

EVALUATION OF RELIABILITY OF A PARALLEL CONFIGURATION BY USING PROBABILITY TREE ANALYSIS

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ABSTRACT:

Reliability networks containing six independent and non-identical units are studies with the aid of probability tree approach. Independent unit network configuration such as parallel network is analyzed. Expressions for system reliability, open mode and short mode failure probability are developed.

Keywords: Reliability, Open mode, Short mode

1. INTRODUCTION:

A device is said to have three states if it operates satisfactorily in its normal mode and fails in either short or open modes. Three-state devices can be arranged in redundant configurations such as parallel arrangements. Redundancy can generally be used to increase the reliability of a system without any change in the reliability of the individual devices that form the system. However, in the case of a system comprising three-state devices, redundancy may either increase or decrease the system reliability. This depends upon the dominant mode of component failure, configuration of the system and the number of redundant components.

In a probability tree, the number of links in each from its origin to its termination point represents the number of units or devices in the network. The total number of paths in a three-state device probability tree is given by 3^n , where n represents the number of units (i.e., three state devices), in a network. The success, open and short (closed) mode of each unit (i.e., three-state device) is assigned a conditional probability. The outcome of each unit is represented by the branching limbs of the probability tree. The total probability of system success is obtained by summing up the associated probabilities with the end point of the success path through the probability tree diagram. Similarly, the system open and short mode failure probabilities can also be obtained from the probability tree diagram.

2. NOTATIONS

The following symbols were used to develop the probability tree analysis

N_i Denotes the normal mode (i.e., success) of the i th unit
(i.e., i th path link success)

O_i Denotes the open mode failure state of the i th unit
(i.e., i th path link failure)

S_i Denotes the short (closed) mode failure state of the i th unit
(i.e., i th path link failure)

p_i Probability of being in state N_i

q_{oi} Probability of being in state O_i

q_{si} Probability of being in state S_i

Probability tree analysis for a six independent and non-identical unit three state device network:

The probability tree diagram for a six independent and non-identical unit three state device network is shown in Figures 2 to 10.

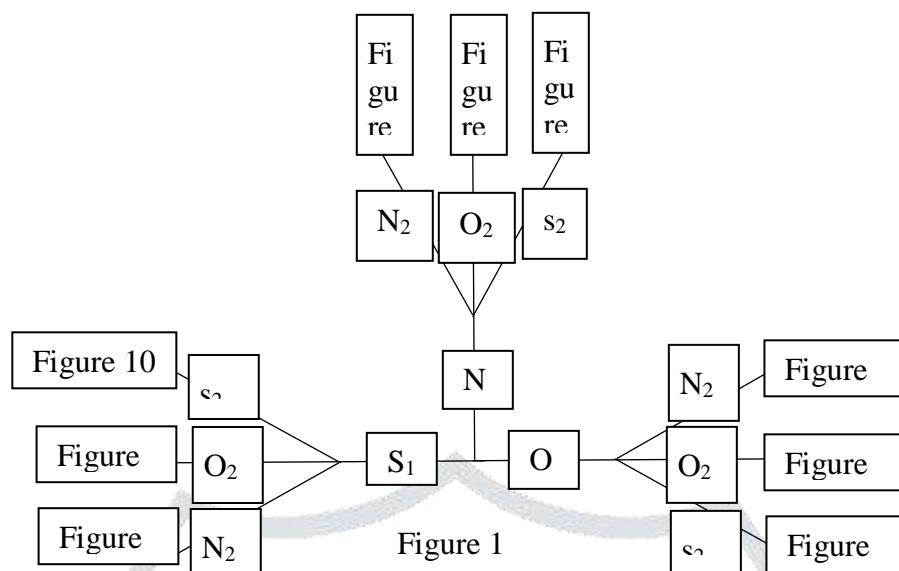


Figure 1

Figure 10

Figure

Figure

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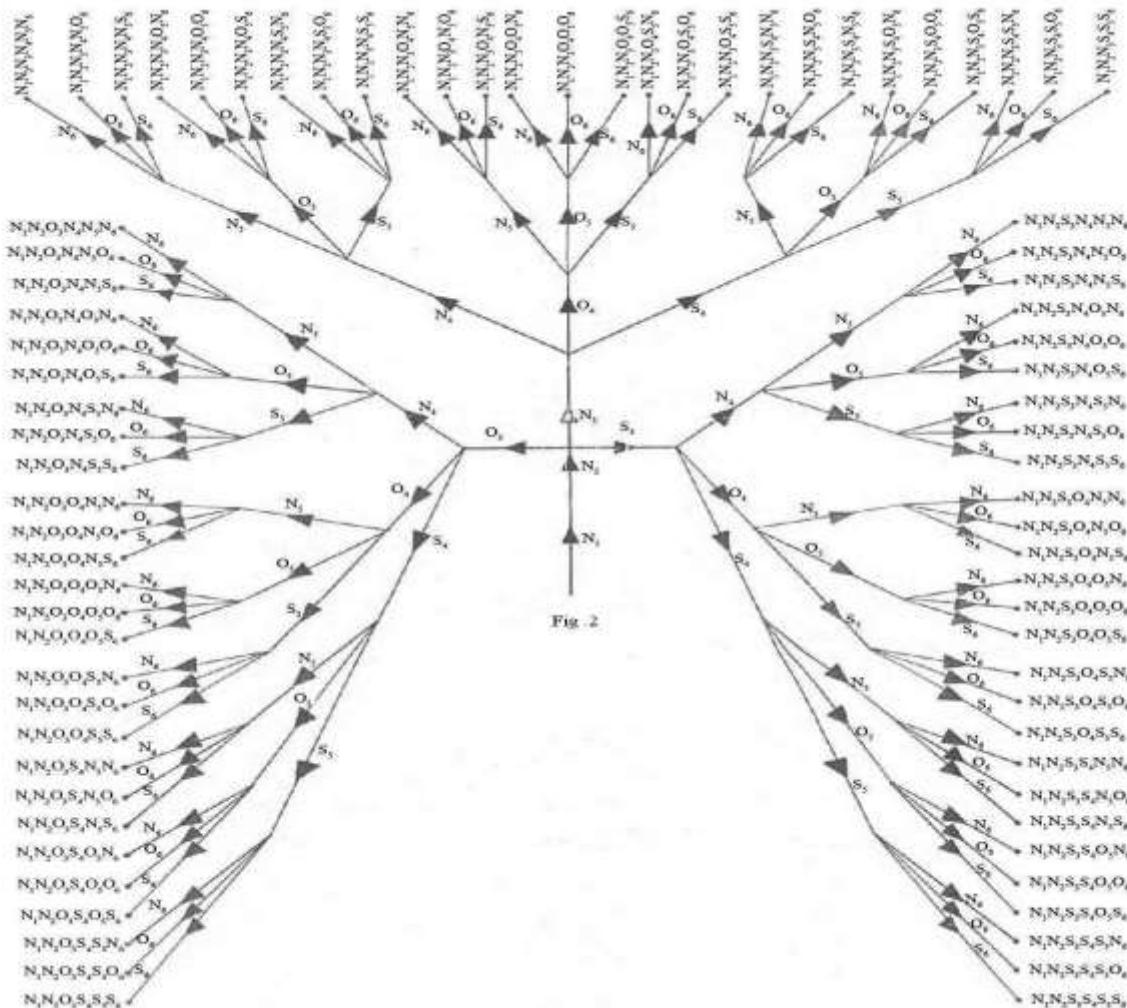


Fig. 2

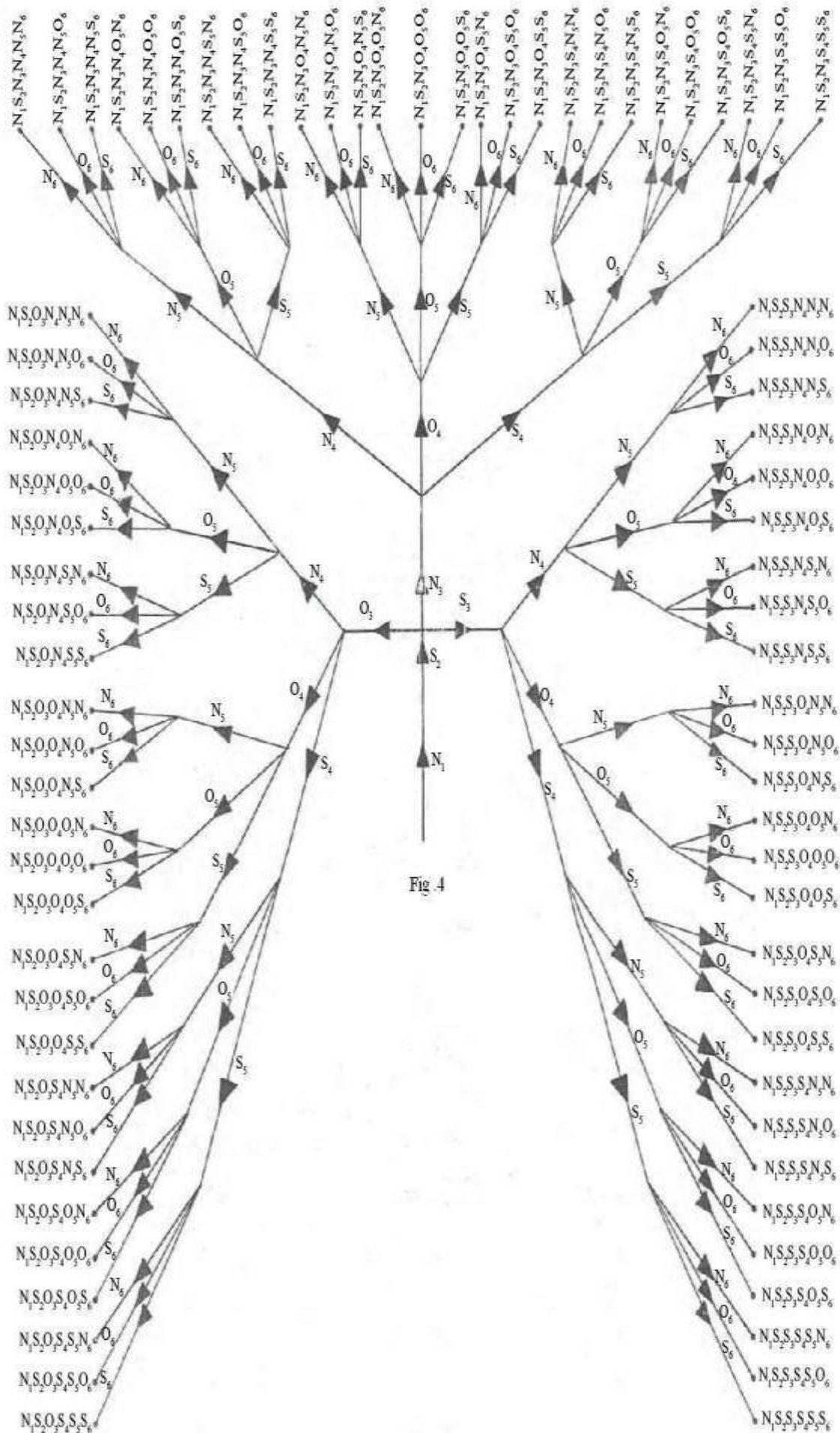


Fig. 4

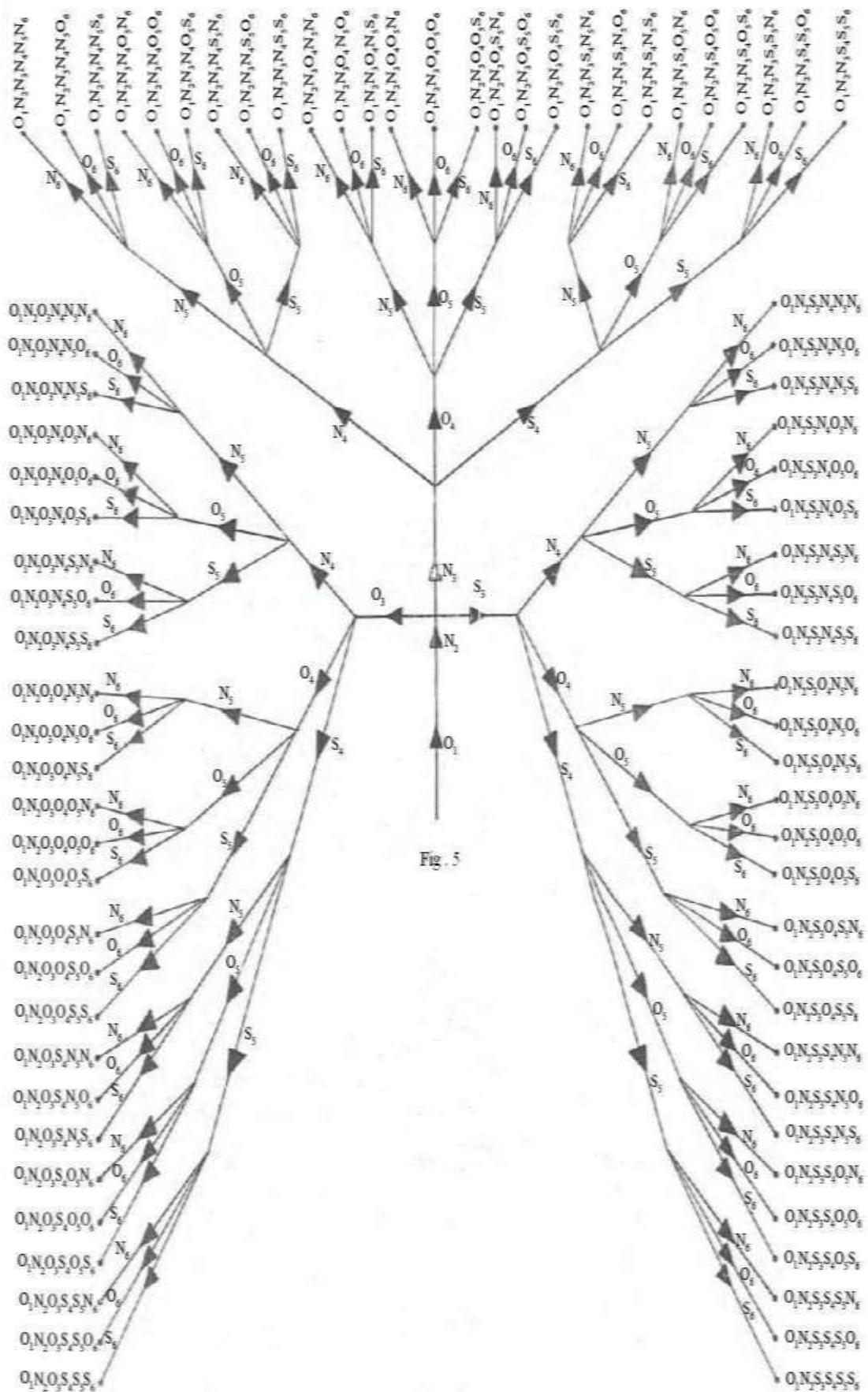


Fig. 5

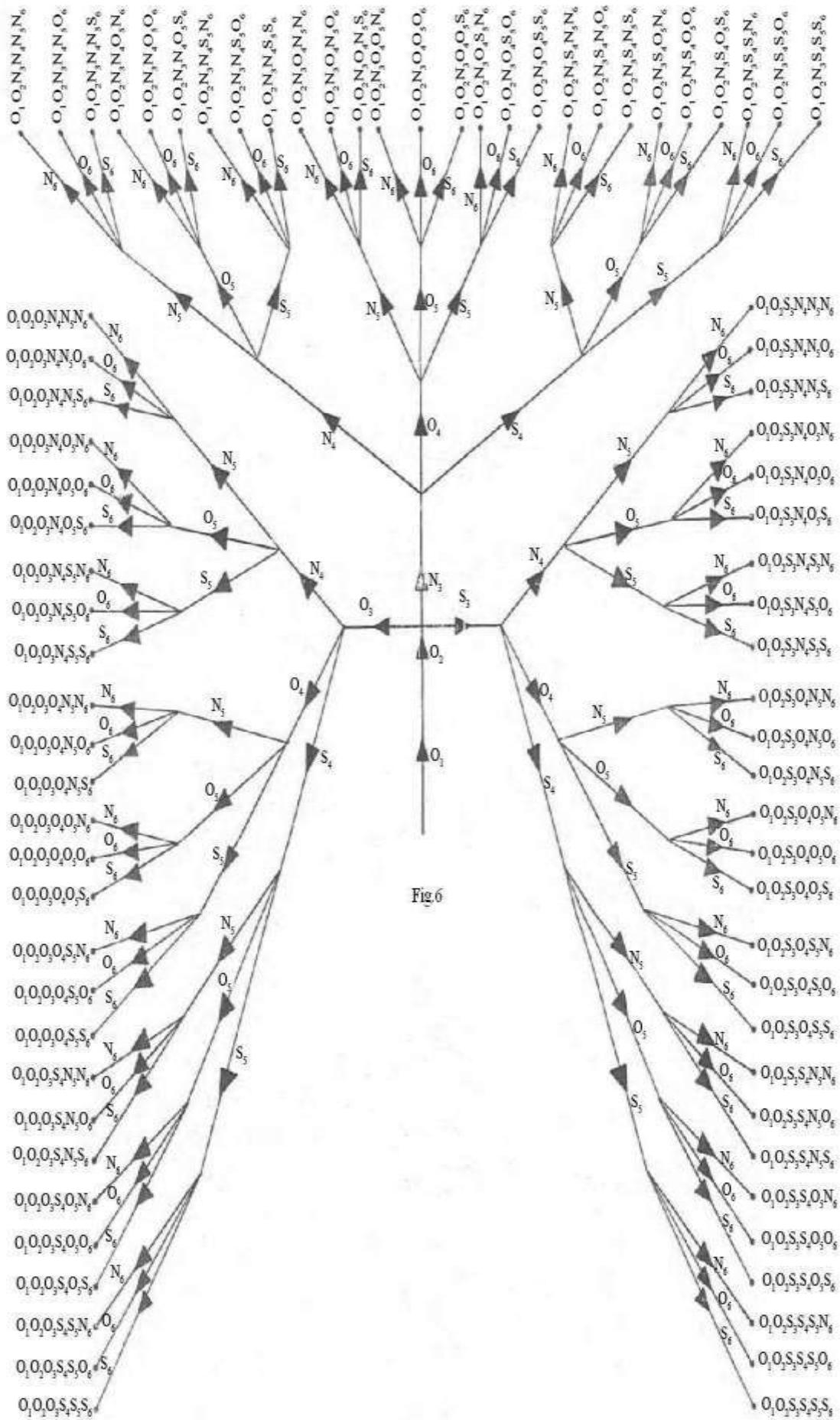


Fig.6

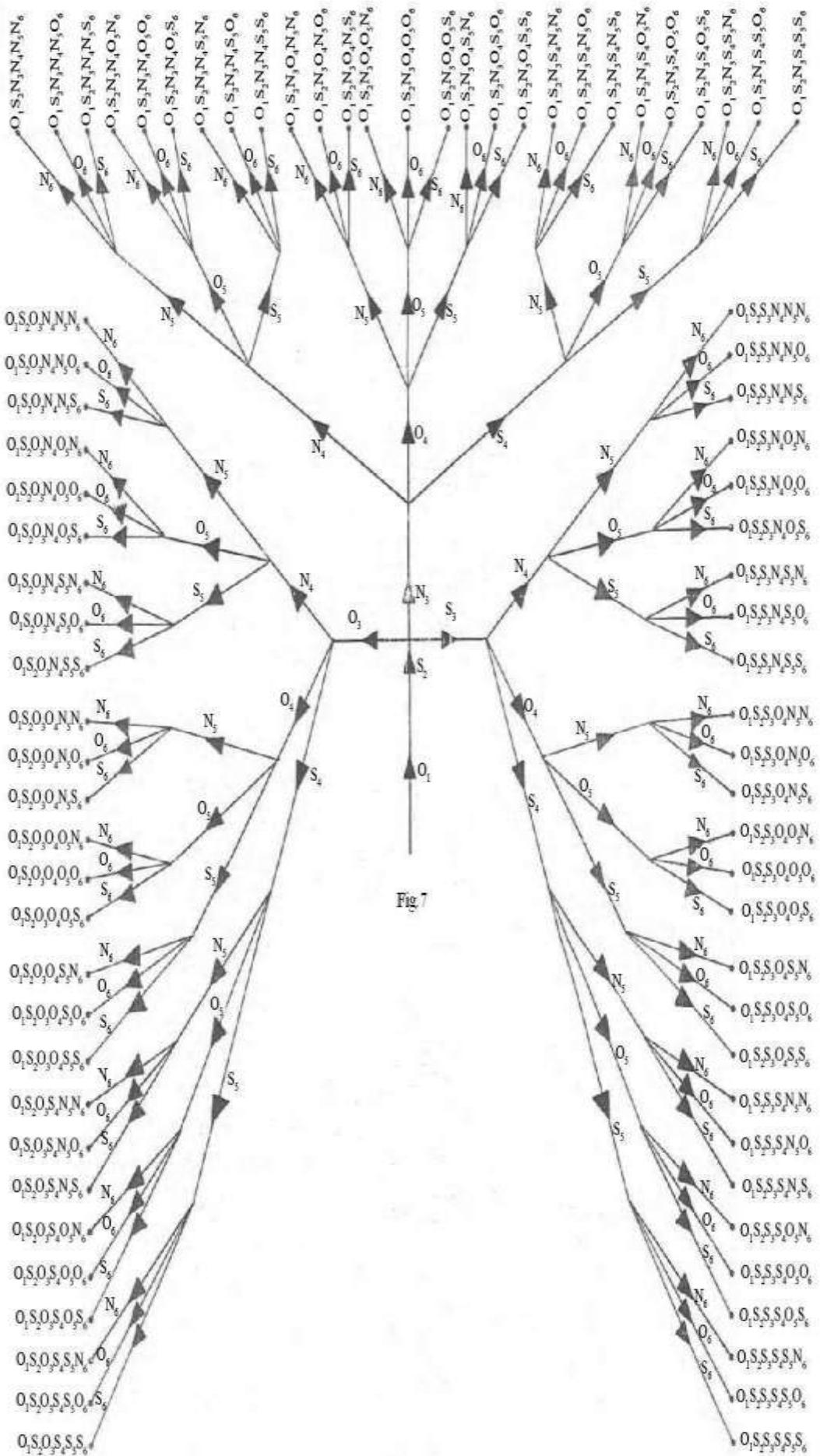


Fig 7

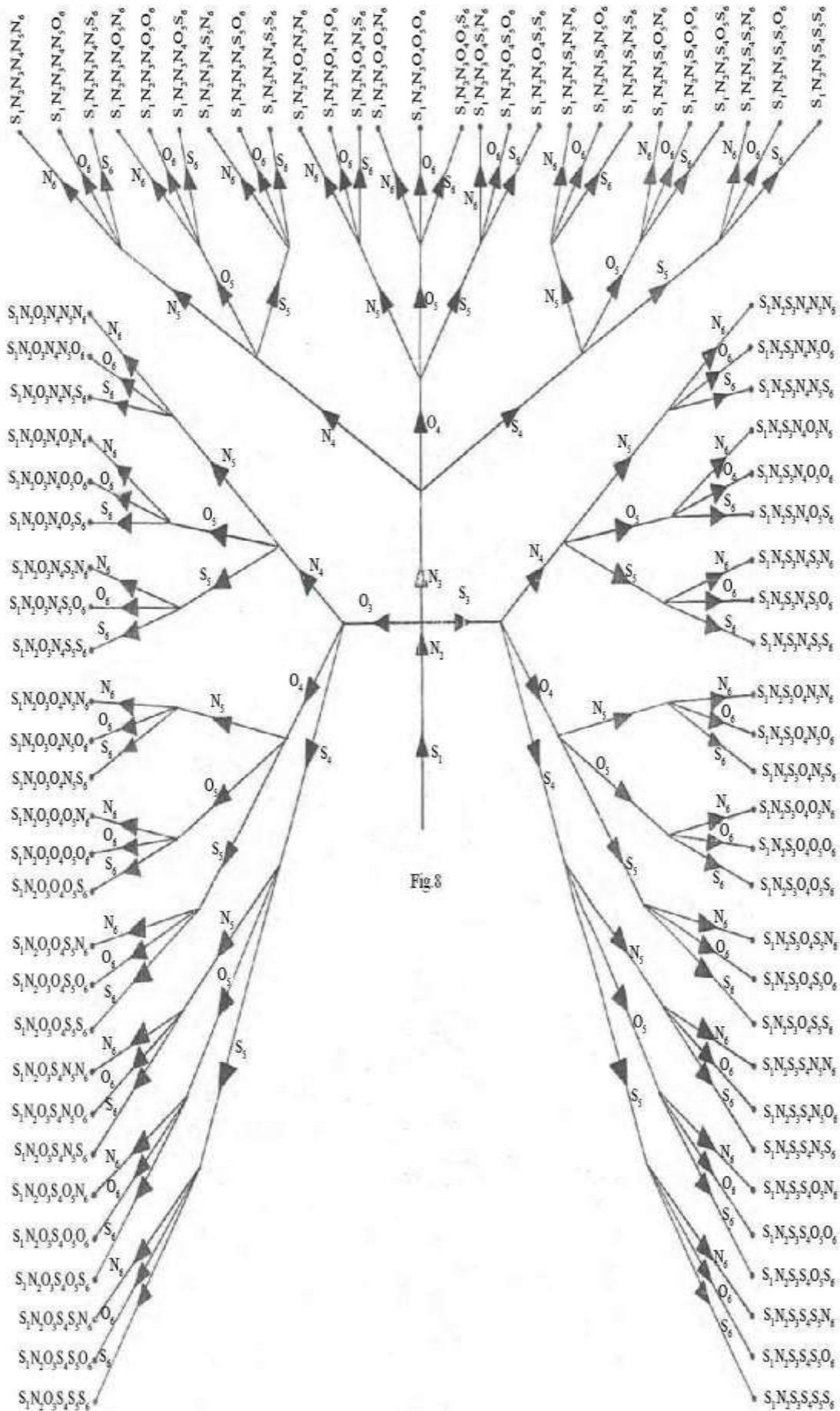


Fig. 3

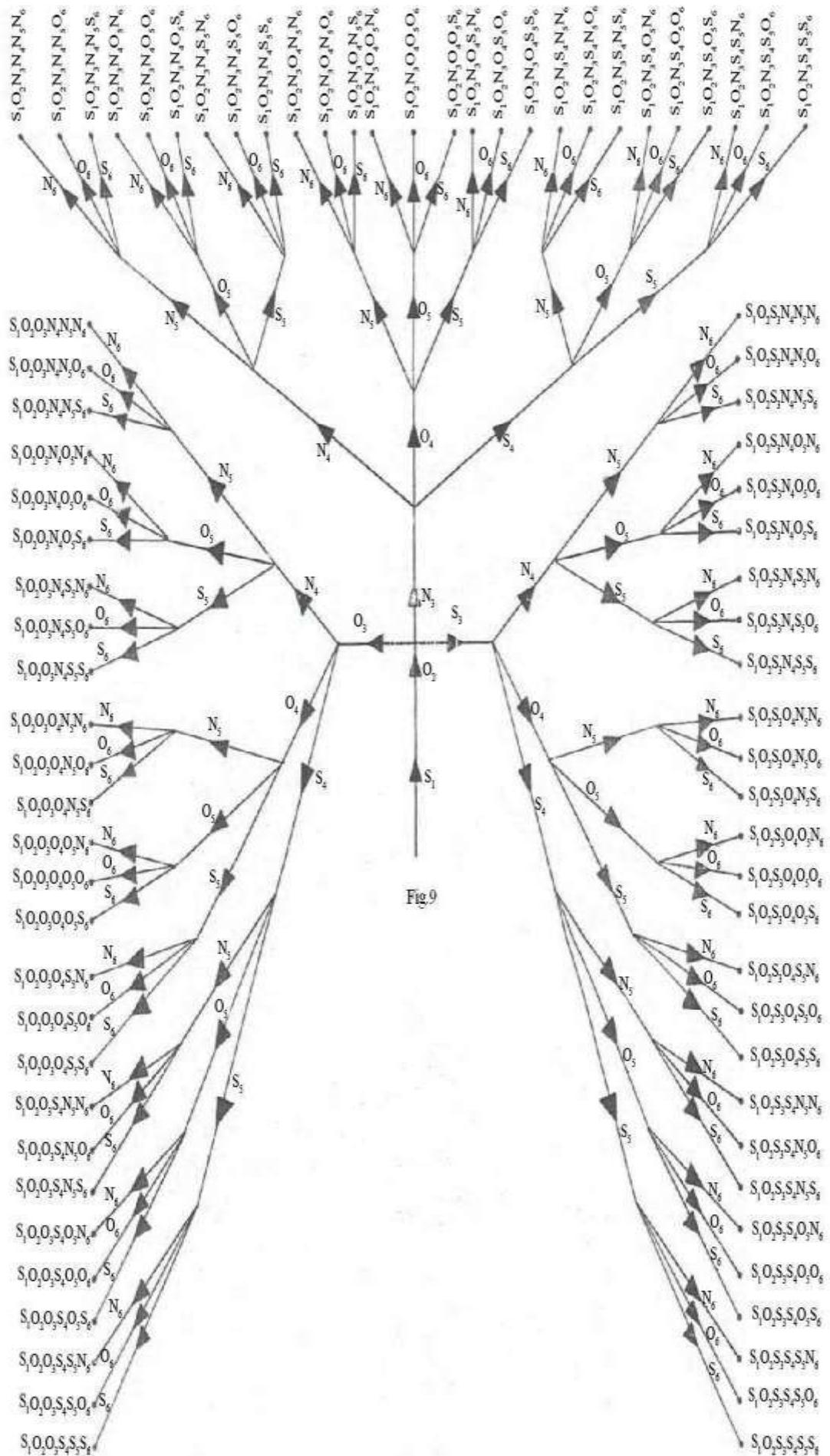


Fig. 9

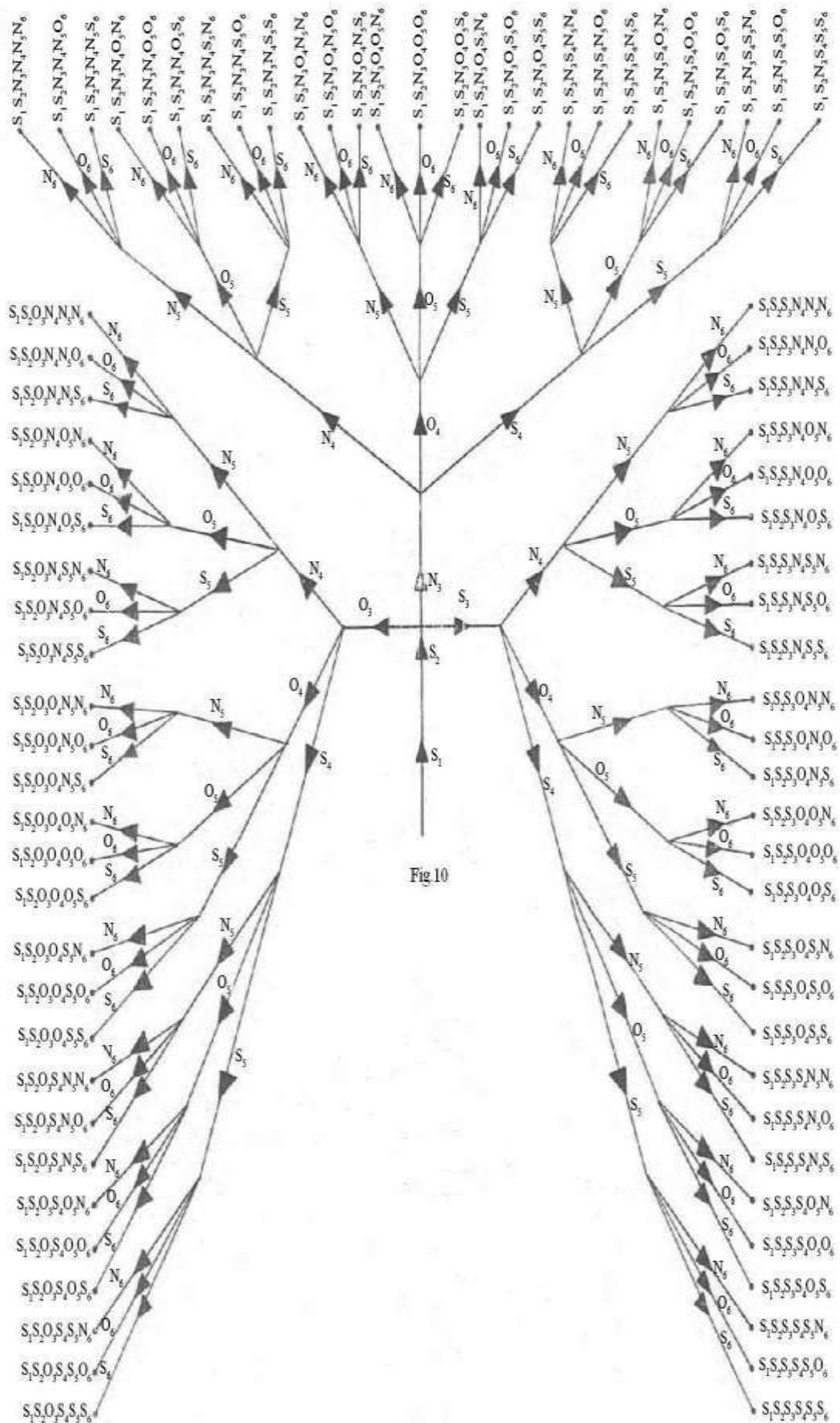
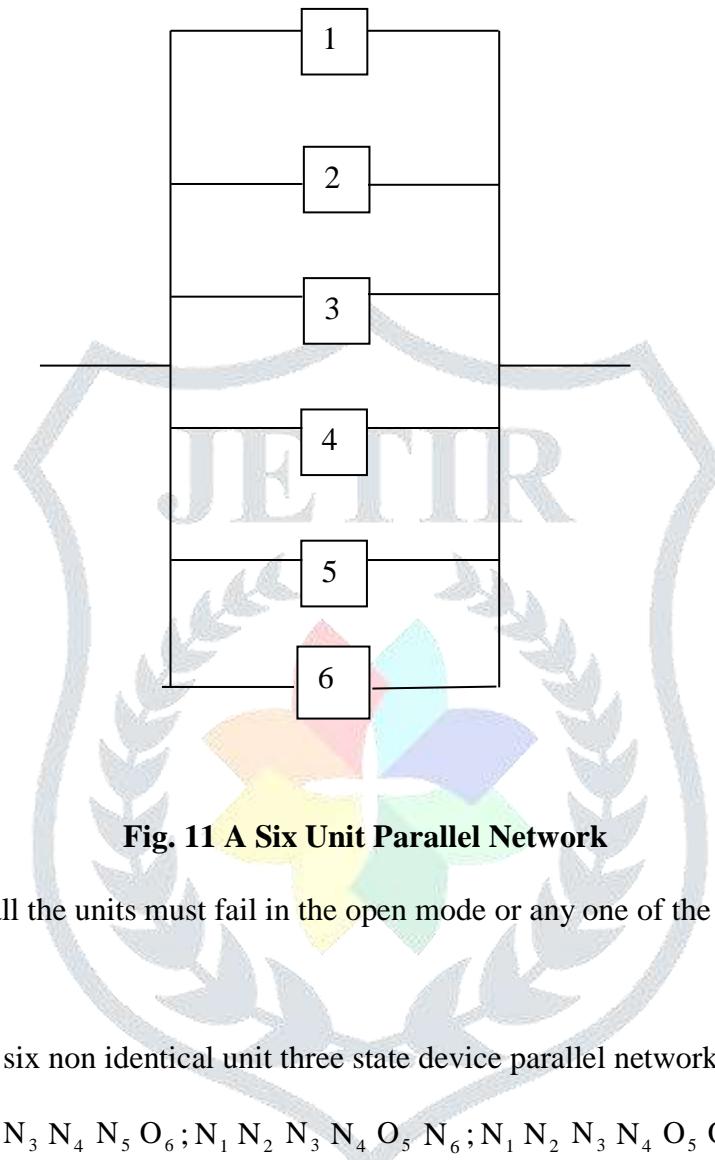


Fig. 10

4. PARALLEL CONFIGURATION:

A six independent and non-identical unit parallel network is shown in figure.



For a parallel configuration, all the units must fail in the open mode or any one of the units must fail in a short mode to cause the system to fail.

From figures 2 to 10, the six non identical unit three state device parallel network success paths are:

$N_1 N_2 N_3 N_4 N_5 N_6; N_1 N_2 N_3 N_4 N_5 O_6; N_1 N_2 N_3 N_4 O_5 N_6; N_1 N_2 N_3 N_4 O_5 O_6; N_1 N_2 N_3 O_4 N_5 N_6;$
 $N_1 N_2 N_3 O_4 N_5 O_6; N_1 N_2 N_3 O_4 O_5 N_6; N_1 N_2 N_3 O_4 O_5 O_6; N_1 N_2 O_3 N_4 N_5 N_6; N_1 N_2 O_3 N_4 N_5 O_6;$
 $N_1 N_2 O_3 N_4 O_5 N_6; N_1 N_2 O_3 N_4 O_5 O_6; N_1 N_2 O_3 O_4 N_5 N_6; N_1 N_2 O_3 O_4 N_5 O_6; N_1 N_2 O_3 O_4 O_5 N_6;$
 $N_1 N_2 O_3 O_4 O_5 O_6; N_1 O_2 N_3 N_4 N_5 N_6; N_1 O_2 N_3 N_4 N_5 O_6; N_1 O_2 N_3 N_4 O_5 N_6; N_1 O_2 N_3 N_4 O_5 O_6;$
 $N_1 O_2 N_3 O_4 N_5 N_6; N_1 O_2 N_3 O_4 N_5 O_6; N_1 O_2 N_3 O_4 O_5 N_6; N_1 O_2 N_3 O_4 O_5 O_6; N_1 O_2 O_3 N_4 N_5 N_6;$
 $N_1 O_2 O_3 N_4 N_5 O_6; N_1 O_2 O_3 N_4 O_5 N_6; N_1 O_2 O_3 N_4 O_5 O_6; N_1 O_2 O_3 O_4 N_5 N_6; N_1 O_2 O_3 O_4 N_5 O_6;$
 $N_1 O_2 O_3 O_4 O_5 N_6; N_1 O_2 O_3 O_4 O_5 O_6; O_1 N_2 N_3 N_4 N_5 N_6; O_1 N_2 N_3 N_4 N_5 O_6; O_1 N_2 N_3 N_4 O_5 N_6;$
 $O_1 N_2 N_3 N_4 O_5 O_6; O_1 N_2 N_3 O_4 N_5 N_6; O_1 N_2 N_3 O_4 N_5 O_6; O_1 N_2 N_3 O_4 O_5 N_6; O_1 N_2 N_3 O_4 O_5 O_6;$

$O_1 N_2 O_3 N_4 N_5 N_6; O_1 N_2 O_3 N_4 N_5 O_6; O_1 N_2 O_3 N_4 O_5 N_6; O_1 N_2 O_3 N_4 O_5 O_6; O_1 N_2 O_3 O_4 N_5 N_6;$
 $O_1 N_2 O_3 O_4 N_5 O_6; O_1 N_2 O_3 O_4 O_5 N_6; O_1 N_2 O_3 O_4 O_5 O_6; O_1 O_2 N_3 N_4 N_5 N_6; O_1 O_2 N_3 N_4 N_5 O_6;$
 $O_1 O_2 N_3 N_4 O_5 N_6; O_1 O_2 N_3 N_4 O_5 O_6; O_1 O_2 N_3 O_4 N_5 N_6; O_1 O_2 N_3 O_4 N_5 O_6; O_1 O_2 N_3 O_4 O_5 N_6;$
 $O_1 O_2 N_3 O_4 O_5 O_6; O_1 O_2 O_3 N_4 N_5 N_6; O_1 O_2 O_3 N_4 N_5 O_6; O_1 O_2 O_3 N_4 O_5 O_6; O_1 O_2 O_3 N_4 O_5 N_6;$
 $O_1 O_2 O_3 O_4 N_5 N_6; O_1 O_2 O_3 O_4 N_5 O_6; O_1 O_2 O_3 O_4 O_5 N_6.$

With the aid of above success paths, the reliability of the independent unit parallel network is given by

$$\begin{aligned}
 R_p = & p_1 p_2 p_3 p_4 p_5 p_6 + p_1 p_2 p_3 p_4 p_5 q_{o6} + p_1 p_2 p_3 p_4 q_{o5} p_6 + p_1 p_2 p_3 p_4 q_{o5} q_{o6} + p_1 p_2 p_3 q_{o4} p_5 p_6 \\
 & + p_1 p_2 p_3 q_{o4} p_5 q_{o6} + p_1 p_2 p_3 q_{o4} q_{o5} p_6 + p_1 p_2 p_3 q_{o4} q_{o5} q_{o6} + p_1 p_2 q_{o3} p_4 p_5 p_6 + p_1 p_2 q_{o3} p_4 p_5 q_{o6} \\
 & + p_1 p_2 q_{o3} p_4 q_{o5} p_6 + p_1 p_2 q_{o3} p_4 q_{o5} q_{o6} + p_1 p_2 q_{o3} q_{o4} p_5 p_6 + p_1 p_2 q_{o3} q_{o4} p_5 q_{o6} + p_1 p_2 q_{o3} q_{o4} q_{o5} p_6 \\
 & + p_1 p_2 q_{o3} q_{o4} q_{o5} q_{o6} + p_1 q_{o2} p_3 p_4 p_5 p_6 + p_1 q_{o2} p_3 p_4 p_5 q_{o6} + p_1 q_{o2} p_3 p_4 q_{o5} p_6 + p_1 q_{o2} p_3 p_4 q_{o5} q_{o6} \\
 & + p_1 q_{o2} p_3 q_{o4} p_5 p_6 + p_1 q_{o2} p_3 q_{o4} p_5 q_{o6} + p_1 q_{o2} p_3 q_{o4} q_{o5} p_6 + p_1 q_{o2} p_3 q_{o4} q_{o5} q_{o6} \\
 & + p_1 q_{o2} q_{o3} p_4 p_5 p_6 + p_1 q_{o2} q_{o3} p_4 p_5 q_{o6} + p_1 q_{o2} q_{o3} p_4 q_{o5} p_6 + p_1 q_{o2} q_{o3} p_4 q_{o5} q_{o6} + p_1 q_{o2} q_{o3} q_{o4} p_5 p_6 \\
 & + p_1 q_{o2} q_{o3} q_{o4} p_5 q_{o6} + p_1 q_{o2} q_{o3} q_{o4} q_{o5} p_6 + p_1 q_{o2} q_{o3} q_{o4} q_{o5} q_{o6} + q_{o1} p_2 p_3 p_4 p_5 p_6 + q_{o1} p_2 p_3 q_{o4} p_5 p_6 \\
 & + q_{o1} p_2 p_3 q_{o4} q_{o5} p_6 + q_{o1} p_2 p_3 q_{o4} q_{o5} q_{o6} + q_{o1} p_2 p_3 q_{o4} p_5 p_6 + q_{o1} p_2 p_3 q_{o4} p_5 q_{o6} + q_{o1} p_2 p_3 q_{o4} q_{o5} p_6 \\
 & + q_{o1} p_2 p_3 q_{o4} q_{o5} q_{o6} + q_{o1} p_2 q_{o3} p_4 p_5 p_6 + q_{o1} p_2 q_{o3} p_4 p_5 q_{o6} + q_{o1} p_2 q_{o3} q_{o4} p_5 p_6 \\
 & + q_{o1} p_2 q_{o3} q_{o4} p_5 q_{o6} + q_{o1} p_2 q_{o3} q_{o4} q_{o5} p_6 + q_{o1} p_2 q_{o3} q_{o4} q_{o5} q_{o6} + q_{o1} p_2 q_{o3} q_{o4} q_{o5} q_{o6} \\
 & + q_{o1} p_2 q_{o3} q_{o4} q_{o5} p_6 + q_{o1} p_2 q_{o3} q_{o4} q_{o5} q_{o6} + q_{o1} p_2 q_{o3} q_{o4} p_5 p_6 + q_{o1} p_2 q_{o3} q_{o4} p_5 q_{o6} + q_{o1} p_2 q_{o3} q_{o4} q_{o5} p_6 \\
 & + q_{o1} p_2 q_{o3} q_{o4} q_{o5} q_{o6} + q_{o1} q_{o2} p_3 q_{o4} p_5 p_6 + q_{o1} q_{o2} p_3 q_{o4} p_5 q_{o6} + q_{o1} q_{o2} p_3 q_{o4} q_{o5} p_6 \\
 & + q_{o1} q_{o2} q_{o3} p_4 p_5 p_6 + q_{o1} q_{o2} q_{o3} q_{o4} p_5 p_6 + q_{o1} q_{o2} q_{o3} q_{o4} p_5 q_{o6} + q_{o1} q_{o2} q_{o3} q_{o4} q_{o5} p_6 \\
 & + q_{o1} q_{o2} q_{o3} q_{o4} p_5 q_{o6} + q_{o1} q_{o2} q_{o3} q_{o4} q_{o5} p_6 + q_{o1} q_{o2} q_{o3} q_{o4} q_{o5} q_{o6} + q_{o1} q_{o2} q_{o3} q_{o4} q_{o5} q_{o6}.
 \end{aligned}$$

$$R_p = \prod_{i=1}^6 (1 - q_{s_i}) - \prod_{i=1}^6 q_{o_i} \quad (1)$$

The open mode failure path of the six non identical unit three state device parallel networks is $O_1 O_2 O_3 O_4 O_5 O_6$.

Thus the open mode failure probability of the six independent and non-identical unit parallel networks is

$$Q_{O(P)} = q_{o1} q_{o2} q_{o3} q_{o4} q_{o5} q_{o6} = \prod_{i=1}^6 q_{o_i} \quad (2)$$

As for the series case the above equation can be generalized for n -units. From figures 1 to 10, the short mode failure paths of the six independent and non-identical unit parallel network are

$N_1 N_2 N_3 N_4 N_5 S_6; N_1 N_2 N_3 N_4 O_5 S_6; N_1 N_2 N_3 N_4 S_5 N_6; N_1 N_2 N_3 N_4 S_5 O_6; N_1 N_2 N_3 N_4 S_5 S_6;$

$N_1 N_2 N_3 O_4 N_5 S_6; N_1 N_2 N_3 O_4 O_5 S_6; N_1 N_2 N_3 O_4 S_5 N_6; N_1 N_2 N_3 O_4 S_5 O_6; N_1 N_2 N_3 O_4 S_5 S_6;$

$N_1 N_2 N_3 S_4 N_5 N_6; N_1 N_2 N_3 S_4 N_5 O_6; N_1 N_2 N_3 S_4 N_5 S_6; N_1 N_2 N_3 S_4 O_5 N_6; N_1 N_2 N_3 S_4 O_5 O_6;$

$N_1 N_2 N_3 S_4 O_5 S_6; N_1 N_2 N_3 S_4 S_5 N_6; N_1 N_2 N_3 S_4 S_5 O_6; N_1 N_2 N_3 S_4 S_5 S_6; N_1 N_2 O_3 N_4 N_5 S_6;$

$N_1 N_2 O_3 N_4 O_5 S_6; N_1 N_2 O_3 N_4 S_5 N_6; N_1 N_2 O_3 N_4 S_5 O_6; N_1 N_2 O_3 N_4 S_5 S_6; N_1 N_2 O_3 O_4 N_5 S_6;$

$N_1 N_2 O_3 O_4 O_5 S_6; N_1 N_2 O_3 O_4 S_5 N_6; N_1 N_2 O_3 O_4 S_5 O_6; N_1 N_2 O_3 O_4 S_5 S_6; N_1 N_2 O_3 S_4 N_5 N_6;$

$N_1 N_2 O_3 S_4 N_5 O_6; N_1 N_2 O_3 S_4 N_5 S_6; N_1 N_2 O_3 S_4 O_5 N_6; N_1 N_2 O_3 S_4 O_5 O_6; N_1 N_2 O_3 S_4 O_5 S_6;$

$N_1 N_2 O_3 S_4 S_5 N_6; N_1 N_2 O_3 S_4 S_5 O_6; N_1 N_2 O_3 S_4 S_5 S_6; N_1 N_2 S_3 N_4 N_5 N_6; N_1 N_2 S_3 N_4 N_5 O_6;$

$N_1 N_2 S_3 N_4 N_5 S_6; N_1 N_2 S_3 N_4 O_5 N_6; N_1 N_2 S_3 N_4 O_5 O_6; N_1 N_2 S_3 N_4 O_5 S_6; N_1 N_2 S_3 N_4 S_5 N_6;$

$N_1 N_2 S_3 N_4 S_5 O_6; N_1 N_2 S_3 N_4 S_5 S_6; N_1 N_2 S_3 O_4 N_5 N_6; N_1 N_2 S_3 O_4 N_5 O_6; N_1 N_2 S_3 O_4 N_5 S_6;$

$N_1 N_2 S_3 O_4 O_5 N_6; N_1 N_2 S_3 O_4 O_5 O_6; N_1 N_2 S_3 O_4 O_5 S_6; N_1 N_2 S_3 O_4 S_5 N_6; N_1 N_2 S_3 O_4 S_5 O_6;$

$N_1 N_2 S_3 O_4 S_5 S_6; N_1 N_2 S_3 S_4 N_5 N_6; N_1 N_2 S_3 S_4 N_5 O_6; N_1 N_2 S_3 S_4 N_5 S_6; N_1 N_2 S_3 S_4 O_5 N_6;$

$N_1 N_2 S_3 S_4 O_5 O_6; N_1 N_2 S_3 S_4 O_5 S_6; N_1 N_2 S_3 S_4 S_5 N_6; N_1 N_2 S_3 S_4 S_5 O_6; N_1 N_2 S_3 S_4 S_5 S_6;$

$N_1 O_2 N_3 N_4 N_5 S_6; N_1 O_2 N_3 N_4 O_5 S_6; N_1 O_2 N_3 N_4 S_5 N_6; N_1 O_2 N_3 N_4 S_5 O_6; N_1 O_2 N_3 N_4 S_5 S_6;$

$N_1 O_2 N_3 O_4 N_5 S_6; N_1 O_2 N_3 O_4 O_5 S_6; N_1 O_2 N_3 O_4 S_5 N_6; N_1 O_2 N_3 O_4 S_5 O_6; N_1 O_2 N_3 O_4 S_5 S_6;$

$N_1 O_2 N_3 S_4 N_5 N_6; N_1 O_2 N_3 S_4 N_5 O_6; N_1 O_2 N_3 S_4 N_5 S_6; N_1 O_2 N_3 S_4 O_5 N_6; N_1 O_2 N_3 S_4 O_5 O_6;$

$N_1 O_2 N_3 S_4 O_5 S_6; N_1 O_2 N_3 S_4 S_5 N_6; N_1 O_2 N_3 S_4 S_5 O_6; N_1 O_2 N_3 S_4 S_5 S_6; N_1 O_2 O_3 N_4 N_5 S_6;$

$N_1 O_2 O_3 N_4 O_5 S_6; N_1 O_2 O_3 N_4 S_5 N_6; N_1 O_2 O_3 N_4 S_5 O_6; N_1 O_2 O_3 N_4 S_5 S_6; N_1 O_2 O_3 O_4 N_5 S_6;$

$N_1 O_2 O_3 O_4 O_5 S_6; N_1 O_2 O_3 O_4 O_5 O_6; N_1 O_2 O_3 O_4 O_5 S_6; N_1 O_2 O_3 O_4 O_5 O_6; N_1 O_2 O_3 S_4 N_5 N_6;$

$N_1 O_2 O_3 S_4 N_5 O_6; N_1 O_2 O_3 S_4 N_5 S_6; N_1 O_2 O_3 S_4 O_5 N_6; N_1 O_2 O_3 S_4 O_5 O_6; N_1 O_2 O_3 S_4 O_5 S_6;$

$N_1 O_2 O_3 S_4 S_5 N_6; N_1 O_2 O_3 S_4 S_5 O_6; N_1 O_2 O_3 S_4 S_5 S_6; N_1 O_2 S_3 N_4 N_5 N_6; N_1 O_2 S_3 N_4 N_5 O_6;$

$N_1 O_2 S_3 N_4 N_5 S_6; N_1 O_2 S_3 N_4 O_5 N_6; N_1 O_2 S_3 N_4 O_5 O_6; N_1 O_2 S_3 N_4 O_5 S_6; N_1 O_2 S_3 N_4 S_5 N_6;$

$N_1 O_2 S_3 N_4 S_5 O_6; N_1 O_2 S_3 N_4 S_5 S_6; N_1 O_2 S_3 O_4 N_5 N_6; N_1 O_2 S_3 O_4 N_5 O_6; N_1 O_2 S_3 O_4 N_5 S_6;$

N₁O₂S₃O₄O₅N₆; N₁O₂S₃O₄O₅O₆; N₁O₂S₃O₄O₅S₆; N₁O₂S₃O₄S₅N₆; N₁O₂S₃O₄S₅O₆;

N₁O₂S₃O₄S₅S₆; N₁O₂S₃S₄N₅N₆; N₁O₂S₃S₄N₅O₆; N₁O₂S₃S₄N₅S₆; N₁O₂S₃S₄O₅N₆;

N₁O₂S₃S₄O₅O₆; N₁O₂S₃S₄O₅S₆; N₁O₂S₃S₄S₅N₆; N₁O₂S₃S₄S₅O₆; N₁O₂S₃S₄S₅S₆;

N₁S₂N₃N₄N₅N₆; N₁S₂N₃N₄N₅O₆; N₁S₂N₃N₄N₅S₆; N₁S₂N₃N₄O₅N₆; N₁S₂N₃N₄O₅O₆;

N₁S₂N₃N₄O₅S₆; N₁S₂N₃N₄S₅N₆; N₁S₂N₃N₄S₅O₆; N₁S₂N₃N₄S₅S₆; N₁S₂N₃O₄N₅N₆;

N₁S₂N₃O₄N₅O₆; N₁S₂N₃O₄S₅; N₁S₂N₃O₄S₅N₆; N₁S₂N₃O₄S₅O₆; N₁S₂N₃O₄S₅S₆;

N₁S₂N₃O₄S₅N₆; N₁S₂N₃O₄S₅O₆; N₁S₂N₃O₄S₅S₆; N₁S₂N₃S₄N₅N₆; N₁S₂N₃S₄N₅O₆;

N₁S₂N₃S₄N₅S₆; N₁S₂N₃S₄O₅N₆; N₁S₂N₃S₄O₅O₆; N₁S₂N₃S₄O₅S₆; N₁S₂N₃S₄O₅S₆;

N₁S₂N₃S₄O₅O₆; N₁S₂N₃O₄N₅N₆; N₁S₂N₃O₄N₅O₆; N₁S₂N₃O₄N₅S₆; N₁S₂N₃O₄O₅N₆;

N₁S₂N₃O₄O₅O₆; N₁S₂N₃O₄O₅S₆; N₁S₂N₃O₄S₅N₆; N₁S₂N₃O₄S₅O₆; N₁S₂N₃O₄S₅S₆;

N₁S₂O₃N₄N₅N₆; N₁S₂O₃N₄N₅O₆; N₁S₂O₃N₄N₅S₆; N₁S₂O₃S₄N₅N₆; N₁S₂O₃S₄N₅O₆;

N₁S₂O₃N₄N₅S₆; N₁S₂O₃N₄O₅N₆; N₁S₂O₃O₄N₅O₆; N₁S₂O₃O₄N₅S₆; N₁S₂O₃O₄O₅N₆;

N₁S₂O₃O₄O₅O₆; N₁S₂O₃O₄O₅S₆; N₁S₂O₃O₄S₅N₆; N₁S₂O₃O₄S₅O₆; N₁S₂O₃O₄S₅S₆;

N₁S₂O₃S₄N₅N₆; N₁S₂O₃S₄N₅O₆; N₁S₂O₃S₄N₅S₆; N₁S₂O₃S₄O₅N₆; N₁S₂O₃S₄O₅O₆;

N₁S₂O₃S₄O₅S₆; N₁S₂O₃S₄O₅O₆; N₁S₂O₃S₄O₅S₆; N₁S₂O₃S₄O₅O₆; N₁S₂O₃S₄O₅N₆;

N₁S₂O₃S₄O₅O₆; N₁S₂O₃S₄O₅S₆; N₁S₂O₃S₄N₅N₆; N₁S₂O₃S₄N₅O₆; N₁S₂O₃S₄N₅S₆;

N₁S₂O₃S₄O₅O₆; N₁S₂O₃S₄O₅S₆; N₁S₂O₃S₄N₅N₆; N₁S₂O₃S₄N₅O₆; N₁S₂O₃S₄N₅S₆;

S₁N₂N₃N₄N₅N₆; S₁N₂N₃N₄N₅O₆; S₁N₂N₃N₄N₅S₆; S₁N₂N₃N₄O₅N₆; S₁N₂N₃N₄O₅O₆;

S₁N₂N₃N₄O₅S₆; S₁N₂N₃N₄S₅N₆; S₁N₂N₃N₄S₅O₆; S₁N₂N₃N₄S₅S₆; S₁N₂N₃N₄O₅N₆;

S₁N₂N₃O₄N₅O₆; S₁N₂N₃O₄S₅N₆; S₁N₂N₃O₄S₅O₆; S₁N₂N₃O₄S₅S₆; S₁N₂N₃O₄O₅N₆;

S₁N₂N₃O₄S₅N₆; S₁N₂N₃O₄S₅O₆; S₁N₂N₃O₄S₅S₆; S₁N₂N₃S₄N₅N₆; S₁N₂N₃S₄N₅O₆;

S₁N₂N₃S₄N₅S₆; S₁N₂N₃S₄O₅N₆; S₁N₂N₃S₄O₅O₆; S₁N₂N₃S₄O₅S₆; S₁N₂N₃S₄S₅N₆;

S₁ S₂ S₃ N₄ S₅ O₆; S₁ S₂ S₃ N₄ S₅ S₆; S₁ S₂ S₃ O₄ N₅ N₆; S₁ S₂ S₃ O₄ N₅ O₆; S₁ S₂ S₃ O₄ N₅ S₆; S₁ S₂ S₃ O₄ O₅ N₆;

S₁ S₂ S₃ O₄ O₅ O₆; S₁ S₂ S₃ O₄ O₅ S₆; S₁ S₂ S₃ O₄ S₅ N₆; S₁ S₂ S₃ O₄ S₅ O₆; S₁ S₂ S₃ O₄ S₅ S₆;

S₁ S₂ S₃ S₄ N₅ N₆; S₁ S₂ S₃ S₄ N₅ O₆; S₁ S₂ S₃ S₄ N₅ S₆; S₁ S₂ S₃ S₄ O₅ N₆; S₁ S₂ S₃ S₄ O₅ O₆; S₁ S₂ S₃ S₄ O₅ S₆; S₁ S₂ S₃ S₄ O₅ S₆;

S₁ S₂ N₃ N₄ N₅ S₆; S₁ S₂ N₃ N₄ O₅ N₆; S₁ S₂ N₃ N₄ O₅ O₆; S₁ S₂ N₃ N₄ O₅ S₆; S₁ S₂ N₃ N₄ O₅ S₆;

S₁ S₂ N₃ N₄ S₅ O₆; S₁ S₂ N₃ N₄ S₅ S₆; S₁ S₂ N₃ O₄ N₅ N₆; S₁ S₂ N₃ O₄ N₅ O₆; S₁ S₂ N₃ O₄ N₅ S₆;

S₁ S₂ N₃ O₄ O₅ N₆; S₁ S₂ N₃ O₄ O₅ O₆; S₁ S₂ N₃ O₄ O₅ S₆; S₁ S₂ N₃ O₄ S₅ N₆; S₁ S₂ N₃ O₄ S₅ O₆;

S₁ S₂ N₃ O₄ S₅ S₆; S₁ S₂ N₃ S₄ N₅ N₆; S₁ S₂ N₃ S₄ N₅ O₆; S₁ S₂ N₃ S₄ N₅ S₆; S₁ S₂ N₃ S₄ O₅ N₆;

S₁ S₂ N₃ S₄ O₅ O₆; S₁ S₂ N₃ S₄ O₅ S₆; S₁ S₂ N₃ S₄ S₅ N₆; S₁ S₂ N₃ S₄ S₅ O₆; S₁ S₂ N₃ S₄ S₅ S₆;

S₁ S₂ N₃ S₄ O₅ S₆; S₁ S₂ N₃ S₄ O₅ S₆; S₁ S₂ N₃ S₄ O₅ S₆; S₁ S₂ N₃ S₄ O₅ S₆; S₁ S₂ N₃ S₄ O₅ S₆;

S₁ S₂ N₃ S₄ O₅ S₆; S₁ S₂ N₃ S₄ O₅ S₆; S₁ S₂ N₃ S₄ O₅ S₆; S₁ S₂ N₃ S₄ O₅ S₆; S₁ S₂ N₃ S₄ O₅ S₆;

S₁ S₂ N₃ S₄ O₅ S₆; S₁ S₂ N₃ S₄ O₅ S₆; S₁ S₂ N₃ S₄ O₅ S₆; S₁ S₂ N₃ S₄ O₅ S₆; S₁ S₂ N₃ S₄ O₅ S₆;

S₁ S₂ N₃ S₄ O₅ S₆; S₁ S₂ N₃ S₄ O₅ S₆; S₁ S₂ N₃ S₄ O₅ S₆; S₁ S₂ N₃ S₄ O₅ S₆; S₁ S₂ N₃ S₄ O₅ S₆;

S₁ O₂ N₃ N₄ N₅ N₆; S₁ O₂ N₃ N₄ N₅ O₆; S₁ O₂ N₃ N₄ N₅ S₆; S₁ O₂ N₃ N₄ O₅ N₆; S₁ O₂ N₃ N₄ O₅ O₆;

S₁ O₂ N₃ N₄ O₅ O₆; S₁ O₂ N₃ N₄ O₅ S₆; S₁ O₂ N₃ N₄ S₅ N₆; S₁ O₂ N₃ N₄ S₅ O₆; S₁ O₂ N₃ N₄ S₅ S₆;

S₁ O₂ N₃ N₄ S₅ S₆; S₁ O₂ N₃ O₄ N₅ N₆; S₁ O₂ N₃ O₄ N₅ O₆; S₁ O₂ N₃ O₄ N₅ S₆; S₁ O₂ N₃ O₄ O₅ N₆;

S₁ O₂ N₃ O₄ O₅ O₆; S₁ O₂ N₃ O₄ O₅ S₆; S₁ O₂ N₃ O₄ S₅ N₆; S₁ O₂ N₃ O₄ S₅ O₆; S₁ O₂ N₃ O₄ S₅ S₆;

S₁ O₂ N₃ S₄ N₅ N₆; S₁ O₂ N₃ S₄ N₅ O₆; S₁ O₂ N₃ S₄ N₅ S₆; S₁ O₂ N₃ S₄ O₅ N₆; S₁ O₂ N₃ S₄ O₅ O₆;

S₁ O₂ N₃ S₄ O₅ O₆; S₁ O₂ N₃ S₄ O₅ S₆; S₁ O₂ N₃ S₄ S₅ N₆; S₁ O₂ N₃ S₄ S₅ O₆; S₁ O₂ N₃ S₄ S₅ S₆;

O₁ N₂ N₃ N₄ O₅ S₆; O₁ N₂ N₃ N₄ S₅ N₆; O₁ N₂ N₃ N₄ S₅ O₆; O₁ N₂ N₃ N₄ S₅ S₆; O₁ N₂ N₃ O₄ N₅ S₆;

O₁ N₂ N₃ O₄ O₅ S₆; O₁ N₂ N₃ O₄ O₅ O₆; O₁ N₂ N₃ O₄ O₅ S₆; O₁ N₂ N₃ O₄ S₅ N₆; O₁ N₂ N₃ S₄ N₅ N₆;

O₁ N₂ N₃ S₄ N₅ O₆; O₁ N₂ N₃ S₄ N₅ S₆; O₁ N₂ N₃ O₄ N₅ S₆; O₁ N₂ O₃ N₄ O₅ S₆; O₁ N₂ N₃ S₄ S₅ N₆;

O₁ N₂ N₃ S₄ S₅ O₆; O₁ N₂ N₃ S₄ S₅ S₆; O₁ N₂ N₃ O₄ N₅ S₆; O₁ N₂ O₃ N₄ S₅ S₆;

O₁ N₂ O₃ N₄ S₅ O₆; O₁ N₂ O₃ N₄ S₅ S₆; O₁ N₂ O₃ O₄ N₅ S₆; O₁ N₂ O₃ O₄ O₅ S₆; O₁ N₂ O₃ O₄ S₅ N₆;
O₁ N₂ O₃ O₄ S₅ O₆; O₁ N₂ O₃ O₄ S₅ S₆; O₁ N₂ O₃ S₄ N₅ N₆; O₁ N₂ O₃ S₄ N₅ O₆; O₁ N₂ O₃ S₄ N₅ S₆;
O₁ N₂ O₃ S₄ O₅ N₆; O₁ N₂ O₃ S₄ O₅ O₆; O₁ N₂ O₃ S₄ O₅ S₆; O₁ N₂ O₃ S₄ S₅ N₆; O₁ N₂ O₃ S₄ S₅ O₆;
O₁ N₂ O₃ S₄ S₅ S₆; O₁ N₂ S₃ N₄ N₅ N₆; O₁ N₂ S₃ N₄ N₅ O₆; O₁ N₂ S₃ N₄ N₅ S₆; O₁ N₂ S₃ N₄ O₅ N₆;
O₁ N₂ S₃ N₄ O₅ O₆; O₁ N₂ S₃ N₄ O₅ S₆; O₁ N₂ S₃ N₄ S₅ N₆; O₁ N₂ S₃ N₄ S₅ O₆; O₁ N₂ S₃ N₄ S₅ S₆;
O₁ N₂ S₃ O₄ N₅ N₆; O₁ N₂ S₃ O₄ N₅ O₆; O₁ N₂ S₃ O₄ N₅ S₆; O₁ N₂ S₃ O₄ O₅ N₆; O₁ N₂ S₃ O₄ O₅ O₆;
O₁ N₂ S₃ O₄ O₅ S₆; O₁ N₂ S₃ O₄ S₅ N₆; O₁ N₂ S₃ O₄ S₅ O₆; O₁ N₂ S₃ O₄ S₅ S₆; O₁ N₂ S₃ S₄ N₅ N₆;
O₁ N₂ S₃ S₄ N₅ O₆; O₁ N₂ S₃ S₄ S₅ N₆; O₁ N₂ S₃ S₄ S₅ O₆; O₁ N₂ S₃ S₄ S₅ S₆; O₁ N₂ S₃ S₄ O₅ N₆;
O₁ N₂ S₃ S₄ O₅ O₆; O₁ N₂ S₃ S₄ O₅ S₆;
O₁ S₂ N₃ N₄ N₅ S₆; O₁ S₂ N₃ N₄ O₅ N₆; O₁ S₂ N₃ N₄ O₅ O₆; O₁ S₂ N₃ N₄ O₅ S₆; O₁ S₂ N₃ N₄ O₅ S₆; O₁ S₂ N₃ N₄ O₅ S₆;
O₁ S₂ N₃ N₄ S₅ O₆; O₁ S₂ N₃ N₄ S₅ S₆; O₁ S₂ N₃ O₄ N₅ N₆; O₁ S₂ N₃ O₄ N₅ O₆; O₁ S₂ N₃ O₄ N₅ S₆;
O₁ S₂ N₃ O₄ O₅ N₆; O₁ S₂ N₃ O₄ O₅ S₆;
O₁ S₂ N₃ O₄ O₅ S₆; O₁ S₂ N₃ O₄ S₅ N₆; O₁ S₂ N₃ O₄ S₅ O₆; O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆;
O₁ S₂ N₃ O₄ S₅ O₆; O₁ S₂ N₃ O₄ S₅ S₆;
O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆;
O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆;
O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆;
O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆;
O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆; O₁ S₂ N₃ O₄ S₅ S₆;

O₁S₂S₃S₄O₅S₆;O₁S₂S₃S₄N₆;O₁S₂S₃S₄S₅O₆;O₁S₂S₃S₄S₅S₆;O₁O₂N₃N₄N₅S₆;

O₁O₂N₃N₄O₅S₆;O₁O₂N₃N₄S₅N₆;O₁O₂N₃N₄S₅O₆;O₁O₂N₃N₄S₅S₆;O₁O₂N₃O₄N₅S₆;

O₁O₂N₃O₄O₅S₆;O₁O₂N₃O₄S₅N₆;O₁O₂N₃O₄S₅O₆;O₁O₂N₃O₄S₅S₆;O₁O₂N₃S₄N₅N₆;

O₁O₂N₃S₄N₅O₆;O₁O₂N₃S₄N₅S₆;O₁O₂N₃S₄O₅N₆;O₁O₂N₃S₄O₅O₆;O₁O₂N₃S₄O₅S₆;

O₁O₂N₃S₄S₅N₆;O₁O₂N₃S₅O₆;O₁O₂N₃S₄S₅S₆;O₁O₂O₃N₄N₅S₆;O₁O₂O₃N₄O₅S₆;

O₁O₂O₃O₄S₅N₆;O₁O₂O₃O₄S₅O₆;O₁O₂O₃O₄S₅S₆;O₁O₂O₃S₄N₅N₆;O₁O₂O₃S₄N₅O₆;

O₁O₂O₃S₄N₅S₆;O₁O₂O₃S₄O₅N₆;O₁O₂O₃S₄O₅O₆;O₁O₂O₃S₄O₅S₆;O₁O₂O₃S₅N₆;

O₁O₂O₃S₅O₆;O₁O₂O₃S₅S₆;O₁O₂S₃N₄N₅N₆;O₁O₂S₃N₄N₅O₆;O₁O₂S₃N₄N₅S₆;

O₁O₂S₃N₄O₅N₆;O₁O₂S₃N₄O₅O₆;O₁O₂S₃N₄O₅S₆;O₁O₂S₃N₄S₅N₆;O₁O₂S₃N₄S₅O₆;

O₁O₂S₃N₄S₅S₆;O₁O₂S₃O₄N₅N₆;O₁O₂S₃O₄N₅O₆;O₁O₂S₃O₄N₅S₆;O₁O₂S₃O₄O₅N₆;

O₁O₂S₃O₄O₅O₆;O₁O₂S₃O₄O₅S₆;O₁O₂S₃O₄S₅N₆;O₁O₂S₃O₄S₅O₆;O₁O₂S₃O₄S₅S₆;

O₁O₂S₃S₄N₅O₆;O₁O₂S₃S₄N₅S₆;O₁O₂S₃S₄N₅N₆;O₁O₂S₃S₄O₅N₆;O₁O₂S₃S₄O₅O₆;

O₁O₂S₃S₄S₅N₆;O₁O₂S₃S₄S₅O₆;O₁O₂S₃S₄S₅S₆.

With the aid of short mode failure paths, the parallel network short mode failure probability is given by

$$\begin{aligned}
 Q_{S(P)} = & p_1 p_2 p_3 p_4 p_5 q_{S6} + p_1 p_2 p_3 p_4 q_{O5} q_{S6} + p_1 p_2 p_3 p_4 q_{S5} p_6 + p_1 p_2 p_3 p_4 q_{S5} q_{O6} + p_1 p_2 p_3 p_4 q_{S5} q_{S6} \\
 & + p_1 p_2 p_3 q_{O4} p_5 q_{S6} + p_1 p_2 p_3 q_{O4} q_{S6} + p_1 p_2 p_3 q_{O4} q_{S5} p_6 + p_1 p_2 p_3 q_{O4} q_{S5} q_{O6} + p_1 p_2 p_3 q_{O4} q_{S5} q_{S6} \\
 & + p_1 p_2 p_3 q_{S4} p_5 p_6 + p_1 p_2 p_3 q_{S4} p_5 q_{O6} + p_1 p_2 p_3 q_{S4} p_5 q_{S6} + p_1 p_2 p_3 q_{S4} q_{O5} p_6 + p_1 p_2 p_3 q_{S4} q_{O5} q_{O6} \\
 & + p_1 p_2 p_3 q_{S4} q_{O5} q_{S6} + p_1 p_2 p_3 q_{S4} q_{S5} p_6 + p_1 p_2 p_3 q_{S4} q_{S5} q_{O6} + p_1 p_2 p_3 q_{S4} q_{S5} q_{S6} + p_1 p_2 q_{O3} p_4 p_5 q_{S6} \\
 & + p_1 p_2 q_{O3} p_4 q_{O5} q_{S6} + p_1 p_2 q_{O3} p_4 q_{S5} p_6 + p_1 p_2 q_{O3} p_4 q_{S5} q_{O6} + p_1 p_2 q_{O3} p_4 q_{S5} q_{S6} + p_1 p_2 q_{O3} q_{O4} p_5 q_{S6} \\
 & + p_1 p_2 q_{O3} q_{O4} q_{S6} + p_1 p_2 q_{O3} q_{O4} q_{S5} p_6 + p_1 p_2 q_{O3} q_{O4} q_{S5} q_{O6} + p_1 p_2 q_{O3} q_{O4} q_{S5} q_{S6} + p_1 p_2 q_{O3} q_{S4} p_5 p_6 \\
 & + p_1 p_2 q_{O3} q_{S4} p_5 q_{O6} + p_1 p_2 q_{O3} q_{S4} q_{S6} + p_1 p_2 q_{O3} q_{S4} q_{S5} p_6 + p_1 p_2 q_{O3} q_{S4} q_{S5} q_{O6} + p_1 p_2 q_{O3} q_{S4} q_{S5} q_{S6} \\
 & + p_1 p_2 q_{O3} q_{S5} p_6 + p_1 p_2 q_{O3} q_{S5} q_{O6} + p_1 p_2 q_{O3} q_{S5} q_{S6} + p_1 p_2 q_{S3} p_4 p_5 p_6 + p_1 p_2 q_{S3} p_4 p_5 q_{S6} + p_1 p_2 q_{S3} p_4 q_{S5} p_6 \\
 & + p_1 p_2 q_{S3} p_4 q_{S5} q_{S6} + p_1 p_2 q_{S3} p_4 q_{O5} p_6 + p_1 p_2 q_{S3} p_4 q_{O5} q_{O6} + p_1 p_2 q_{S3} p_4 q_{O5} q_{S6} + p_1 p_2 q_{S3} p_4 q_{S5} q_{S6}
 \end{aligned}$$

$$\begin{aligned}
& + p_1 p_2 q_{S3} p_4 q_{S5} q_{O6} + p_1 p_2 q_{S3} p_4 q_{S5} q_{S6} + p_1 p_2 q_{S3} q_{O4} p_5 p_6 + p_1 p_2 q_{S3} q_{O4} p_5 q_{O6} + p_1 p_2 q_{S3} q_{O4} p_5 q_{S6} \\
& + p_1 p_2 q_{S3} q_{O4} q_{O5} p_6 + p_1 p_2 q_{S3} q_{O4} q_{O5} q_{O6} + p_1 p_2 q_{S3} q_{O4} q_{O5} q_{S6} + p_1 p_2 q_{S3} q_{O4} q_{S5} p_6 + p_1 p_2 q_{S3} q_{O4} q_{S5} q_{O6} \\
& + p_1 p_2 q_{S3} q_{O4} q_{S5} q_{S6} + p_1 p_2 q_{S3} q_{S4} p_5 p_6 + p_1 p_2 q_{S3} q_{S4} p_5 q_{O6} + p_1 p_2 q_{S3} q_{S4} p_5 q_{S6} + p_1 p_2 q_{S3} q_{S4} q_{O5} p_6 \\
& + p_1 p_2 q_{S3} q_{S4} q_{O5} q_{O6} + p_1 p_2 q_{S3} q_{S4} q_{O5} q_{S6} + p_1 p_2 q_{S3} q_{S4} q_{S5} p_6 + p_1 p_2 q_{S3} q_{S4} q_{S5} q_{O6} + p_1 p_2 q_{S3} q_{S4} q_{S5} q_{S6} \\
& + p_1 q_{O2} p_3 p_4 p_5 q_{S6} + p_1 q_{O2} p_3 p_4 q_{O5} q_{S6} + p_1 q_{O2} p_3 p_4 q_{S5} p_6 + p_1 q_{O2} p_3 p_4 q_{S5} q_{O6} + p_1 q_{O2} p_3 p_4 q_{S5} q_{S6} \\
& + p_1 q_{O2} p_3 q_{O4} p_5 q_{S6} + p_1 q_{O2} p_3 q_{O4} q_{O5} q_{S6} + p_1 q_{O2} p_3 q_{O4} q_{S5} p_6 + p_1 q_{O2} p_3 q_{O4} q_{S5} q_{O6} + p_1 q_{O2} p_3 q_{O4} q_{S5} q_{S6} \\
& + p_1 q_{O2} p_3 q_{S4} p_5 p_6 + p_1 q_{O2} p_3 q_{S4} p_5 q_{O6} + p_1 q_{O2} p_3 q_{S4} p_5 q_{S6} + p_1 q_{O2} p_3 q_{S4} q_{O5} p_6 + p_1 q_{O2} p_3 q_{S4} q_{O5} q_{O6} \\
& + p_1 q_{O2} p_3 q_{S4} q_{O5} q_{S6} + p_1 q_{O2} p_3 q_{S4} q_{S5} p_6 + p_1 q_{O2} p_3 q_{S4} q_{S5} q_{O6} + p_1 q_{O2} p_3 q_{S4} q_{S5} q_{S6} \\
& + p_1 q_{O2} q_{O3} p_4 p_5 q_{S6} + p_1 q_{O2} q_{O3} p_4 q_{O5} q_{S6} + p_1 q_{O2} q_{O3} p_4 q_{S5} p_6 + p_1 q_{O2} q_{O3} p_4 q_{S5} q_{O6} + p_1 q_{O2} q_{O3} p_4 q_{S5} q_{S6} + \\
& p_1 q_{O2} q_{O3} q_{O4} p_5 q_{S6} \\
& + p_1 q_{O2} q_{O3} q_{O4} q_{O5} q_{S6} + p_1 q_{O2} q_{O3} q_{O4} q_{S5} p_6 + p_1 q_{O2} q_{O3} q_{O4} q_{S5} q_{O6} + p_1 q_{O2} q_{O3} q_{O4} q_{S5} q_{S6} \\
& + p_1 q_{O2} q_{O3} q_{S4} p_5 p_6 + p_1 q_{O2} q_{O3} q_{S4} p_5 q_{O6} + p_1 q_{O2} q_{O3} q_{S4} p_5 q_{S6} + p_1 q_{O2} q_{O3} q_{S4} q_{O5} p_6 \\
& + p_1 q_{O2} q_{O3} q_{S4} q_{O5} q_{O6} + p_1 q_{O2} q_{O3} q_{S4} q_{S5} q_{S6} + p_1 q_{O2} q_{O3} q_{S4} q_{S5} p_6 + p_1 q_{O2} q_{O3} q_{S4} q_{S5} q_{O6} \\
& + p_1 q_{O2} q_{O3} q_{S4} q_{S5} q_{S6} + p_1 q_{O2} q_{S3} p_4 p_5 p_6 + p_1 q_{O2} q_{S3} p_4 p_5 q_{O6} + p_1 q_{O2} q_{S3} p_4 p_5 q_{S6} + p_1 q_{O2} q_{S3} p_4 q_{O5} p_6 \\
& + p_1 q_{O2} q_{S3} p_4 q_{O5} q_{O6} + p_1 q_{O2} q_{S3} p_4 q_{O5} q_{S6} + p_1 q_{O2} q_{S3} p_4 q_{S5} p_6 + p_1 q_{O2} q_{S3} p_4 q_{S5} q_{O6} + p_1 q_{O2} q_{S3} p_4 q_{S5} q_{S6} \\
& + p_1 q_{O2} q_{S3} q_{O4} p_5 p_6 + p_1 q_{O2} q_{S3} q_{O4} p_5 q_{O6} + p_1 q_{O2} q_{S3} q_{O4} p_5 q_{S6} + p_1 q_{O2} q_{S3} q_{O4} q_{O5} p_6 \\
& + p_1 q_{O2} q_{S3} q_{O4} q_{O5} q_{O6} + p_1 q_{O2} q_{S3} q_{O4} q_{O5} q_{S6} + p_1 q_{O2} q_{S3} q_{O4} q_{S5} p_6 + p_1 q_{O2} q_{S3} q_{O4} q_{S5} q_{O6} \\
& + p_1 q_{O2} q_{S3} q_{O4} q_{S5} q_{S6} + p_1 q_{O2} q_{S3} q_{S4} p_5 p_6 + p_1 q_{O2} q_{S3} q_{S4} p_5 q_{O6} + p_1 q_{O2} q_{S3} q_{S4} p_5 q_{S6} + p_1 q_{O2} q_{S3} q_{S4} q_{O5} p_6 \\
& + p_1 q_{O2} q_{S3} q_{S4} q_{O5} q_{O6} + p_1 q_{O2} q_{S3} q_{S4} q_{O5} q_{S6} + p_1 q_{O2} q_{S3} q_{S4} q_{S5} p_6 + p_1 q_{O2} q_{S3} q_{S4} q_{S5} q_{O6} \\
& + p_1 q_{O2} q_{S3} q_{S4} q_{S5} q_{S6} + p_1 q_{S2} p_3 p_4 p_5 p_6 + p_1 q_{S2} p_3 p_4 p_5 q_{O6} + p_1 q_{S2} p_3 p_4 p_5 q_{S6} + p_1 q_{S2} p_3 p_4 q_{O5} p_6 \\
& + p_1 q_{S2} p_3 p_4 q_{O5} q_{O6} + p_1 q_{S2} p_3 p_4 q_{O5} q_{S6} + p_1 q_{S2} p_3 p_4 q_{S5} p_6 + p_1 q_{S2} p_3 p_4 q_{S5} q_{O6} + p_1 q_{S2} p_3 p_4 q_{S5} q_{S6} \\
& + p_1 q_{S2} p_3 q_{O4} p_5 p_6 + p_1 q_{S2} p_3 q_{O4} p_5 q_{O6} + p_1 q_{S2} p_3 q_{O4} p_5 q_{S6} + p_1 q_{S2} p_3 q_{O4} q_{S5} p_6 + p_1 q_{S2} p_3 q_{O4} q_{S5} q_{O6} \\
& + p_1 q_{S2} p_3 q_{O4} q_{S5} q_{S6} + p_1 q_{S2} p_3 q_{S4} p_5 p_6 + p_1 q_{S2} p_3 q_{S4} p_5 q_{O6} + p_1 q_{S2} p_3 q_{S4} p_5 q_{S6} + p_1 q_{S2} p_3 q_{S4} q_{O5} p_6 \\
& + p_1 q_{S2} p_3 q_{S4} q_{O5} q_{O6} + p_1 q_{S2} p_3 q_{S4} q_{O5} q_{S6} + p_1 q_{S2} p_3 q_{S4} q_{S5} p_6 + p_1 q_{S2} p_3 q_{S4} q_{S5} q_{O6} + p_1 q_{S2} p_3 q_{S4} q_{S5} q_{S6}
\end{aligned}$$

$$\begin{aligned}
& + p_1 q_{S2} p_3 q_{S4} q_{S5} p_6 + p_1 q_{S2} p_3 q_{S4} q_{S5} q_{O6} + p_1 q_{S2} p_3 q_{S4} q_{S5} q_{S6} + p_1 q_{S2} q_{O3} p_4 p_5 p_6 + p_1 q_{S2} q_{O3} p_4 p_5 q_{O6} \\
& + p_1 q_{S2} q_{O3} p_4 p_5 q_{S6} + p_1 q_{S2} q_{O3} p_4 q_{O5} p_6 + p_1 q_{S2} q_{O3} p_4 q_{O5} q_{O6} + p_1 q_{S2} q_{O3} p_4 q_{O5} q_{S6} + p_1 q_{S2} q_{O3} p_4 q_{S5} p_6 \\
& + p_1 q_{S2} q_{O3} p_4 q_{S5} q_{O6} + p_1 q_{S2} q_{O3} p_4 q_{S5} q_{S6} + p_1 q_{S2} q_{O3} q_{O4} p_5 p_6 + p_1 q_{S2} q_{O3} q_{O4} p_5 q_{O6} \\
& + p_1 q_{S2} q_{O3} q_{O4} p_5 q_{S6} + p_1 q_{S2} q_{O3} q_{O4} q_{O5} p_6 + p_1 q_{S2} q_{O3} q_{O4} q_{O5} q_{O6} \\
& + p_1 q_{S2} q_{O3} q_{O4} q_{O5} q_{S6} + p_1 q_{S2} q_{O3} q_{O4} q_{S5} + p_1 q_{S2} q_{O3} q_{S4} p_5 p_6 + p_1 q_{S2} q_{O3} q_{S4} p_5 q_{O6} \\
& + p_1 q_{S2} q_{O3} q_{S4} p_5 q_{S6} + p_1 q_{S2} q_{O3} q_{S4} q_{O5} p_6 + p_1 q_{S2} q_{O3} q_{S4} q_{O5} q_{O6} + p_1 q_{S2} q_{O3} q_{S4} q_{O5} q_{S6} \\
& + p_1 q_{S2} q_{O3} q_{S4} q_{S5} p_6 + p_1 q_{S2} q_{O3} q_{S4} q_{S5} q_{O6} + p_1 q_{S2} q_{O3} q_{S4} q_{S5} q_{S6} + p_1 q_{S2} q_{S3} p_4 p_5 p_6 + p_1 q_{S2} q_{S3} p_4 p_5 q_{O6} \\
& + p_1 q_{S2} q_{S3} p_4 p_5 q_{S6} + p_1 q_{S2} q_{S3} p_4 q_{O5} p_6 + p_1 q_{S2} q_{S3} p_4 q_{O5} q_{O6} + p_1 q_{S2} q_{S3} p_4 q_{S5} + p_1 q_{S2} q_{S3} p_4 q_{S5} p_6 \\
& + p_1 q_{S2} q_{S3} p_4 q_{S5} q_{O6} + p_1 q_{S2} q_{S3} q_{O4} p_5 p_6 + p_1 q_{S2} q_{S3} q_{O4} p_5 q_{O6} + p_1 q_{S2} q_{S3} q_{O4} p_5 q_{S6} + p_1 q_{S2} q_{S3} q_{O4} q_{O5} p_6 \\
& + p_1 q_{S2} q_{S3} q_{O4} q_{O5} q_{O6} + p_1 q_{S2} q_{S3} q_{O4} q_{O5} q_{S6} + p_1 q_{S2} q_{S3} q_{O4} q_{S5} p_6 + p_1 q_{S2} q_{S3} q_{S4} p_5 p_6 \\
& + p_1 q_{S2} q_{S3} q_{S4} p_5 q_{S6} + p_1 q_{S2} q_{S3} q_{S4} q_{O5} p_6 + p_1 q_{S2} q_{S3} q_{S4} q_{O5} q_{O6} + p_1 q_{S2} q_{S3} q_{S4} q_{O5} q_{S6} \\
& + p_1 q_{S2} q_{S3} q_{S4} q_{S5} p_6 + p_1 q_{S2} q_{S3} q_{S4} q_{S5} q_{O6} + p_1 q_{S2} q_{S3} q_{S4} q_{S5} q_{S6} + q_{S1} p_2 p_3 p_4 p_5 p_6 + q_{S1} p_2 p_3 p_4 p_5 q_{O6} \\
& + q_{S1} p_2 p_3 p_4 p_5 q_{S6} + q_{S1} p_2 p_3 p_4 q_{O5} p_6 + q_{S1} p_2 p_3 p_4 q_{O6} + q_{S1} p_2 p_3 p_4 q_{S5} p_6 + q_{S1} p_2 p_3 p_4 q_{S5} q_{O6} \\
& + q_{S1} p_2 p_3 p_4 q_{S5} q_{O6} + q_{S1} p_2 p_3 p_4 q_{S5} q_{S6} + q_{S1} p_2 p_3 q_{O4} p_5 p_6 + q_{S1} p_2 p_3 q_{O4} p_5 q_{O6} + q_{S1} p_2 p_3 q_{O4} p_5 q_{S6} \\
& + q_{S1} p_2 p_3 q_{O4} q_{O5} p_6 + q_{S1} p_2 p_3 q_{O4} q_{O5} q_{O6} + q_{S1} p_2 p_3 q_{O4} q_{S5} p_6 + q_{S1} p_2 p_3 q_{S4} p_5 p_6 + q_{S1} p_2 p_3 q_{S4} q_{O5} p_6 \\
& + q_{S1} p_2 p_3 q_{S4} q_{O5} q_{O6} + q_{S1} p_2 p_3 q_{S4} q_{O5} q_{S6} + q_{S1} p_2 p_3 q_{S4} q_{S5} p_6 + q_{S1} p_2 p_3 q_{S4} q_{S5} q_{O6} + q_{S1} p_2 p_3 q_{S4} q_{S5} q_{S6} \\
& + q_{S1} p_2 q_{O3} p_4 p_5 p_6 + q_{S1} p_2 q_{O3} p_4 p_5 q_{O6} + q_{S1} p_2 q_{O3} p_4 p_5 q_{S6} + q_{S1} p_2 q_{O3} p_4 q_{S5} q_{O6} + q_{S1} p_2 q_{O3} q_{S6} + q_{S1} p_2 q_{O3} q_{O4} p_5 p_6 \\
& + q_{S1} p_2 q_{O3} q_{O4} p_5 q_{O6} + q_{S1} p_2 q_{O3} q_{O4} p_5 q_{S6} + q_{S1} p_2 q_{O3} q_{O4} q_{O5} p_6 + q_{S1} p_2 q_{O3} q_{O4} q_{O5} q_{O6} \\
& + q_{S1} p_2 q_{O3} q_{O4} q_{O5} q_{S6} + q_{S1} p_2 q_{O3} q_{O4} q_{S5} p_6 + q_{S1} p_2 q_{O3} q_{O4} q_{S5} q_{O6} + q_{S1} p_2 q_{O3} q_{O4} q_{S5} q_{S6}
\end{aligned}$$

$$\begin{aligned}
& + q_{S1} p_2 q_{O3} q_{S4} p_5 p_6 + q_{S1} p_2 q_{O3} q_{S4} p_5 q_{O6} + q_{S1} p_2 q_{O3} q_{S4} p_5 q_{S6} + q_{S1} p_2 q_{O3} q_{S4} q_{O5} p_6 + q_{S1} p_2 q_{O3} q_{S4} q_{O5} q_{O6} \\
& + q_{S1} p_2 q_{O3} q_{S4} q_{O5} q_{S6} + q_{S1} p_2 q_{O3} q_{S4} q_{S5} p_6 + q_{S1} p_2 q_{O3} q_{S4} q_{S5} q_{O6} \\
& + q_{S1} p_2 q_{O3} q_{S4} q_{S5} q_{S6} + q_{S1} p_2 q_{S3} p_4 p_5 p_6 + q_{S1} p_2 q_{S3} p_4 p_5 q_{O6} \\
& + q_{S1} p_2 q_{S3} p_4 p_5 q_{S6} + q_{S1} p_2 q_{S3} p_4 q_{O5} p_6 + q_{S1} p_2 q_{S3} p_4 q_{O5} q_{O6} + q_{S1} p_2 q_{S3} p_4 q_{O5} q_{S6} \\
& + q_{S1} p_2 q_{S3} p_4 q_{S5} p_6 + q_{S1} p_2 q_{S3} p_4 q_{S5} q_{O6} + q_{S1} p_2 q_{S3} p_4 q_{S5} q_{S6} + q_{S1} p_2 q_{S3} q_{O4} p_5 p_6 + q_{S1} p_2 q_{S3} q_{O4} p_5 q_{O6} \\
& + q_{S1} p_2 q_{S3} q_{O4} p_5 q_{S6} + q_{S1} p_2 q_{S3} q_{O4} q_{O5} p_6 + q_{S1} p_2 q_{S3} q_{O4} q_{O5} q_{O6} + q_{S1} p_2 q_{S3} q_{O4} q_{O5} q_{S6} \\
& + q_{S1} p_2 q_{S3} q_{O4} q_{S5} p_6 + q_{S1} p_2 q_{S3} q_{O4} q_{S5} q_{O6} + q_{S1} p_2 q_{S3} q_{O4} q_{S5} q_{S6} + q_{S1} p_2 q_{S3} q_{S4} p_5 p_6 + q_{S1} p_2 q_{S3} q_{S4} p_5 q_{O6} \\
& + q_{S1} p_2 q_{S3} q_{S4} p_5 q_{S6} + q_{S1} p_2 q_{S3} q_{S4} q_{O5} p_6 + q_{S1} p_2 q_{S3} q_{S4} q_{O5} q_{O6} + q_{S1} p_2 q_{S3} q_{S4} q_{O5} q_{S6} \\
& + q_{S1} p_2 q_{S3} q_{S4} q_{O5} q_{S6} + q_{S1} p_2 q_{S3} q_{S4} q_{S5} p_6 + q_{S1} p_2 q_{S3} q_{S4} q_{S5} q_{O6} + q_{S1} p_2 q_{S3} q_{S4} q_{S5} q_{S6} + q_{S1} q_{S2} p_3 p_4 p_5 p_6 + \\
& q_{S1} q_{S2} p_3 p_4 p_5 q_{O6} + q_{S1} q_{S2} p_3 p_4 p_5 q_{S6} + q_{S1} q_{S2} p_3 p_4 q_{O5} p_6 + q_{S1} q_{S2} p_3 p_4 q_{S5} q_{S6} + q_{S1} q_{S2} p_3 p_4 q_{S5} q_{O6} \\
& + q_{S1} q_{S2} p_3 p_4 q_{S5} q_{S6} + q_{S1} q_{S2} p_3 q_{O4} p_5 p_6 + q_{S1} q_{S2} p_3 q_{O4} p_5 q_{O6} + q_{S1} q_{S2} p_3 q_{O4} p_5 q_{S6} + q_{S1} q_{S2} p_3 q_{O4} q_{O5} p_6 + \\
& q_{S1} q_{S2} p_3 q_{O4} q_{O5} q_{O6} + q_{S1} q_{S2} p_3 q_{O4} q_{O5} q_{S6} + q_{S1} q_{S2} p_3 q_{O4} q_{S5} p_6 + q_{S1} q_{S2} p_3 q_{O4} q_{S5} q_{O6} \\
& + q_{S1} q_{S2} p_3 q_{O4} q_{S5} q_{S6} + q_{S1} q_{S2} p_3 q_{S4} p_5 p_6 + q_{S1} q_{S2} p_3 q_{S4} p_5 q_{O6} + q_{S1} q_{S2} p_3 q_{S4} p_5 q_{S6} + q_{S1} q_{S2} p_3 q_{S4} q_{O5} p_6 \\
& + q_{S1} q_{S2} p_3 q_{S4} q_{O5} q_{O6} + q_{S1} q_{S2} p_3 q_{S4} q_{O5} q_{S6} + q_{S1} q_{S2} p_3 q_{S4} q_{S5} p_6 + q_{S1} q_{S2} p_3 q_{S4} q_{S5} q_{O6} \\
& + q_{S1} q_{S2} p_3 q_{S4} q_{S5} q_{S6} + q_{S1} q_{S2} q_{O3} p_4 p_5 p_6 + q_{S1} q_{S2} q_{O3} p_4 p_5 q_{O6} + q_{S1} q_{S2} q_{O3} p_4 p_5 q_{S6} + q_{S1} q_{S2} q_{O3} q_{O5} p_6 \\
& + q_{S1} q_{S2} q_{O3} p_4 q_{O5} q_{O6} + q_{S1} q_{S2} q_{O3} p_4 q_{O5} q_{S6} + q_{S1} q_{S2} q_{O3} p_4 q_{S5} p_6 + q_{S1} q_{S2} q_{O3} p_4 q_{S5} q_{O6} \\
& + q_{S1} q_{S2} q_{O3} p_4 q_{S5} q_{S6} + q_{S1} q_{S2} q_{O3} q_{O4} p_5 p_6 + q_{S1} q_{S2} q_{O3} q_{O4} p_5 q_{O6} + q_{S1} q_{S2} q_{O3} q_{O4} p_5 q_{S6} \\
& + q_{S1} q_{S2} q_{O3} q_{O4} q_{O5} p_6 + q_{S1} q_{S2} q_{O3} q_{O4} q_{O5} q_{O6} + q_{S1} q_{S2} q_{O3} q_{O4} q_{O5} q_{S6} + q_{S1} q_{S2} q_{O3} q_{O4} q_{S5} p_6 \\
& + q_{S1} q_{S2} q_{O3} q_{O4} q_{S5} q_{O6} + q_{S1} q_{S2} q_{O3} q_{O4} q_{S5} q_{S6} + q_{S1} q_{S2} q_{O3} q_{S4} p_5 p_6 + q_{S1} q_{S2} q_{O3} q_{S4} p_5 q_{O6} \\
& + q_{S1} q_{S2} q_{O3} q_{S4} p_5 q_{S6} + q_{S1} q_{S2} q_{O3} q_{S4} q_{O5} p_6 + q_{S1} q_{S2} q_{O3} q_{S4} q_{O5} q_{O6} + q_{S1} q_{S2} q_{O3} q_{S4} q_{O5} q_{S6} \\
& + q_{S1} q_{S2} q_{O3} q_{S5} p_6 + q_{S1} q_{S2} q_{O3} q_{S5} q_{O6} + q_{S1} q_{S2} q_{O3} q_{S5} q_{S6} + q_{S1} q_{S2} q_{S3} p_4 p_5 p_6
\end{aligned}$$

$$\begin{aligned}
& + q_{S1} q_{S2} q_{S3} p_4 q_{O5} q_{S6} + q_{S1} q_{S2} q_{S3} p_4 q_{S5} p_6 + q_{S1} q_{S2} q_{S3} p_4 q_{S5} q_{O6} + q_{S1} q_{S2} q_{S3} p_4 q_{S5} q_{S6} + q_{S1} q_{S2} q_{S3} q_{O4} p_5 p_6 \\
& + q_{S1} q_{S2} q_{S3} q_{O4} p_5 q_{O6} + q_{S1} q_{S2} q_{S3} q_{O4} p_5 q_{S6} + q_{S1} q_{S2} q_{S3} q_{O4} q_{O5} p_6 + q_{S1} q_{S2} q_{S3} q_{O4} q_{O5} q_{O6} \\
& + q_{S1} q_{S2} q_{S3} q_{O4} q_{O5} q_{S6} + q_{S1} q_{S2} q_{S3} q_{O4} q_{S5} p_6 + q_{S1} q_{S2} q_{S3} q_{O4} q_{S5} q_{O6} + q_{S1} q_{S2} q_{S3} q_{O4} q_{S5} q_{S6} \\
& + q_{S1} q_{S2} q_{S3} q_{S4} p_5 p_6 + q_{S1} q_{S2} q_{S3} q_{S4} p_5 q_{O6} + q_{S1} q_{S2} q_{S3} q_{S4} p_5 q_{S6} + q_{S1} q_{S2} q_{S3} q_{S4} q_{O5} p_6 \\
& + q_{S1} q_{S2} q_{S3} q_{S4} q_{O5} q_{O6} + q_{S1} q_{S2} q_{S3} q_{S4} q_{O5} q_{S6} + q_{S1} q_{S2} q_{S3} q_{S4} q_{S5} p_6 + q_{S1} q_{S2} q_{S3} q_{S4} q_{S5} q_{O6} \\
& + q_{S1} q_{S2} q_{S3} q_{S4} q_{S5} q_{S6} + q_{S1} q_{O2} p_3 p_4 p_5 p_6 + q_{S1} q_{O2} p_3 p_4 p_5 q_{O6} + q_{S1} q_{O2} p_3 p_4 p_5 q_{S6} + q_{S1} q_{O2} p_3 p_4 q_{O5} p_6 \\
& + q_{S1} q_{O2} p_3 p_4 q_{O5} q_{O6} + q_{S1} q_{O2} p_3 p_4 q_{O5} q_{S6} + q_{S1} q_{O2} p_3 p_4 q_{S5} p_6 + q_{S1} q_{O2} p_3 p_4 q_{S5} q_{O6} + q_{S1} q_{O2} p_3 p_4 q_{S5} q_{S6} \\
& + q_{S1} q_{O2} p_3 q_{O4} p_5 p_6 + q_{S1} q_{O2} p_3 q_{O4} p_5 q_{O6} + q_{S1} q_{O2} p_3 q_{O4} p_5 q_{S6} + q_{S1} q_{O2} p_3 q_{O4} q_{O5} p_6 \\
& + q_{S1} q_{O2} p_3 q_{O4} q_{O5} q_{O6} + q_{S1} q_{O2} p_3 q_{O4} q_{O5} q_{S6} + q_{S1} q_{O2} p_3 q_{O4} q_{S5} p_6 + q_{S1} q_{O2} p_3 q_{O4} q_{S5} q_{O6} \\
& + q_{S1} q_{O2} p_3 q_{O4} q_{S5} q_{S6} + q_{S1} q_{O2} p_3 q_{S4} p_5 p_6 + q_{S1} q_{O2} p_3 q_{S4} p_5 q_{O6} + q_{S1} q_{O2} p_3 q_{S4} p_5 q_{S6} \\
& + q_{S1} q_{O2} p_3 q_{S4} q_{O5} p_6 + q_{S1} q_{O2} p_3 q_{S4} q_{O5} q_{O6} + q_{S1} q_{O2} p_3 q_{S4} q_{O5} q_{S6} + q_{S1} q_{O2} p_3 q_{S4} q_{S5} p_6 \\
& + q_{S1} q_{O2} p_3 q_{S4} q_{S5} q_{O6} + q_{S1} q_{O2} p_3 q_{S4} q_{S5} q_{S6} + q_{S1} q_{O2} q_{O3} p_4 p_5 p_6 + q_{S1} q_{O2} q_{O3} p_4 p_5 q_{O6} \\
& + q_{S1} q_{O2} q_{O3} p_4 p_5 q_{S6} + q_{S1} q_{O2} q_{O3} p_4 q_{O5} p_6 + q_{S1} q_{O2} q_{O3} q_{O5} p_6 + q_{S1} q_{O2} q_{O3} q_{O4} p_5 p_6 \\
& + q_{S1} q_{O2} q_{O3} p_4 q_{S5} p_6 + q_{S1} q_{O2} q_{O3} p_4 q_{S5} q_{O6} + q_{S1} q_{O2} q_{O3} p_4 q_{S5} q_{S6} + q_{S1} q_{O2} q_{O3} q_{O4} p_5 p_6 \\
& + q_{S1} q_{O2} q_{O3} q_{O4} p_5 q_{O6} + q_{S1} q_{O2} q_{O3} q_{O4} p_5 q_{S6} + q_{S1} q_{O2} q_{O3} q_{O4} q_{O5} p_6 + q_{S1} q_{O2} q_{O3} q_{O4} q_{O5} q_{O6} \\
& + q_{S1} q_{O2} q_{O3} q_{O4} q_{O5} q_{S6} + q_{S1} q_{O2} q_{O3} q_{O4} q_{S5} p_6 + q_{S1} q_{O2} q_{O3} q_{O4} q_{S5} q_{O6} + q_{S1} q_{O2} q_{O3} q_{O4} q_{S5} q_{S6} \\
& + q_{S1} q_{O2} q_{O3} q_{S4} p_5 p_6 + q_{S1} q_{O2} q_{O3} q_{S4} p_5 q_{O6} + q_{S1} q_{O2} q_{O3} q_{S4} p_5 q_{S6} + q_{S1} q_{O2} q_{O3} q_{S4} q_{O5} p_6 \\
& + q_{S1} q_{O2} q_{O3} q_{S4} q_{O5} q_{O6} + q_{S1} q_{O2} q_{O3} q_{S4} q_{O5} q_{S6} + q_{S1} q_{O2} q_{O3} q_{S4} q_{S5} p_6 + q_{S1} q_{O2} q_{O3} q_{S4} q_{S5} q_{O6} \\
& + q_{S1} q_{O2} q_{O3} q_{S4} q_{S5} q_{S6} + q_{S1} q_{O2} q_{S3} p_4 p_5 p_6 + q_{S1} q_{O2} q_{S3} p_4 p_5 q_{O6} + q_{S1} q_{O2} q_{S3} p_4 p_5 q_{S6} + q_{S1} q_{O2} q_{S3} p_4 q_{O5} p_6 \\
& + q_{S1} q_{O2} q_{S3} p_4 q_{O5} q_{O6} + q_{S1} q_{O2} q_{S3} p_4 q_{O5} q_{S6} + q_{S1} q_{O2} q_{S3} p_4 q_{S5} p_6 + q_{S1} q_{O2} q_{S3} p_4 q_{S5} q_{O6} \\
& + q_{S1} q_{O2} q_{S3} q_{O5} p_6 + q_{S1} q_{O2} q_{S3} q_{O5} q_{O6} + q_{S1} q_{O2} q_{S3} q_{O5} q_{S6} + q_{S1} q_{O2} q_{S3} q_{O4} p_5 p_6 \\
& + q_{S1} q_{O2} q_{S3} q_{O4} q_{O5} p_6 + q_{S1} q_{O2} q_{S3} q_{O4} q_{O5} q_{O6} + q_{S1} q_{O2} q_{S3} q_{O4} q_{O5} q_{S6} + q_{S1} q_{O2} q_{S3} q_{O4} q_{S5} p_6
\end{aligned}$$

$$\begin{aligned}
& + q_{s1} q_{o2} q_{s3} q_{s4} q_{s5} p_6 + q_{s1} q_{o2} q_{s3} q_{s4} q_{s5} q_{o6} + q_{s1} q_{o2} q_{s3} q_{s4} q_{s5} q_{s6} + q_{o1} p_2 p_3 p_4 p_5 q_{s6} \\
& + q_{o1} p_2 p_3 p_4 q_{o5} q_{s6} + q_{o1} p_2 p_3 p_4 q_{s5} p_6 + q_{o1} p_2 p_3 p_4 q_{s5} q_{o6} + q_{o1} p_2 p_3 p_4 q_{s5} q_{s6} + q_{o1} p_2 p_3 q_{o4} p_5 q_{s6} \\
& + q_{o1} p_2 p_3 q_{o4} q_{o5} q_{s6} + q_{o1} p_2 p_3 q_{o4} q_{s5} p_6 + q_{o1} p_2 p_3 q_{o4} q_{s5} q_{o6} + q_{o1} p_2 p_3 q_{o4} q_{s5} q_{s6} + q_{o1} p_2 p_3 q_{s4} p_5 p_6 \\
& + q_{o1} p_2 p_3 q_{s4} p_5 q_{o6} + q_{o1} p_2 p_3 q_{s4} p_5 q_{s6} + q_{o1} p_2 p_3 q_{s4} q_{o5} p_6 + q_{o1} p_2 p_3 q_{s4} q_{o6} + q_{o1} p_2 p_3 q_{s4} q_{o5} q_{s6} \\
& + q_{o1} p_2 p_3 q_{s4} q_{s5} p_6 + q_{o1} p_2 p_3 q_{s4} q_{s5} q_{o6} + q_{o1} p_2 p_3 q_{s4} q_{s5} q_{s6} + q_{o1} p_2 q_{o3} p_4 p_5 q_{s6} + q_{o1} p_2 q_{o3} p_4 q_{o5} q_{s6} \\
& + q_{o1} p_2 q_{o3} p_4 q_{s5} q_{s6} + q_{o1} p_2 q_{o3} p_4 q_{s5} q_{o6} + q_{o1} p_2 q_{o3} p_4 q_{s5} q_{s6} + q_{o1} p_2 q_{o3} q_{s4} p_5 p_6 + q_{o1} p_2 q_{o3} q_{s4} p_5 q_{o6} \\
& + q_{o1} p_2 q_{o3} q_{s4} p_5 q_{s6} + q_{o1} p_2 q_{o3} q_{s4} q_{o5} p_6 + q_{o1} p_2 q_{o3} q_{s4} q_{o6} + q_{o1} p_2 q_{o3} q_{s4} q_{o5} q_{s6} \\
& + q_{o1} p_2 q_{o3} q_{s4} q_{s5} p_6 + p_2 q_{o3} q_{s4} q_{s5} q_{o6} + q_{o1} p_2 q_{o3} q_{s4} q_{s5} q_{s6} + q_{o1} p_2 q_{s3} p_4 p_5 p_6 + q_{o1} p_2 q_{s3} p_4 p_5 q_{o6} \\
& + q_{o1} p_2 q_{s3} p_4 p_5 q_{s6} + q_{o1} p_2 q_{s3} p_4 q_{o5} p_6 + q_{o1} p_2 q_{s3} p_4 q_{o5} q_{o6} + q_{o1} p_2 q_{s3} p_4 q_{o5} q_{s6} + q_{o1} p_2 q_{s3} p_4 q_{s5} p_6 \\
& + q_{o1} p_2 q_{s3} p_4 q_{s5} q_{o6} + q_{o1} p_2 q_{s3} p_4 q_{s5} q_{s6} + q_{o1} p_2 q_{s3} q_{o4} p_5 p_6 + q_{o1} p_2 q_{s3} q_{o4} p_5 q_{o6} \\
& + q_{o1} p_2 q_{s3} q_{o4} p_5 q_{s6} + q_{o1} p_2 q_{s3} q_{o4} q_{o5} p_6 + p_2 q_{s3} q_{o4} q_{o5} q_{o6} \\
& + q_{o1} p_2 q_{s3} q_{o4} q_{o5} q_{s6} + q_{o1} p_2 q_{s3} q_{o4} q_{s5} p_6 + q_{o1} p_2 q_{s3} q_{o4} q_{s5} q_{o6} \\
& + q_{o1} p_2 q_{s3} q_{o4} q_{s5} q_{s6} + q_{o1} p_2 q_{s3} q_{s4} p_5 p_6 \quad + q_{o1} p_2 q_{s3} q_{s4} p_5 q_{o6} \\
& + q_{o1} p_2 q_{s3} q_{s4} p_5 q_{s6} + q_{o1} p_2 q_{s3} q_{s4} q_{o5} p_6 + q_{o1} p_2 q_{s3} q_{s4} q_{o6} \\
& + q_{o1} p_2 q_{s3} q_{s4} q_{s5} p_6 + q_{o1} p_2 q_{s3} q_{s4} q_{s5} q_{o6} \\
& + q_{o1} p_2 q_{s3} q_{s4} q_{s5} q_{s6} + q_{o1} q_{s2} p_3 p_4 p_5 p_6 + q_{o1} q_{s2} p_3 p_4 p_5 q_{o6} + q_{o1} q_{s2} p_3 p_4 p_5 q_{s6} + q_{o1} q_{s2} p_3 p_4 q_{o5} p_6 \\
& + q_{s2} p_3 p_4 q_{o5} q_{o6} + q_{o1} q_{s2} p_3 p_4 q_{o5} q_{s6} + q_{o1} q_{s2} p_3 p_4 q_{s5} p_6 + q_{o1} q_{s2} p_3 p_4 q_{s5} q_{o6} + q_{o1} q_{s2} p_3 p_4 q_{s5} q_{s6} \\
& + q_{o1} q_{s2} p_3 q_{o4} p_5 p_6 + q_{o1} q_{s2} p_3 q_{o4} p_5 q_{o6} + q_{o1} q_{s2} p_3 q_{o4} p_5 q_{s6} + q_{o1} q_{s2} p_3 q_{o4} q_{o5} p_6 \\
& + q_{o1} q_{s2} p_3 q_{o4} q_{o5} q_{o6} + q_{o1} q_{s2} p_3 q_{o4} q_{o5} q_{s6} + q_{o1} q_{s2} p_3 q_{o4} q_{s5} p_6 + q_{o1} q_{s2} p_3 q_{o4} q_{s5} q_{o6} \\
& + q_{o1} q_{s2} p_3 q_{o4} q_{s5} q_{s6} + q_{o1} q_{s2} p_3 q_{s4} p_5 p_6 + q_{o1} q_{s2} p_3 q_{s4} p_5 q_{o6} + q_{o1} q_{s2} p_3 q_{s4} p_5 q_{s6} + q_{o1} q_{s2} p_3 q_{s4} q_{o5} \\
& p_6 + q_{o1} q_{s2} p_3 q_{s4} q_{o5} q_{o6} + q_{o1} q_{s2} p_3 q_{s4} q_{o5} q_{s6} + q_{o1} q_{s2} p_3 q_{s4} q_{s5} p_6 + q_{o1} q_{s2} p_3 q_{s4} q_{s5} q_{o6} \\
& + q_{o1} q_{s2} p_3 q_{s4} q_{s5} q_{s6} + q_{o1} q_{s2} q_{o3} p_4 p_5 p_6 + q_{o1} q_{s2} q_{o3} p_4 p_5 q_{o6} + q_{o1} q_{s2} q_{o3} p_4 p_5 q_{s6} \\
& + q_{o1} q_{s2} q_{o3} p_4 q_{o5} p_6 + q_{o1} q_{s2} q_{o3} p_4 q_{o5} q_{o6} + q_{o1} q_{s2} q_{o3} p_4 q_{o5} q_{s6} + q_{o1} q_{s2} q_{o3} p_4 q_{s5} p_6
\end{aligned}$$

$$\begin{aligned}
& + q_{o1} q_{s2} q_{o3} p_4 q_{s5} q_{o6} + q_{o1} q_{s2} q_{o3} p_4 q_{s5} q_{s6} + q_{o1} q_{s2} q_{o3} q_{o4} p_5 p_6 + q_{o1} q_{s2} q_{o3} q_{o4} p_5 q_{o6} \\
& + q_{o1} q_{s2} q_{o3} q_{o4} p_5 q_{s6} + q_{o1} q_{s2} q_{o3} q_{o4} q_{o5} p_6 + q_{o1} q_{s2} q_{o3} q_{o4} q_{o5} q_{o6} + q_{o1} q_{s2} q_{o3} q_{o4} q_{o5} q_{s6} \\
& + q_{o1} q_{s2} q_{o3} q_{o4} q_{s5} p_6 + q_{o1} q_{s2} q_{o3} q_{o4} q_{s5} q_{o6} + q_{o1} q_{s2} q_{o3} q_{o4} q_{s5} q_{s6} + q_{o1} q_{s2} q_{o3} q_{s4} p_5 p_6 \\
& + q_{o1} q_{s2} q_{o3} q_{s4} p_5 q_{o6} + q_{o1} q_{s2} q_{o3} q_{s4} p_5 q_{s6} + q_{o1} q_{s2} q_{o3} q_{s4} q_{o5} p_6 + q_{o1} q_{s2} q_{o3} q_{s4} q_{o5} q_{o6} \\
& + q_{o1} q_{s2} q_{o3} q_{s4} q_{o5} q_{s6} + q_{o1} q_{s2} q_{o3} q_{s4} q_{s5} p_6 + q_{o1} q_{s2} q_{o3} q_{s4} q_{s5} q_{o6} + q_{o1} q_{s2} q_{o3} q_{s4} q_{s5} q_{s6} \\
& + q_{o1} q_{s2} q_{s3} p_4 p_5 p_6 + q_{o1} q_{s2} q_{s3} p_4 p_5 q_{o6} + q_{o1} q_{s2} q_{s3} p_4 p_5 q_{s6} + q_{o1} q_{s2} q_{s3} p_4 q_{o5} p_6 \\
& + q_{o1} q_{s2} q_{s3} p_4 q_{o5} q_{o6} + q_{o1} q_{s2} q_{s3} p_4 q_{o5} q_{s6} + q_{o1} q_{s2} q_{s3} p_4 q_{s5} p_6 + q_{o1} q_{s2} q_{s3} p_4 q_{s5} q_{o6} \\
& + q_{o1} q_{s2} q_{s3} p_4 q_{s5} q_{s6} + q_{o1} q_{s2} q_{s3} q_{o4} p_5 p_6 + q_{o1} q_{s2} q_{s3} q_{o4} p_5 q_{o6} + q_{o1} q_{s2} q_{s3} q_{o4} p_5 q_{s6} \\
& + q_{o1} q_{s2} q_{s3} q_{o4} q_{o5} p_6 + q_{o1} q_{s2} q_{s3} q_{o4} q_{o5} q_{o6} + q_{o1} q_{s2} q_{s3} q_{o4} q_{o5} q_{s6} + q_{o1} q_{s2} q_{s3} q_{o4} q_{s5} p_6 \\
& + q_{o1} q_{s2} q_{s3} q_{o4} q_{s5} q_{o6} + q_{o1} q_{s2} q_{s3} q_{o4} q_{s5} q_{s6} + q_{o1} q_{s2} q_{s3} q_{s4} p_5 p_6 + q_{o1} q_{s2} q_{s3} q_{s4} q_{o5} p_6 \\
& + q_{o1} q_{s2} q_{s3} q_{s4} p_5 q_{s6} + q_{o1} q_{s2} q_{s3} q_{s4} q_{o5} p_6 + q_{o1} q_{s2} q_{s3} q_{s4} q_{o5} q_{o6} + q_{o1} q_{s2} q_{s3} q_{s4} q_{o5} q_{s6} \\
& + q_{o1} q_{s2} q_{s3} q_{s4} q_{s5} p_6 + q_{o1} q_{s2} q_{s3} q_{s4} q_{s5} q_{o6} + q_{o1} q_{s2} q_{s3} q_{s4} q_{s5} q_{s6} + q_{o1} q_{o2} p_3 p_4 p_5 q_{s6} \\
& + q_{o1} q_{o2} p_3 p_4 q_{o5} q_{s6} + q_{o1} q_{o2} p_3 p_4 q_{s5} p_6 + q_{o1} q_{o2} p_3 p_4 q_{s5} q_{o6} + q_{o1} q_{o2} p_3 p_4 q_{s5} q_{s6} + q_{o1} q_{o2} p_3 q_{o4} p_5 q_{s6} \\
& + q_{o1} q_{o2} p_3 q_{o4} q_{o5} q_{s6} + q_{o1} q_{o2} p_3 q_{o4} q_{s5} p_6 + q_{o1} q_{o2} p_3 q_{o4} q_{s5} q_{o6} + q_{o1} q_{o2} p_3 q_{o4} q_{s5} q_{s6} \\
& + q_{o1} q_{o2} p_3 q_{s4} p_5 p_6 + q_{o1} q_{o2} p_3 q_{s4} p_5 q_{o6} + q_{o1} q_{o2} p_3 q_{s4} p_5 q_{s6} + q_{o1} q_{o2} p_3 q_{s4} q_{o5} p_6 \\
& + q_{o1} q_{o2} p_3 q_{s4} q_{o5} q_{o6} + q_{o1} q_{o2} p_3 q_{s4} q_{o5} q_{s6} + q_{o1} q_{o2} p_3 q_{s4} q_{s5} p_6 + q_{o1} q_{o2} p_3 q_{s4} q_{s5} q_{o6} \\
& + q_{o1} q_{o2} p_3 q_{s4} q_{s5} q_{s6} + q_{o1} q_{o2} q_{o3} p_4 p_5 q_{s6} + q_{o1} q_{o2} q_{o3} q_{o4} p_5 q_{s6} + q_{o1} q_{o2} q_{o3} q_{o4} q_{o5} p_6 \\
& + q_{o1} q_{o2} q_{o3} q_{o4} q_{s5} p_6 + q_{o1} q_{o2} q_{o3} q_{o4} q_{s5} q_{o6} + q_{o1} q_{o2} q_{o3} q_{o4} q_{s5} q_{s6} + q_{o1} q_{o2} q_{o3} q_{o4} q_{s6} \\
& + q_{o1} q_{o2} q_{o3} q_{s4} p_5 q_{o6} + q_{o1} q_{o2} q_{o3} q_{s4} p_5 q_{s6} + q_{o1} q_{o2} q_{o3} q_{s4} q_{o5} p_6 + q_{o1} q_{o2} q_{o3} q_{s4} q_{o5} q_{o6} \\
& + q_{o1} q_{o2} q_{o3} q_{s4} q_{o5} q_{s6} + q_{o1} q_{o2} q_{o3} q_{s4} q_{s5} p_6 + q_{o1} q_{o2} q_{o3} q_{s4} q_{s5} q_{o6} + q_{o1} q_{o2} q_{o3} q_{s4} q_{s5} q_{s6} \\
& + q_{o1} q_{o2} q_{s3} p_4 p_5 p_6 + q_{o1} q_{o2} q_{s3} p_4 p_5 q_{o6} + q_{o1} q_{o2} q_{s3} p_4 p_5 q_{s6} + q_{o1} q_{o2} q_{s3} p_4 q_{o5} p_6 \\
& + q_{o1} q_{o2} q_{s3} p_4 q_{o5} q_{o6} + q_{o1} q_{o2} q_{s3} p_4 q_{o5} q_{s6} + q_{o1} q_{o2} q_{s3} p_4 q_{s5} p_6 + q_{o1} q_{o2} q_{s3} p_4 q_{s5} q_{o6} \\
& + q_{o1} q_{o2} q_{s3} p_4 q_{s5} q_{s6} + q_{o1} q_{o2} q_{s3} q_{o4} p_5 p_6 + q_{o1} q_{o2} q_{s3} q_{o4} q_{o5} p_6 + q_{o1} q_{o2} q_{s3} q_{o4} q_{s5} p_6
\end{aligned}$$

$$\begin{aligned}
 & + q_{o1} q_{o2} q_{s3} q_{o4} q_{o5} p_6 + q_{o1} q_{o2} q_{s3} q_{o4} q_{o5} q_{o6} + q_{o1} q_{o2} q_{s3} q_{o4} q_{o5} q_{s6} + q_{o1} q_{o2} q_{s3} q_{o4} q_{s5} p_6 \\
 & + q_{o1} q_{o2} q_{s3} q_{o4} q_{s5} q_{o6} + q_{o1} q_{o2} q_{s3} q_{o4} q_{s5} q_{s6} + q_{o1} q_{o2} q_{s3} q_{s4} p_5 p_6 + q_{o1} q_{o2} q_{s3} q_{s4} p_5 q_{o6} \\
 & + q_{o1} q_{o2} q_{s3} q_{s4} p_5 q_{s6} + q_{o1} q_{o2} q_{s3} q_{s4} q_{o5} p_6 + q_{o1} q_{o2} q_{s3} q_{s4} q_{o5} q_{o6} + q_{o1} q_{o2} q_{s3} q_{s4} q_{o5} q_{s6} \\
 & + q_{o1} q_{o2} q_{s3} q_{s4} q_{s5} p_6 + q_{o1} q_{o2} q_{s3} q_{s4} q_{s5} q_{o6} + q_{o1} q_{o2} q_{s3} q_{s4} q_{s5} q_{s6} = 1 - \prod_{i=1}^6 (1 - q_{s_i}) \quad (3)
 \end{aligned}$$

Reference:

1. A method to evaluate Reliability of three state device networks. Balbir S. Dhillon and Subramanyam N. Rayapati, Microelectron reliability, Vol.26, No.3, pp.535-554, 1986.

