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## Optimum Placement of PMU for Wide Area Measurement Systems

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Abstract: This paper presents identifying the best selection process for selecting the most effective stabilizing signal to improve damping of inter area oscillations multimachine power system. Phasor Measurement Units or PMUs are one of he main component of the Wide Area Measurement Systems (WAMS). The large amount of data collected by PMUs need to be channelized to regional and global data centers where real-time state estimation, and protection, stabilization decisions are made. It is studied in this paper that how different signal selection techniques gives different control loop for damping of a particular inter area mode of oscillations. In spite of these the controller locations were obtained for optimum placement of phasor measurement units for wide area measurement systems. It is resulted from the two area 4 machine system that the HSV based signal selection approach performs excellent in both small and large disturbance for the test system compared to both residue and geometric measure of joint controllability and observability approach. Non-linear simulations are carried out in order to evaluate the performance of different approaches of signal selection under study.

**Key Words:** Inter-area oscillations, residue approach, geometric measures, power system stabilizer (PSS), Phasor Measurement Unit (PMU)

#### I. INTRODUCTION

Power system stability is one of the major issues in power systems which deals with the response of the system to the disturbances occurred in the network. Some of the major oscillations attributed to system collapse are local mode, intraplant mode, inter-area mode, control mode and torsional mode of oscillations. From all of these modes inter area mode of oscillations are very severe and observed over a large region of the network. To make the system stable, it is essential to effectively damp the inter-area modes of oscillations.

In conventional approach, supplementary control signals are used to damp the inter-area oscillation which are provided to the excitation system by installing Power System Stabilizer (PSS) at the generator location. The PSS use the local stabilizing signal such as deviation of generator speed and provides the supplementary control input to the excitation. But the PSS taking local signal may not be always effective to damp inter area oscillations, because the local controllers are having lack of global observations. It is also observed that the local signals have lack modal controllability and observability. But it is proved that under certain operating condition the inter area mode may be controllable from one area and observable from another control area. In this case the local controllers cannot provide effective damping.

In recent years, the global observation of the power system is achieved by using wide area measurement systems through phasor measurement units (PMUs) which receives signal from the satellite based global positioning system (GPS). The usage of remote signal for damping controller has become successful due to the advancement of Phasor Measurement Units (PMUs). PMUs have significant contribution in newly developed Wide Area Measurement System (WAMS) technology. The Phasor Measurement Unit is the main component of the WAMS which is used for the measurement of the electric quantities of interest (voltage and the current phasors, frequency and the rate of change of frequency). PMUs also permits the transmission and synchronization of the performed measurements.

PMUs can deliver control signals and synchronous phasors at high speed. PMUs are situated at remote location with respect to the controllers and the signals from PMU are called as remote stabilizing signals. PMUs are placed at strategic locations on the grid at the buses [5] and obtain a coherent picture of the whole network in real time. It is significant to know that the phasor technology was developed to compliment the SCADA system.

Attribute	SCADA	PMU
Observability	Steady State	Dynamic/ Transient
Measurement	Analog	Digital
Measured	Magnitude –	Magnitude (RMS)
Quantity	(RMS) –	and phase offset
	MW,	from common
	MVAR	reference – MW,
		MVAR, and Angle
		Difference
Monitoring	Local	Wide Area
Resolution	2-4 Samples	up to 60 samples per
	per second	seconds
Phase Angle	No	Yes
Measurement		

#### II. ELECTROMECHANICAL MODES:

- (1) Intra plant mode: Machines installed at the same power generation site oscillate against each other at a frequency ranging from 2.0 to 3.0 Hz depending on the unit ratings and the reactance connecting them.
- (II) Local plant mode: In this mode, one generator swings against the rest of the system at 1.0 to 2.0 Hz. The effect of the oscillation is localized to the generator and the line connecting the generator to the grid.
- (III) Inter-area mode oscillations: It involves two coherent group of generators swinging against each other at 1 Hz or less. It is observed over a large area of the network. The oscillation frequency is approximately 0.3 Hz.
- (IV) Control mode oscillations: These are related to generators and poorly tuned exciters, governors, HVDC converters and SVC controls. Excitation systems and load can interact through the control modes.
- (V) Torsional mode oscillations: These types of modes are linked with a turbine generator shaft system in the frequency range of 10-46 Hz. Mostly these modes are excited when a multi-stage turbine generator is connected to the grid system through a series compensated line.

#### III. SYNCHROPHASOR

A phasor represents the magnitude and phase angle of voltage and current sinusoidal waveforms at a specific point in time. Synchrophasor are precise time-synchronized measurements of some parameters on the power system, now can be obtained from grid monitoring devices known as phasor measurement units (PMUs).

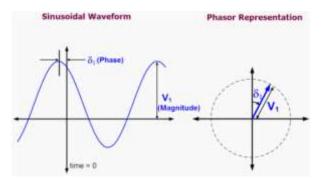


Fig.3.1 Sinusoidal Waveform and Phasor Representation

PMUs measures current, voltage, and frequency.it also calculate phasors, and this accumulation of time synchronized grid condition data is called phasor data. Each phasor measurement is time stamped against Global Positioning System universal time; when a phasor measurement is time stamped, it is known as Synchrophasor [8]. This allows measurements to be synchronized, taken by PMUs by different owners or by at different locations and time-aligned, then immixed to provide a precise, comprehensive opinion of an entire region or interconnection. PMUs samples at speeds of 30 observations per second, however conventional monitoring technologies (such as SCADA) can measure once in every two to four seconds.

#### IV. SYNCHROPHASOR DATA SYSTEMS

The purpose of a Synchrophasor data system is, rapid measurements (at least 30 per second) of phasors of voltage and current (magnitude and their respective phasor angles) which are precisely time stamped and these measurements are made available to analyze and display grid conditions in transmission and power system control centers. Eventually, Synchrophasor data systems can be used for automated control of grid. A Synchrophasor system will improve real-time situational awareness and decision support tools to improve system reliability. Synchrophasor measurements can also be used to improve component and system models for both on-line and off-line network analysis to assess system security and adequacy to withstand expected contingencies. The components of a Synchrophasor data system includes:

- (I) Phasor Measurement Unit (PMU): Calculates voltage and current phasors based on digital sampling of alternating current (AC) waveforms and an accurate time signal provided by a GPS clock. A PMU provides communication to remote locations in a standard protocol at rates of at least 30 samples per second.
- (II)Communication System: it is a mechanism to transport the digital information from the PMU to the location where the data will be used. Communication is typically made through a private wide-area network (WAN) but any digital transport system can be used that offers, required security and availability; functional necessities for a Synchrophasor system architecture.
- (III) Phasor Data Concentrator (PDC): it receives and time-synchronizes phasor data received from multiple PMUs to generate a real-time, time-aligned output data stream. It can also exchange phasor data with other PDCs located at other positions. With the help of multiple PDCs, multiple layers of concentration can be carried out within an individual Synchrophasor data system. A PDC collects phasor data from multiple PMUs or other PDCs, and aligns the data by time-tag to create a time-synchronized dataset, and passes this dataset on to other information systems. Depending on the role of PDC its function can vary or its location between the source PMUs and the higher-level applications []. A local PDC can

be situated physically close to PMUs (typically at a substation) to manage the accumulation and communication of time-synchronized data from local PMUs, store the data for use within the substation and send it to higher level concentrators.

(IV) Data Storage: Systems to store Synchrophasor data and make it available in a convenient manner for post-real-time analysis can be integrated with the PDC or be stand-alone data historians or, in the case of smaller implementations, be traditional relational data base systems. Traditional relational databases can be used to manage phasor data for a short period of history or for implementations that contain a small number of PMUs [20]. Distributed non-relational databases are used to manage big datasets by large internet firms. These systems have some relational database features that can be used effectively with data systems that contain many, many terabytes of information. They divide the data up into smaller blocks that are processed in parallel. This technology is being explored for use in Synchrophasor data systems as well.

#### V. EIGEN VALUE ANALYSIS:

For analyzing the small signal stability of any system, the system model can be linearized around an operating point i.e. the disturbances are considered to be so small or incremental in nature so that a linear model of the system around an operating point can be developed. The state space representation of the power system can be written as

$$\dot{x} = Ax + Bu$$
$$y = Cx$$

Once the state space model of a power system is obtained the small signal stability of the system can be calculated and analysed and the eigenvalues  $\lambda_i$  are calculated for the A matrix. They are the non-trivial solutions of the equation:

$$det(A - \lambda I) = 0$$

The solutions of characteristic equation are the eigenvalues of the  $n \times n$  matrix A. These eigenvalues are of the form  $\sigma \pm j\omega$ . The stability of the operating point may be analyzed by studying the eigenvalues.

The conjugate-pair complex eigenvalues  $(\sigma \pm j\omega)$  each corresponds to an oscillatory mode. A pair with a positive  $\sigma$  represents an unstable oscillatory mode since these eigenvalues yield an unstable time response of the system. However, a pair with a negative  $\sigma$  represents a desired stable oscillatory mode. Eigenvalues associated with an unstable or poorly damped oscillatory mode are also called dominant modes since their contribution dominates the time response of the system. It is quite obvious that the desired state of the system is for all of the eigenvalues to be in the left-hand side of the complex plane.

The damped frequency of the oscillation in Hertz and damping ratio are given by:

$$f = \frac{\omega}{2\pi}$$

$$\xi = \frac{-\sigma}{\sqrt{\sigma^2 + \omega^2}}$$

The operating point is stable if all of the eigenvalues are on the left-hand side of the imaginary axis of the complex plane; otherwise it is unstable.

### VI. SIGNAL SELECTION AND CONTROLLER LOCATIONS

In order to damp the inter area oscillations; wide area controller employing signals from remote locations are very much necessary because they are more controllable and observable compared to local signals. The remote stabilizing signals are often considered to as "global signals". In the selection of stabilizing signals and control location the effort should be to use as few measurement and control device as possible to achieve acceptable damping effect.

The controllability and observability methods are often used to select controller location and stabilizing signals. There are three different approaches are used for measurement and control signal selection such as

#### (I) Residue approach:

The transfer function of an interconnected power system associated with the state equations can be uttered by

$$G(s) = C(sI - A)^{-1}B = \sum_{i=1}^{n} \frac{R_i}{(s - \lambda_i)}$$

Where  $R_i$  is known as residue matrix of size  $\mathbf{q} \times \mathbf{p}$  associated with  $\lambda_i$ 

$$R_i = C\phi_i\psi_i B$$

For  $j=1,2,\ldots,q$  and  $k=1,2,\ldots,p$  the elements of the residue matrix  $R_i$  can be expressed as

$$R_i(j, k) = C_i \phi_i \psi_i B_k$$

In fact the residue can be represented as the product of the mode's controllability and observability.

The controllability for the mode i at  $k^{th}$ generator can be represented as

$$cont_{i,k} = |\psi_i B_k|$$

The observability of the mode i from  $j^{th}$  output is defined by  $obj_{i,k} = \left| C_i \varphi_i \right|$ 

From above equations, it is concluded that

$$|\mathbf{R}_{\mathbf{i}}| = |\mathbf{C}_{\mathbf{j}} \mathbf{\phi}_{\mathbf{i}} \mathbf{\psi}_{\mathbf{i}} \mathbf{B}_{\mathbf{k}}| = \mathbf{obj}_{\mathbf{j},\mathbf{k}} * \mathbf{cont}_{\mathbf{j},\mathbf{k}}$$

It has been proved that the PSS is installed at that generator where largest residue for the  $i^{th}$  mode is found.

The limitation of the residue approach is that the approach is only valid for signals of the same type. However signals of widely varying physical significance such as tie-line power flow (MW), bus frequency (Hz), shaft speed (rad/s), angle shift (deg.), etc. will be involved in the output matrix

simultaneously, then residue approach suffers a lot from scaling problem. To overcome this problem geometric approach is used.

#### (II) Geometric approach:

Optimal selection of measured signal and control site location is performed with the geometric measures of joint controllability and observability approach. The indices for controllability and observability  $\mathrm{COI}_k$  and  $\mathrm{OBI}_j$  for a particular  $i^{th}$  mode of oscillations are defined by:

$$COI_k = cos \big(\theta(\psi_i, B_k)\big) = \frac{|\psi_i B_k|}{\|\psi_i\| \|B_k\|}$$

$$OBI_{j} = cos\left(\theta\left(\varphi_{i}, C_{j}\right)\right) = \frac{\left|C_{j}\varphi_{i}\right|}{\left\|C_{i}\right\|\left\|\varphi_{i}\right\|}$$

where,  $b_k$  is the  $k^{th}$  column of input matrix B (corresponding to the ith input),  $\psi_i$  is the left eigenvector of  $i^{th}$  mode of oscillation and  $c_j$  is the  $j^{th}$  row of output matrix C (corresponding to the  $j^{th}$  output).  $\phi_i$  is right eigenvector of  $i^{th}$  mode of oscillations. The symbol  $|\ |$  and  $|\ |\ |$  are the absolute value of a scalar and standard-2 norm respectively. The joint controllability and observability index of geometric approach is defined by

Joint-index k, 
$$j = COI_k * OBI_j$$

If  $COI_k = 0$ , then the mode k is uncontrollable from input i and If  $OBI_j = 0$ , then the mode k is unobservable from the output j.

#### (III) Hankel Singular Value based approach

As in the above two cases HSV also can be used for the measure of controllability and observability index of the given system. For a linear system, the HSV can be defined as

$$\sigma_i = \sqrt{\lambda_i(PQ)}, \quad i = 1, ..., n$$

Where  $\sigma_i$  reflects the index of joint controllability and observability and  $\sqrt{\lambda_i(PQ)}$  reflects the  $i^{th}$  eigenvalue of PQ. The P and Q are controllability and observability Gramian matrix respectively.

The (A, B) are controllable if the controllability Gramian P is defined as

$$P = \int_0^\infty e^{At} BB^T e^{A^T t} dt$$

Matrix P is a solution of the following Lyapunov equation  $AP + PA^{T} + BB^{T} = 0$ 

The (A, C) are observable if the observability Gramian matrix is defined as

$$Q = \int_0^\infty e^{A^T t} CC^T e^{At} dt$$

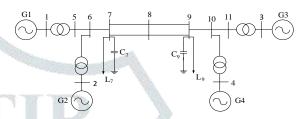
Matrix Q is the solution of following Lyapunov equation:

$$A^TO + OA + C^TC = 0$$

Now in the remaining sections the above methods of selection of control signal will be tested in the case study example.

#### VII. TEST SYSTEM

Despite the high level of activity in recent years on widearea control, there are many aspects remain poorly understood due to the complexity in large power system. Therefore a small Kundur's two area 4 machine power system has been set up to deal with the most of the issues/challenges faced by wide-area control. In the test system all the generators are equipped with governor, AVR, and IEEE ST1A type static exciter [13]. The loads taken here are constant impendence type and connected to bus no. 7 and 9. The structure of the case study power system is given in Fig.2



Figure

#### 2: Kundur's two area four machine system

It is assumed that the Local signal based PSSs are assumed to be connected with the chosen generators that are determined as suitable control location, for damping of local area oscillations. After the calculation of most suitable stabilizing signal and control location a Global signal based PSS is employed supplement to the input of AVR along with Local PSS for the damping of inter area oscillations [16]. The exporting Power  $P_{tie}$  from area 1 to area 2 through tie line is 413 MW and chosen as nominal operating point.

#### VIII. SMALL SIGNAL STABILITY ANALYSIS

Power system dynamic components of the studied system are modelled according to the Kundur's benchmark system database. With the detailed modal analysis, it came to know that each generator has 11 states and the total order of the nonlinear model is 44. In normal operating condition, the power transfer through tie-line connecting two areas is 413 MW and load consumption of area 1 is 967 MW and of area 2 is 1767 MW. The nonlinear model of the studied system is linearized around the initial operating point of tie-line power ( $P_{tie} = 413 \text{ MW}$ ). After performing modal analysis with Power System Toolbox (PST), 44 modes with their eigenvalues, damping ratio and frequency are obtained which are tabulated in table I

Table I: Two Area System Modes of Oscillations

Mode No.	Eigen Value	Damping Ratio	Frequency (Hz)
5	- 0.2522 - 0.6536i	0.3601	0.1040
15	0.0453 - 4.1135i	- 0.011	0.6547

There is only one inter-area mode having frequency of 0.6547 Hz, presented in the system. This mode is referred to lightly

damp inter-area mode 15 with eigenvalue (0.0453 - 4.1135i) and damping ratio of -0.011. The objective of the proposed WADC is aimed at achieving adequate acceptable damping for this mode.

In addition to the critical mode identification, modal analysis was also performed for coherent machine identification where the one group of generators forms one area and oscillating with another group of generators [17]. Compass plot shows the coherent areas in the studied system as shown in figure 5.2.

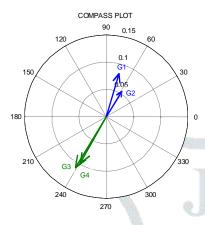


Figure 3: Coherent Area Identification using Compass Plot

There are four arrows representing the four generators. The length and direction of each arrow is corresponding to the magnitude and phase angle of respective eigenvector for the critical mode of machine. In the compass plot, it is clear that generator 1 and generator 2 forms area 1, and generator 3 and generator 4 forms another area so that the studied system termed as two area system when area 1 is oscillating with respect to area 2. The small signal stability analysis [18] is performed under no fault condition and by applying small disturbance of 0.05 to the voltage reference of exciter in generator 1 of area 1.

## IX. OPTIMAL SIGNAL SELECTION AND CONTROL SITE LOCATION

The tie-line active power flow at various lines of the system has been taken for signal selection. The signal selection is carried out by residue approach, geometric measure of controllability/observability approach and Hankel Singular Value (HSV) based signal selection approach. Table-II, Table-III and Table-IV shows results obtained from Residue approach, Geometric approach and HSV approach respectively.

Table II: Normalized values of the Residue approach for the 4 machine two area system

Signals	Generators			
	G-1	G-2	G-3	G-4
P6-7	0.5298	0.6849	0.5206	0.6686
P7-8	0.3545	0.4584	0.3484	0.4475
P8-9	0.3224	0.4169	0.3168	0.4070
P9-10	0.7735	1	0.7601	0.9763

Table III: Normalized values of the geometric measure of controllability/observability approach for 4 machine 11 bus system.

Generators -	Signals			
	$P_{6-7}$	P <sub>7-8</sub>	P <sub>8-9</sub>	$P_{9-10}$
G-1	0.3528	0.7735	0.7655	0.4179
G-2	0.4560	1	0.9897	0.5402
G-3	0.3466	0.7601	0.7522	0.4106
G-4	0.4452	0.9763	0.9662	0.5274

Table IV: Absolute values of HSV for 2 area 4 machine system

Generators	Signals			
	$P_{6-7}$	P <sub>7-8</sub>	$P_{8-9}$	$P_{9-10}$
G-1	$8.6030e^{-04}$	0.0178	0.0111	0.0274
G-2	0.0052	0.0860	0.1075	0.3661
G-3	0.1192	0.4895	0.3264	0.8804
G-4	0.1878	0.4361	0.3304	1

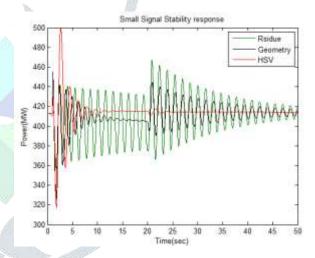


Fig. 9.1: Tie line active power flow due to step change in voltage reference at generator-1

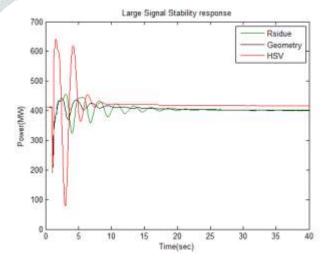


Fig. 9.2: Tie line active power response for 3 phase fault at bus 8

It can be observed from above results that the signal selected by HSV based signal selection approach provides better response as compared to residue geometric approach. It is also resulted that in case of large disturbance, the HSV based signal selection approach performs excellent in comparison with residue and geometric approach.

#### X. CONCLUSION

The selection of control loop for a given inter area mode by three different method of signal selection approaches are obtained. In order to validate the result of three different methods, the Kundur's two area four machine system has been used for the case study example. The responses of Tie line active power flow is investigated for three methods i.e Residue, Geometrical and HSV are observed. The controller locations for the optimum placement of PMU for wide area measurement system are obtained.

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