

PRIME E-CORDIAL LABELING OF SOME SPECIAL GRAPHS

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Abstract : Let G be a simple (p,q) graph and let $f:E(G) \rightarrow \{1,2,3,\dots,n\}$ be a mapping. Then f is called a prime E-cordial labelling of a graph G , if there exists an induced labeling $f^*:V(G) \rightarrow \{0,1\}$ defined by $f^*(V) = \{\sum f(uv/uv \in E(G) \pmod{2})\}$.

A graph G which admits prime E-cordial labeling is called a prime E-cordial graph.

Here, we have proved that Peterson graph, Fan graph, Flower graph admits prime E-cordial labeling.

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I. INTRODUCTION

We consider a finite, connected, undirected and simple graph $G=(V(G), E(G))$ with p -vertices and q -edges which is denoted by $G(p,q)$. For standard terminology and notations we refer Gathon [4].

Definition 1.1:

The graph labeling is an assignment of numbers to the vertices or edges or both subject to certain conditions.

Definition 1.2:

A binary vertex labeling of a graph G with on induced edge labeling $f^*:E(G) \rightarrow \{0,1\}$ defined by $f^*(e=uv) = |f(u)-f(v)|$ is called a cordial labeling if $|v_f(0)-v_f(1)| \leq 1$ and $|e_f(0)-e_f(1)| \leq 1$. A graph G is a cordial graph if G admits a cordial labelling.

The concept of cordial labeling was introduced by Ebrahim Cahit (Turkey) as a weaker version of graceful and harmonious labelings. He also investigated several results on this newly defined concept.

Definition 1.3:

Let G be a graph with vertex set $V(G)$ and edge set $E(G)$ and let $f: E(G) \rightarrow \{0,1\}$ define a mapping f^* on $V(G)$ by $f^*(V) = \sum f(uv) / uv \in E(G) \pmod{2}$. The function f is called an E-cordial labeling of G if $|v_f(0)-v_f(1)| \leq 1$ and $|e_f(0)-e_f(1)| \leq 1$. A graph G is called E-cordial graph if G admits an E-cordial labeling.

In 1997,Yilmag and Cahit[3] introduced E-cordial labeling as a weaker version of edge-graceful labeling and with the blend of cordial labeling.

Definition 1.4:

The Peterson graph is a 3-regular graph with 10 vertices and 15 edges.

Definition 1.5:

The Fan graph is denoted by F_n and described as $F_n=P_n+K_1$, where P_n indicates the path graph with n vertices.

Definition 1.6:

The Helm graph H_n is the graph obtained from a wheel graph W_n by attaching a pendant vertex through an edge tip end rim vertex of W_n .

Definition 1.7:

The Flower graph Fl_n is the graph obtained from a helm H_n by joining each pendant vertices of the helm to the apex vertex. Here the pendant vertices of helm H_n are referred as extended vertices of Fl_n .

2. Main Results:

Theorem 2.1:

Peterson graph P_n admits prime E-cordial labeling.

Proof:

Peterson graph is a 3-regular graph with 10 vertices and 15 edges.

Let u_0,u_1,\dots,u_{14} be the edges and let v_0,v_1,\dots,v_9 be the vertices of the graph.

Let e_1,e_2,\dots,e_5 be the inner edges.

We defined the labeling as follows $f: E(G) \rightarrow \{1,2,3,5,\dots,15\}$ then the induced function $f^*(V) = \sum f(uv / uv \in E(G) \pmod{2})$

Thus the labeling defined above satisfies the conditions of prime E-cordial labeling.

Hence, the proof.

Illustration 2.2:

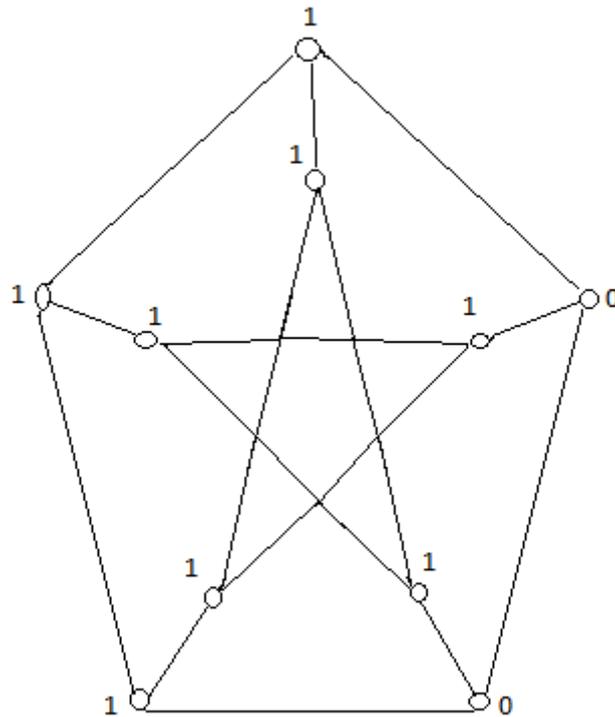


Figure 1: Prime E-cordial labeling of Peterson P_n graph

Theorem 2.3:

The fan graph F_n admits prime E-cordial labeling.

Proof:

Let F_n be a fan graph joining by a path P_n of length $n-1$.

Let u_0, u_1, \dots, u_{n-1} be the edges and let v_0, v_1, \dots, v_{n-1} be the vertices of the graph.

We defined the labeling function as follows $f: E(G) \rightarrow \{1, 2, 3, 5, \dots, n\}$ then the induced function $f^*(v) = \sum f(uv / uv \in E(G) \pmod{2})$

Thus the labeling defined above satisfies the conditions of prime E-cordial labeling. Hence, F_n is a prime E-cordial graph.

Illustration 2.4:

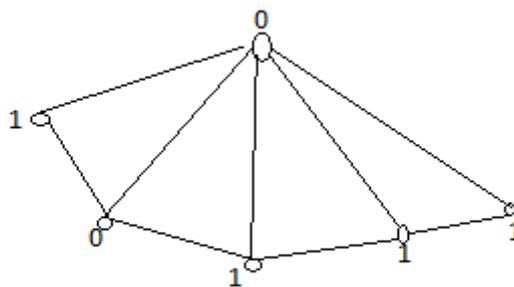


Figure 2: Prime E-cordial labeling of F_8

Theorem 2.5:

The flower graph fl_n admits prime E-cordial labeling.

Proof:

Let fl_n be a flower graph.

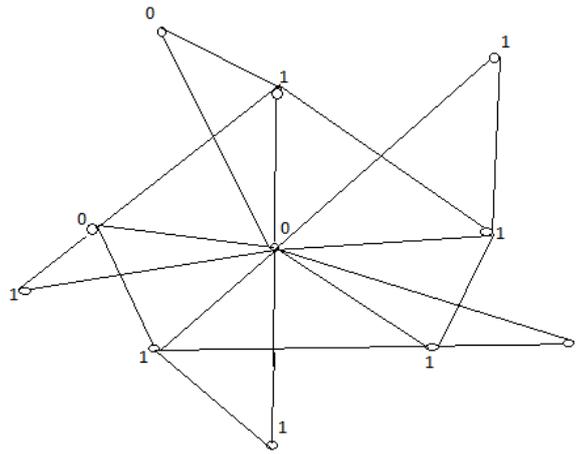
The flower graph fl_n joining by a path P_n of length $n-1$.

Let u_0 be the apex vertex u_1, u_2, \dots, u_n be the rim vertices and let $u_1^1, u_2^1, \dots, u_n^1$ be the external vertices.

We defined the labeling function as follows $f: E(G) \rightarrow \{1, 2, 3, \dots, n\}$ then the induced function.

$f^*(V) = \sum f(uv / uv \in E(G) \pmod{2})$

Thus the labeling defined above satisfies the conditions of prime E-cordial labeling. Thus, the flower graph fl_n is a prime E-cordial labeling.

Illustration 2.6:Figure 3: Prime E-cordial labeling of fl_5 .**Conclusion:**

In this paper, we have obtained prime E-cordial labeling for Peterson graph, Fan graph and the Flower graph. We further motivated to verify the above labeling process for some more special classes of graphs.

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