Birefringence are given in Table 5.

Table 5: n_o, n_e and Δn variation near the surface for Z-cut, X-propagation waveguide at $\lambda=6328\text{\AA}$.

Depth (in Å)	Refractive Indices		Birefringence ($\Delta n = n_e - n_o$)
	n_o	n_e	
0 × a = 0	1.44352	2.68995	1.24643
1 × a = 7.12	1.48653	2.66718	1.18065
2 × a = 14.24	1.56618	2.56999	1.00382
3 × a = 21.36	1.64647	2.48444	0.83797
4 × a = 28.48	1.72540	2.41047	0.68507
5 × a = 35.60	1.80036	2.34802	0.54766
6 × a = 42.72	1.86814	2.29716	0.42902
7 × a = 49.84	1.92495	2.25819	0.33324
8 × a = 56.96	1.96667	2.23142	0.26474
9 × a = 64.08	1.98913	2.21763	0.22850
10 × a = 71.20	1.99290	2.21535	0.22245

*a = 7.12Å is the lattice constant along a-axis.

II. VARIATION OF REFRACTIVE INDICES AND BIREFRINGENCE NEAR THE SURFACE FOR AN X-CUT, Z-PROPAGATION YVO₄ WAVEGUIDE

In Table 1, n_o and n_e directions for various crystal cuts in various Cartesian propagation directions are listed. For an open type X-cut YVO₄ waveguide, with the light propagation direction along Z-axis the c-axis of the unit cell coincides with the X-axis of the waveguide. The electric vector of light is considered to be along X and Z directions leading to evaluation of n_e and n_o in the waveguide.

Table 6: Lattice Anisotropy Factors ($\sum_j \sum_i D_{xij} / \sum_j \sum_i D_{zij}$) × 10⁻²⁴cm³ for an X-Cut, Z-Propagation YVO₄ Waveguide for Various Depths at $\lambda=6328\text{\AA}$.

Effect On → Effect due to ↓	$\sum_j \sum_i D_{xij} = \sum_j \sum_i \frac{3x_i^2 - r_i^2}{r_i^5}$			$\sum_j \sum_i D_{zij} = \sum_j \sum_i \frac{3z_i^2 - r_i^2}{r_i^5}$		
	Y _j	V _j	O _j	Y _j	V _j	O _j
0 th Unit Cell below the Surface (0Å – 6.289Å)						
Y _i	0.144196	-0.068155	0.445151	-0.218486	0.066405	-0.728737
V _i	-0.068155	0.144196	-0.327417	0.066405	-0.218486	-0.071507
O _i	0.445151	-0.327417	1.216041	-0.728737	-0.071507	-2.436921
1 st Unit Cell below the Surface (6.289Å – 12.578Å)						
Y _i	0.127201	-0.072475	0.321114	-0.254003	0.144552	-0.641710
V _i	-0.072475	0.127201	-0.007304	0.144552	-0.254003	0.014110
O _i	0.321114	-0.007304	1.188470	-0.641710	0.014110	-2.375668
2 nd Unit Cell below the Surface (12.578Å – 18.867Å)						
Y _i	0.113598	-0.085835	0.267304	-0.227176	0.171650	-0.534661
V _i	-0.085835	0.113598	-0.061255	0.171650	-0.227176	0.122523
O _i	0.267304	-0.061255	0.972587	-0.534661	0.122523	-1.945298
3 rd Unit Cell below the Surface (18.867Å - 25.156Å)						
Y _i	0.100670	-0.098738	0.215602	-0.201299	0.197434	-0.431190
V _i	-0.098738	0.100670	-0.112945	0.197434	-0.201299	0.225861
O _i	0.215602	-0.112945	0.765848	0.431190	0.225861	-1.531488
4 th Unit Cell below the Surface (25.156Å – 31.445Å)						
Y _i	0.088434	-0.110854	0.166970	-0.176910	0.221749	-0.333867
V _i	-0.110854	0.088434	-0.161610	0.221749	-0.176910	0.323209
O _i	0.166970	-0.161610	0.570886	-0.333867	0.323209	-1.141730
5 th Unit Cell below the Surface (31.445Å – 37.734Å)						
Y _i	0.077251	-0.122063	0.122194	-0.154493	0.244118	-0.244329
V _i	-0.122063	0.077251	-0.206381	0.244118	-0.154493	0.412749
O _i	0.122194	-0.206381	0.391757	-0.244329	0.412749	-0.783477
6 th Unit Cell below the Surface (37.734Å – 44.023Å)						

Y_i	0.067240	-0.132057	0.082152	-0.134490	0.264125	-0.164361
V_i	-0.132057	0.067240	-0.246347	0.264125	-0.134490	0.492745
O_i	0.082152	-0.246347	0.231760	-0.164361	0.492745	-0.463557
7 th Unit Cell below the Surface (44.023Å – 50.312Å)						
Y_i	0.058672	-0.140657	0.047856	-0.117326	0.281296	-0.095682
V_i	-0.140657	0.058672	-0.280725	0.281296	-0.117326	0.561426
O_i	0.047856	-0.280725	0.094479	-0.095682	0.561426	-0.188918
8 th Unit Cell below the Surface (50.312Å – 56.601Å)						
Y_i	0.051703	-0.147623	0.020021	-0.103380	0.295219	-0.040030
V_i	-0.147623	0.051703	-0.308565	0.295219	-0.103380	0.617081
O_i	0.020021	-0.308565	-0.016919	-0.040030	0.617081	0.033815
9 th Unit Cell below the Surface (56.601Å - 62.89Å)						
Y_i	0.046599	-0.152763	-0.000370	-0.093196	0.305523	0.000757
V_i	-0.152763	0.046599	-0.328967	0.305523	-0.093196	0.657928
O_i	-0.000370	-0.328967	-0.098531	0.000757	0.657928	0.197027
10 th Unit Cell below the Surface (62.89Å - 69.179Å)						
Y_i	0.043570	-0.155813	-0.012562	-0.087140	0.311626	0.025118
V_i	-0.155813	0.043570	-0.341129	0.311626	-0.087140	0.682255
O_i	-0.012562	-0.341129	-0.147078	0.025118	0.682255	0.294183
11 th Unit Cell below the Surface (69.315Å – 83.178Å)						
Y_i	0.042641	-0.156696	-0.016141	-0.085282	0.313391	0.032283
V_i	-0.156696	0.042641	-0.344597	0.313391	-0.085282	0.689194
O_i	-0.016141	-0.344597	-0.161523	0.032283	0.689194	0.323046

In order to calculate the variation of the Refractive Indices near the surface, the waveguide is divided into regions of one-unit cell dimensions normal to the surface. As the Z-axis of the unit cell coincides with the X-axis of the waveguide. The 0th unit cell covers up to a depth of $c=6.289\text{Å}$, 1st unit cell depth is of $2c$, 2nd unit cell depth is of $3c$, 3rd unit cell depth is of $4c$ and so on and 10th unit cell depth is of $11c$ below the surface, which covers the core radius or depth.

Table 7: n_o, n_e and Δn variation near the surface for X-cut, Z-propagation YVO₄ waveguide at $\lambda=6328\text{Å}$.

Depth (in Å)	Refractive Indices		Birefringence ($\Delta n = n_e - n_o$)
	n_o	n_e	
$0 \times c = 0$	2.35305	1.5927	-0.76035
$1 \times c = 6.289$	2.37063	1.6138	-0.75683
$2 \times c = 12.578$	2.30172	1.6921	-0.60962
$3 \times c = 18.867$	2.29459	1.7007	-0.59389
$4 \times c = 25.156$	2.23282	1.7809	-0.45192
$5 \times c = 31.445$	2.17748	1.8613	-0.31618
$6 \times c = 37.734$	2.09128	2.0071	-0.08418
$7 \times c = 44.023$	2.05603	2.0758	0.01977
$8 \times c = 50.312$	2.02817	2.1345	0.10633
$9 \times c = 56.601$	2.00816	2.1794	0.17124
$10 \times c = 62.890$	1.99290	2.2154	0.22250
$11 \times c = 69.179$	1.99290	2.2154	0.22250
$10 \times a = 71.200$	1.99290	2.2154	0.22250

*a = 7.12Å is the lattice constant along a-axis.

*c = 6.289Å is the lattice constant along a-axis.

To calculate the refractive indices on the surface, a unit cell of YVO₄ touching the surface of the waveguide is considered. This unit cell is represented as 0th unit cell. The Local field effects are within a radius of 6.289Å for different lattice sites with this position are evaluated. The centre is then shifted to 1st unit cell below the surface and local fields are evaluated. This procedure is continued to ten times the lattice constant 'c' where the radius of the sphere of influence is 62.89Å . At this position all the sphere of local field is totally within the core of the waveguide.

The local anisotropic factors ' $\Sigma_j \Sigma_i D_{ij}$'s are given in Table 6. The values given in these tables represent the 'local field' as seen by each of the species of Y, V and O atoms. The values of Refractive Indices and Birefringence are given in Table 7.

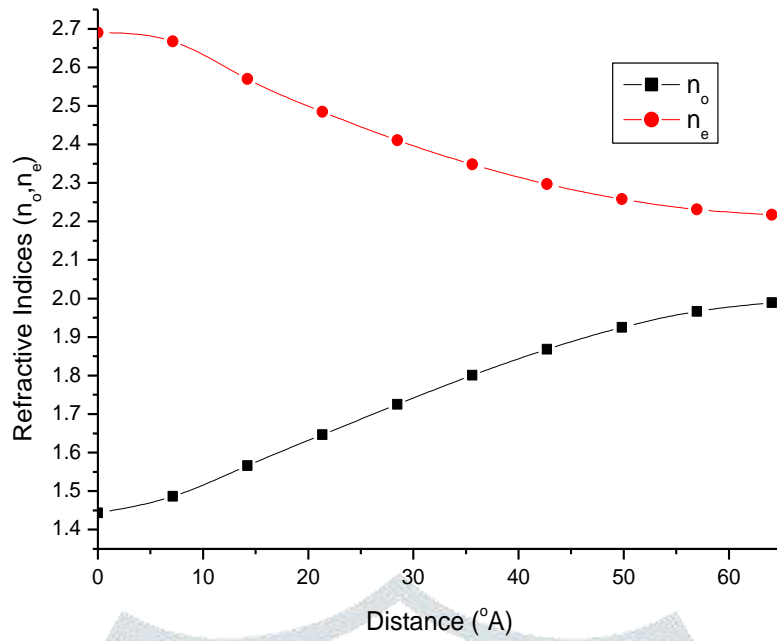


Figure 1: Variation of n_o and n_e near the Surface of an Z-cut, X-propagation YVO₄ Waveguide at $\lambda = 6328\text{\AA}$.

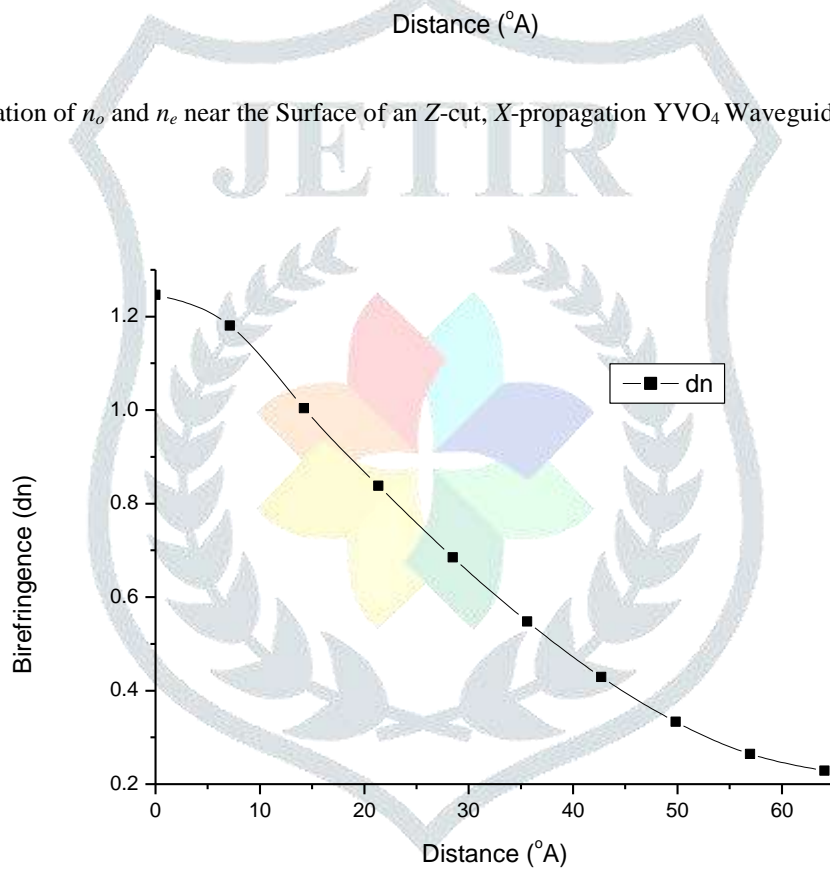


Figure 2: Variation of Birefringence near the Surface of an Z-cut, X-propagation YVO₄ Waveguide at $\lambda = 6328\text{\AA}$.

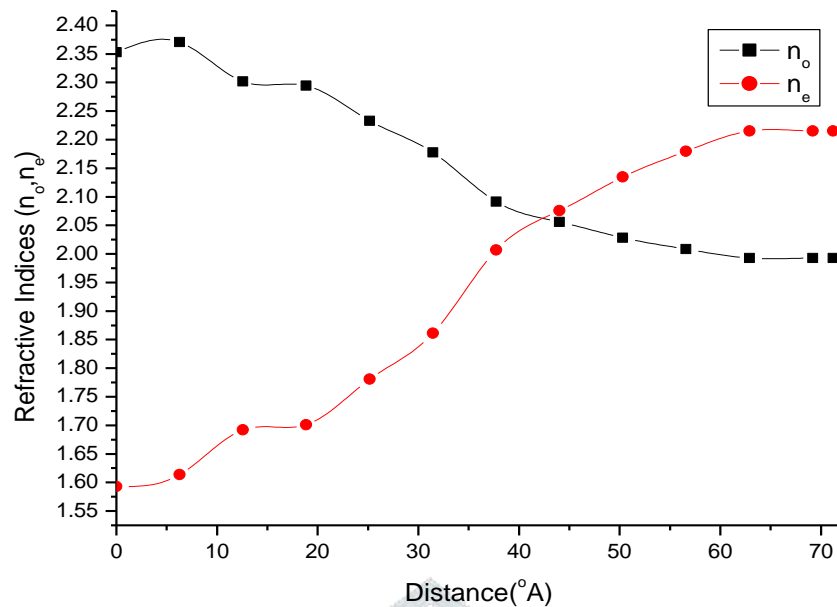


Figure 3. Variation of n_o and n_e near the Surface of a X-cut, Z-propagation YVO₄ Waveguide at $\lambda = 6328\text{\AA}$.

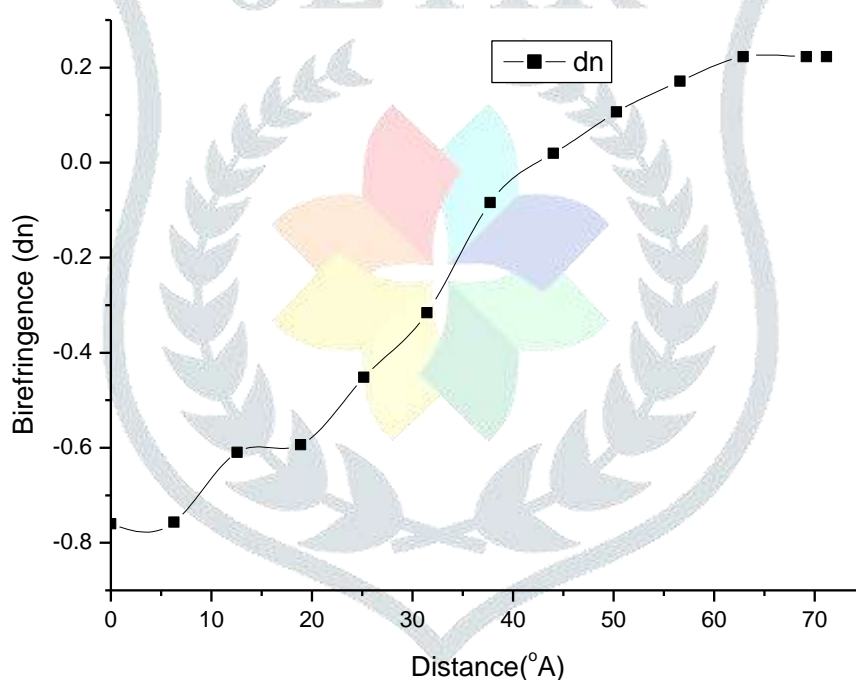


Figure 4. Variation of Birefringence near the Surface of a X-cut, Z-propagation YVO₄ Waveguide at $\lambda = 6328\text{\AA}$.

VI. RESULTS AND DISCUSSION

The calculations are carried out for YVO₄ optical waveguide at wavelength 6328Å. For an X-cut, Z-propagation YVO₄ waveguide, n_o is found to increase from 1.44 on the surface to 1.99 in the interior, whereas n_e is found to decrease from 2.69 on the surface to 2.22 in the interior of the waveguide. For a Z-cut waveguide, n_o is found to increase from 1.44 to 1.99 whereas n_e is found to decrease from 2.69 to 2.22. The opposite behavior in the variation of n_o and n_e near the surface of the X-cut, and Z-cut waveguides are primarily due to the dipole orientation in the lattice being different for the two directions of the electric vectors of light.

Variation of the refractive index near the surface is to be considered in the studies involving the propagation mechanisms of light through all such waveguides.

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