



RIETVELD REFINEMENT: GOLD STANDARD OF QUANTITATIVE ANALYSIS

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ABSTRACT:

The Rietveld refinement is a popular analytical technique for the quantitative phase analysis of various natural and synthetic materials. It can be used for both fully crystalline multiphase systems as well as for materials containing even an amorphous fraction. This method involves the analysis of XRPD data and utilizes the Rietveld refinement technique to determine the relative proportions of each phase present in the sample. Overall, the Rietveld method offers a reliable and accurate means of characterizing materials and is essential for various scientific and industrial applications. A modified version of the Rietveld computer program has been used to perform quantitative phase analysis of multicomponent mixtures using X-ray powder diffraction data. The improved program was successful in determining composition of mixtures with high accuracy and precision. Quantitative information was obtained through refined individual scale factors and unit cell volumes using Rietveld refinement program. The analytical report of quantitative phase analysis using Rietveld refinement method specify the details of the instrument used for data collection as well as software and databases employed for the Rietveld refinement. To correct the preferred orientation, we processed the XRPD patterns using commonly available program Rietveld refinement. It allows for accurate determination of crystal structure, lattice parameter and atomic positions.

Key words: Rietveld refinement, XRPD, Quantitative phase analysis, preferred orientation

INTRODUCTION:

Rietveld refinement is a multiparameter curve fitting methodology to refine X Ray diffraction result [1,2,3]. Rietveld refinement technique was developed for the refinement of crystal structure, it is also very efficient in quantitative phase analysis [4]. It was first introduced and implemented full profile refinement method in powder diffraction by professor Hugo Rietveld [1,5,6]. In modern crystallography it is treated as a black box [7]. Crystal structure data having physical constants used for calculating reflection intensities eliminates the errors associated with the procedures [4]. The Rietveld refinement is mainly developed for refinement of crystal structure from neutron powder diffraction data. The physical origins affect diffraction lines, the diffraction angle have high degree of correlation between the refinable parameters [8].

Quantitative phase analysis is capable of determining the proportion of each crystalline phase in a multiphase sample, as well as identifying the presence and quantity of amorphous phases. This technique utilizes diffraction patterns to measure the intensities of diffraction peaks from each phase and compares them to reference standards. By accurately quantifying the amount of each phase present, quantitative phase analysis provides crucial information for material characterization and optimizing manufacturing processes. The technique is widely used

in fields such as materials science, geology, and pharmaceuticals ^[9]. Rietveld refinement based quantitative phase analysis is more accurate and precise than methods based on chemical extraction ^[10]. The precision of the method was tested by independent replicate sample preparation and analysis. The analysis yielded information on the proportions of different phases and the refined substitutions of elements. These findings provide insight into the composition and structure of the material being analysed ^[11]. This technique refines user selected parameters to minimise the difference between experimental (observed) pattern and model based on hypothesised crystal structure and instrument parameters (calculated pattern) ^[1] by least square method ^[12,13].

Rietveld analysis is a complex process, since it must fit structural, sample, instrumental terms. It can also provide result that cannot be obtained in other ways or results at their ultimate precision. With the availability of appropriate specimen, structural determination from single crystal diffraction is preferred, sometimes measurement condition preferred powder diffraction. For this reason, use of Rietveld refinement technique is increasing ^[14].

Application

- microstructural information
- Crystalline size distribution
- Average domain size
- Crystalline defect concentration ^[8]
- Texture analysis
- Standardless Quantitative phase analysis ^[12]
- Percentage crystallinity
- Quantitative phase analysis
- Characterization of substitution
- Unit cell determination and shape
- Atomic coordinates/bond length
- Micro strain in crystal lattice- texture effects ^[15]

It can apply only when the cell dimensions and space group are known and when a reasonable model exists for the structure and allows extraction of the maximum amount of information contained in the powder pattern. The refinement technique allows calculation of shift in the parameters which improve the fit of calculated powder pattern to the observed one ^[16]. It is able to refine whole profile with parameters including half-width, zero shift, cell parameters ^[17], preferred orientation correction ^[18,19], overall asymmetry correction, overall scale factor, overall isotropic temperature factor, fractional coordinates of the atoms, atomic isotropic temperature and the components of the magnetic vectors of each atom ^[20,21].

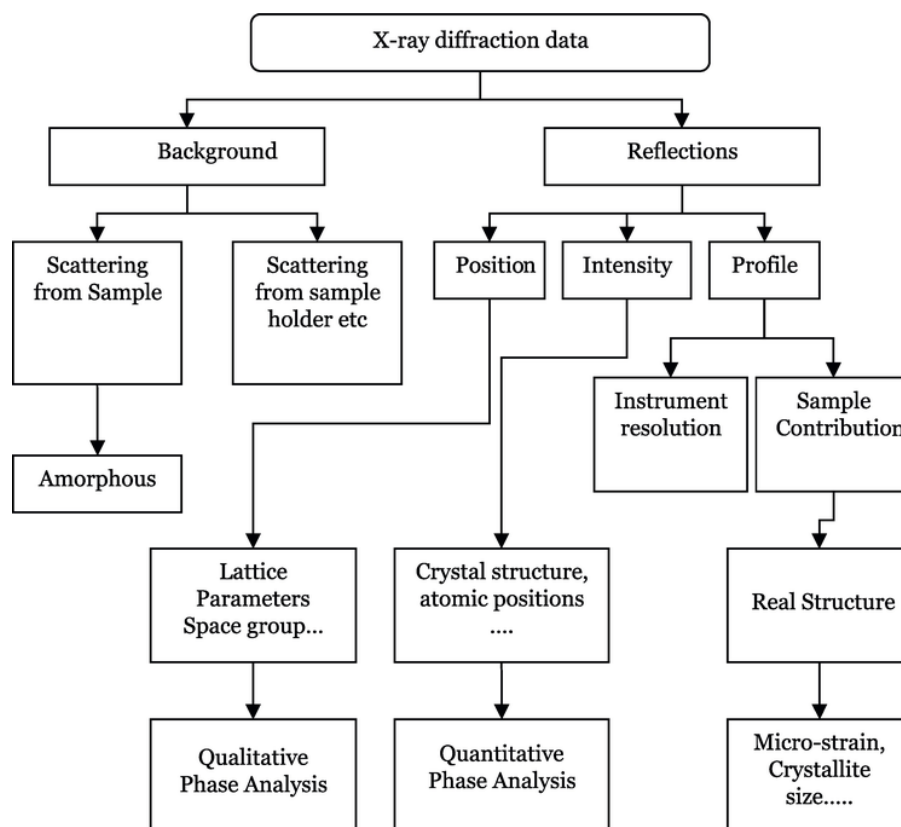


Fig: The algorithm of whole profile refinement program developed by Hugo M Rietveld [reconstructed from the IUCr newsletter no. 26, Dec 2001].

For performing Rietveld refinement, it is essential that powder diffraction data be collected approximately. There are so many factors to be considered prior to data collection, quality of diffractometer, quality of the instrument alignment, and calibration, suitable radiation, wavelength, appropriate sample preparation and thickness. Structure refinement does not yield sensible result, if the relative intensities are not correct. The peak describes the both sample and instrument function. Single peak is selected for the diffraction pattern as a standard peak. The percentage depends on the peak shape. The peak is fitted to some criteria and this curve is divided into symmetric and asymmetric part; values are stored in tabulated form. Before refinement the structural parameters and the position of the peak should be matched well [6]. Peak shape depends on crystallite/domain size, stress/strain, defects/vacancies, source/geometry, slit-size/detector resolution and $2\theta/hkl$ indices [22].

Two approaches are used in powder diffraction pattern. One is linear interpolation between the peak or it can be modelled by empirically. Both these methods work well and fit easily with a plot. Most of the peak not resolved in the baseline so the estimation of background is difficult. In this condition background subtraction approach is used, the background is re-estimated and re-subtracted in the refinement [23].

The refinement decreases the uncertainties in cell-parameter determination. Cell parameters are influenced by sample height, instrumental and sample factors, sample absorption, peak shape and instrumental calibration. On heating material undergoes a phase transition to simple cubic structure [24].

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Rietveld refinement analysis is an effective tool for determining the magnetic structure of materials using powder diffraction data.

The GSAS (The General Structure and Analysis System) software is commonly used and it has the ability to compute magnetic scattering [3].

For n diffraction peaks $n-1$ parameters can refine

Accurate structural information from powder diffraction data is enhanced by combination of Rietveld refinement and Maximum Entropy Methods (MEM) [12]. It is done in sets of two to five cycles at a time but for effective refinements hundreds of cycles will be required and thousands for complex systems. The GSAS (The General Structure and Analysis System) software is commonly used and it has the ability to compute magnetic scattering [3].

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R value

Reliability factors or residual values or Rietveld refinement indices or R values by Rietveld enabled us to visualize profile fit between observed and calculated patterns more effectively [3,25,26,27].

The weighted profile R value, $R_{wp} = \frac{\sum w_i (y_{c,i} - y_{o,i})^2}{\sum w_i y_{o,i}^2}$

Where, w_i the weight at i^{th} step, $y_{c,i}$ is the observed intensity and $y_{o,i}$ is the calculated intensity. [28]

MATERIALS AND METHODS:

Requirements for Rietveld refinement

- Experimental diffraction pattern
- Suitable peak and background functions
- A structure method that makes physical and chemical sense [12]

Crystal structure information get from

- Publications
- Commercial Databases
 - ✓ ICSD (International Crystal Structure Database)
 - ✓ LPF (Linus Pauling File)
 - ✓ NIST Structural Database
- Free Online Databases
 - ✓ ICDD (International Centre for Diffraction Data)
 - ✓ CCDC
 - ✓ Crystallographic open data base
 - ✓ Webmineral
 - ✓ Mincrust
 - ✓ American Mineralogist
 - ✓ Protein data bank
 - ✓ Nucleic acid Database [28]

Rietveld programs

- Fullprof
- GSAS
- Bruker TOPAS
- MDI Jade or Ruby
- Rietica
- PSSP
- Powder cell
- Panalytical X'Pert highscore Plus v3.0d [29]
- EDINP
- XRS-82 [30]

Challenges

- Lack of 100 % representative specimen especially powder sample- Differences in grain size, preferred orientation, inhomogeneous grain boundary and other microscopic difference cause limitations
- Porosity of sample- I case of nanomaterial the increase in surface area to volume ratio cause apparent amorphicity in crystalline sample.
- Continues motion of either or both detector and sours of goniometer and recording transit timer of cameras ^[31]
- Errors in input file, can corrected by converting filer into suitable format using software's ^[32].

REFERENCE:

1. Samal S. K.. Rietveld refinement: A technique more than just identification. *Journal of Applied and Computational Mathematics*. 2019; 8(1): 432
2. Freire Aguiar FN, Santos Pimentel RM, Rocha Barbosa HH, Almedia Leite FA, Mazzetto SE, et al. The thermal stability of (CaTiO₃)_{1-x}(Cr₃/4Fe₅/4O₃)_x ceramic composites in the microwave region. *Materials Sciences and Application*. 1967;7(22):151-152.
3. Rietveld H. A profile refinement method for nuclear and magnetic structures. *Journal of Applied Crystallography*.1969 22(2). 65-71
4. Nemet Z, Sajo I, Demeter A. Rietveld refinement in the routine quantitative analysis of famotidine polymorphs. *Journal of pharmaceutical and biomedical analysis*2010;51(3):572-6.
5. Young RA .(The Rietveld method. International Union of Crystallography, Oxford University Press,1993: 252-254.
6. McCusker LB, Von Dreele RB, Cox DE, Louer D, Scardi P . Rietveld refinement guidelines. *Journal of Applied Crystallography*1999;32(1): 36-50
7. Evans JS, Evans IR. Structure analysis from powder diffraction data: Rietveld refinement in excel. *Journal of Chemical Education* 2020;98(2):495-505.
8. Balzar D, Popa NC. Analyzing microstructure by Rietveld refinement. *Rigaku Journal* 2005;22(22):16-25.
9. Gualtieri, A.; Gatta, G. D.; Arletti, R.; Artioli, G.; Ballirano, P.; Cruciani, G.; Guagliardi, A.; Malferrari, D.; Masciocchi, N.; Scardi, P. Quantitative phase analysis using the Rietveld method: Towards a procedure for checking the reliability and quality of the results 2019;88(2): 147-151
10. Santini TC. Application of the Rietveld refinement method for quantification of mineral concentrations in bauxite residues (alumina refining tailings). *International Journal of Mineral Processing* 2015;10(130):1-0.
11. Monecke T, Kohler S, Kleeberg R, Herzig PM, Gemmill JB. Quantitative phase-analysis by the Rietveld method using X-ray powder-diffraction data: Application to the study of alteration halos associated with volcanic-rock-hosted massive sulfide deposits. *The Canadian Mineralogist* 2001;39(6):1617-1633.
12. Dinnebier.R. Commision on powder diffraction. International Union of Crystallography 2001.
13. Kumar. L, Kumar. P, Narayan. A and Kar. M. (2013) Rietveld analysis of XRD patterns of different sizes of nanocrystalline cobalt ferrite. *International Nano Letters* 2013;(3):1-12
14. International tables for crystallography vol H,chapter 2019;4.(7): 465-472.
15. Döbelin N, Lession -1 RMS Foundation, Bettlach, Switzerland
16. Deschamps. J. R, Anderson. J. L, Encyclopaedia of Science and TechnologY(third edition). Academic press. 2002;121-153 <https://doi.org/10.1016/B0-12-227410-5/00160-5>
17. Sakata M, Cooper MJ. (1979). An analysis of the Rietveld refinement method. *Journal of Applied Crystallography*, 1979;12(6):554–63.
18. Dollase WA. (1986) Correction of intensities for preferred orientation in powder diffractometry: application of the March model. *Journal Applied Crystallography*,1986; 19(4):267–72
19. Altomare. Early finding of preferred orientation: Applications to direct methods', *Journal of Applied Crystallography*1996; 29(4):341–345. doi:10.1107/s0021889896000271.
20. Hester JR . Improved asymmetric peak parameter refinement. *Journal Applied Crystallography* 2013.; 46(4):1219-20
21. Finger LW, Cox DE, Jephcoat AP. Correction for powder diffraction peak asymmetry due to axial divergence. *Journal Applied Crystallography*.1994;27(6):892-900.

22. Langford JI. Some applications of pattern fitting to powder diffraction data. *Progress in Crystal Growth Characterization*.1987;1(14):185–211
23. Buhrke, V. E., Jenkins, R., & Smith, D. K. (1998). *A practical guide for the preparation of specimens for x-ray fluorescence and x-ray diffraction analysis*. New York: Wiley-VCH.
24. Stinton GW, Evans JS. Parametric rietveld refinement. *Journal of Applied Crystallography*.2007;40(1):87-95.
25. McCusker, L. B., Von Dreele, R. B., Cox, D. J., Louër, D., & Scardi, P. Rietveld refinement guidelines. *Journal of Applied Crystallography*, 1999;32(1):36–50. <https://doi.org/10.1107/s0021889898009856>
26. Rietveld HM. Line profiles of neutron powder-diffraction peaks for structure refinement.*ActaCrystallography*.1996;22(1):151–152. <https://doi.org/10.1107/S0365110X67000234>
27. Post, J. E., & Bish, D. L. Rietveld refinement of crystal structures using powder x-ray diffraction data. *De Gruyter eBooks*. 1989;277–308. <https://doi.org/10.1515/9781501509018-012>
28. Berar, J., & Lelann, P. E.s.d.'s and estimated probable error obtained in Rietveld refinements with local correlations. *Journal of Applied Crystallography*, 1991;24(1):1–5.
29. Pecharsky, V., & Zavalij, P. *Fundamentals of powder diffraction and structural characterization of materials*, second edition. Springer Science& Business Media.2008
30. Hill. R. J. Rietveld refinement round robin.I. analysis of standard x ray and neutron data for Pb SO4 .1992; *Journal of Applied Crystallography*. 25(5):589-610
31. Ewald PP. X-ray diffraction by finite and imperfect crystal lattices. *Proceedings of the Physical Society* 1940;52(1):167.
32. David WIF. (2004). Powder diffraction: Least-squares and beyond. *Journal of Research of the National Institute of Standards and Technology*.2004;109(1):107.

