

# SOLUTION OF DYNAMIC ECONOMIC POWER DISPATCH PROBLEM USING AI TECHNIQUES

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**Abstract-** This research paper gives solution for Economic Load Dispatch (ELD) problem with considering valve point effect. ELD is the oldest and most important problem of optimal power flow. Objective of the ELD problems is to find out the optimal combination of power outputs of generating units so as to cope up the load demand at minimum cost while satisfying all the equality and inequality constraints. Conventionally, the function of cost for each unit in ELD problems has been approximately represented by a quadratic equation and is solved using various conventional and artificial intelligent techniques of optimization. Unfortunately, high non-linearity is present in the input-output characteristics of generating units due to presences of prohibited operating zones, valve point loading effects, and multi-fuel effects, etc. Thus, the practical ELD problem is formulated as optimization problem of a non-smooth function with equality and inequality constraints, which cannot be solved by the conventional optimization methods. The performance of Cuckoo Search method and PSO with some modifications is tested on a standard test bed system i.e. IEEE 30-bus 6-generators system.

**Keywords:** Valve-point effect, Cuckoo search method (CS), Particle Swarm Optimization (PSO).

## I. INTRODUCTION

The prime responsibility of a power engineer is to maintain economy and continuity of power supply. So that electrical power systems are designed and operated in order to meet the highly dynamic demands of various types of loads. Economic Load Dispatch (ELD) is a method to schedule the generator's power outputs with respect to the load demands in order to minimize of the operational cost, and to operate the power system most economically. Over the years, many efforts have been made to solve the Economic Load Dispatch (ELD) problem, incorporating different kinds of constraints or multiple objective functions through various mathematical programming and optimization techniques. Various algorithms available for optimizations are broadly classified into conventional methods and swarm intelligence based AI techniques. The conventional methods include Newton-Raphson (NR) method, Lambda Iteration method (LIM), Base Point and Participation Factor method, Gradient Point (GP) method, etc[1]. However, these classical strategy of optimal power dispatch require to consider the incremental cost curves to be monotonically increasing or it should be piece-wise linear[2]. In this paper non-smooth function of ELD is considered which shows the input-output characteristics of modern generating units. These curves are highly non-linear

(with valve-point effect and rate limits etc.) and having multiple local optimum points in the cost function. The objective function of ELD problem with valve-point effect is not a linear one and it is non-differential too[15]. These functions are valued by classical dispatch algorithms which resulted in huge revenue loss over the time. Consideration of non-linearity in cost functions of generating units requires highly robust algorithms to avoid getting stuck at local optimum solutions[3]. In this respect, stochastic search algorithms like Genetic Algorithm (GA)[9], Evolutionary Strategy (ES)[12], Evolutionary Programming (EP)[2-3,13], Particle Swarm Optimization (PSO)[18] and Simulated Annealing (SA) may prove to be very efficient in solving highly nonlinear ELD problem without any restrictions on the shape of the cost curves. Although, these heuristic methods do not always guarantee the global optimal solution, they generally provide a fast and reasonable solution (sub optimal or near global optimal).

Recently a new evolutionary technique i.e. Cuckoo Search method (CS) has been introduced in 2009 by Xin-She Yang, this algorithm is encouraged by brooding behaviour of cuckoo birds. This algorithm can take care of optimality on rough and discontinuous surface[20]. It can handle integer and discrete optimization problems efficiently. This algorithm is easy to implement on any optimization problem because of it has less number of control variables[14,20]. The CS algorithm has been used as an optimization tool in solving various single and multi-objective OPF problems[15-16]. Second technique is particle swarm optimization (PSO) which has been used to solve various engineering problems[18-22]. This paper proposes two evolutionary optimization techniques namely Cuckoo Search (CS) method and Modified PSO (MPSO) to solve ELD for the electric power system. Above two techniques are respectively used to solve an ELD problem with valve point effect for IEEE 30 bus standard system and the comparison between results obtained by above two methods has been presented.

## II. PROBLEM FORMULATION

### A. Problem objectives

The generating cost of any plant is the cost of fuel required to generate electric power in order to meet the power demand and power losses in the system. Economic dispatch (ED) problem

is to be considered as minimization of total generating cost  $C_i$ , by varying the generated power output  $P_g$  from each unit within its min-max limits.

### I. Objective function

The objective function of DED problem is to minimize the total production cost of power over a given dispatch period, while satisfying various constraints. The objective function is formulated as [22-23]

$$\text{Minimize, } F_T = \sum_{h=1}^H \sum_{i=1}^{NG} f(P_i) \quad (1)$$

For accurate non convex models of the objective function, the DED problem with valve point effects has to be considered. The real input-output characteristics displays higher-order nonlinearities and discontinuities present in curve due to valve-point effect in fossil fuel burning power plants. The valve-point effects introduce ripples in the heat-rate curves.

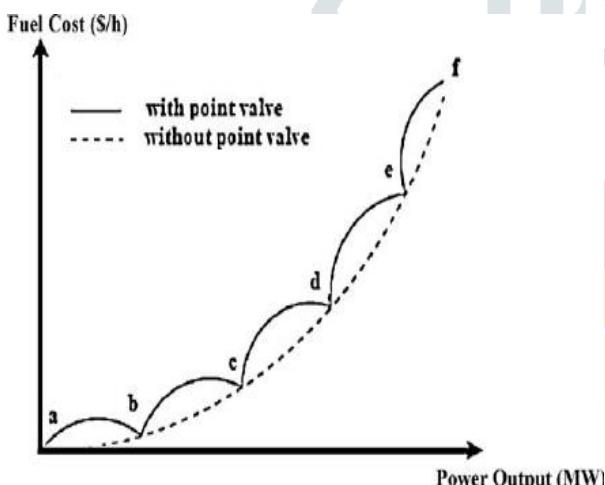


Figure 1 Fuel-Cost curve with and without valve point effect

The valve-point loading effect has been demonstrated in a periodic rectified sinusoidal function. Mathematically, economic load dispatch problem considering valve point loading is defined as following:

$$F(P_i) = (a_i P_i^2 + b_i P_i + c_i + |d_i * \sin\{e_i * (P_i^{\min} - P_i)\}|) \quad (2)$$

Where-  $a_i$ ,  $b_i$ ,  $c_i$ ,  $d_i$ ,  $e_i$  are the cost co-efficient of the  $i$ th generating unit.

### B. System Constraints

In this paper following equality and inequality constraints are considered:

#### 1) Equality Constraints

Real power balance i.e. total generation should be equal to total demand plus losses, is to be considered as equality constraint [13].

$$\sum_{i=1}^{NG} P_{g_i} - \sum_{i=1}^{NB} P_{d_i} - P_{loss} = 0 \quad (3)$$

Here,  $NG$  is no. of generating units and  $NB$  is the number of load buses.  $P_g$  is the active power generated;  $P_d$  is the active power load.

Where,  $P_{loss}$  denotes active power loss in power system network. Transmission losses may vary from 5 to 15% of total load. It is very important to calculate transmission losses while solving an economic load dispatch (ELD) problem.

$$P_{loss} = \sum_{k=1}^{NL} g_k \left[ |V_i|^2 + |V_j|^2 - 2|V_i||V_j| \cos(\delta_i - \delta_j) \right] \quad (4)$$

#### 2) Inequality Constraints

Generator power output limits, minimum and maximum limits are to be considered as inequality constraints.

$$P_{g_i}^{\min} \leq P_{g_i} \leq P_{g_i}^{\max} \quad (5)$$

Here  $NG$  shows the number of generators, ( $i = 1, 2, \dots, NG$ )

## II. SWARM INTELLIGENCE BASED ALGORITHMS

### A. Cuckoo search method

#### 1) Overview

Cuckoo Search (CS) method is one of the recent developed meta-heuristic algorithms. This method is based on breeding behaviour of bird's family named as "Cuckoo". It's similarity with the working behaviour of cuckoo birds which is based on brooding parasitism, this algorithm also works in order to find most suitable host nest.

#### 2) Cuckoo Breeding Behaviour

Cuckoo Search (CS) method works on basics of the breeding behaviour of cuckoo birds. Cuckoo is a family of birds like Ani and Guira found in various regions of all over the world. Brooding behaviour of cuckoo birds is very different. These birds lay their eggs in communal nests because of their eggs are same in colour.

Population generation in Cuckoo Search is similar to other evolutionary algorithms. The initial population is generated randomly within the min-max limits of control parameter.

$$X_i = X_i^{\min} + \text{rand}() * (X_i^{\max} - X_i^{\min}) \quad (6)$$

( $i = 1, 2, \dots, NP$ ) Where,  $i$  is the number of eggs.

Vector  $X^{t+1}$  represent new solutions generated from the present set of solutions  $X^t$ , with the help of Levy walks.

$$X^{t+1} = X^t + \alpha \oplus \text{Levy}(\lambda) \quad (7)$$

$$\text{Levy}(\lambda) = t^{-\lambda} \quad (8)$$

The symbol  $\oplus$  shows element wise multiplication. Here,  $\alpha$  is the step size. It can vary between 0.1-1.0[14].

$$\alpha = 0.01 * s(X - G_{best}) \quad (9)$$

### 3) Steps of Cuckoo Search

On behalf of the CS algorithm's theory we have the following idealized rules[1]:

1. The number of host nests and Cuckoos kept constant.
2. Each Cuckoo can lay single or multiple eggs at a time and dumps it in a randomly chosen nest.
3. The best nests with high quality eggs will be passed over to the next generation.
4. The probability of getting identified the eggs laid by cuckoo by host, is  $Pa$  which lie in the range of  $[0, 1]$ .

## B. Particle Swarm Optimization

### 1) Overview

Particle Swarm Optimization (PSO) algorithm is an efficient evolutionary algorithm (EA) which is inspired by the social flocking behaviour of birds and the schooling behaviour of fish. All the particles in the PSO fly through problem space. Thus, working behaviour of swarm intelligent techniques is based on three important factors:

1. **Cohesion**—Stick together.
2. **Separation**—doesn't come too close.
3. **Alignment**—Follow the general heading of the flock.

### 2) Initialization

As like other evolutionary algorithms, PSO is also initialized with some random solutions. In PSO, each individual "i", called particle, represents a solution to the optimization problem i.e. a vector of decision variables,  $X_i$ [13].

$$X_i = X_i^{\min} + \text{rand}() * (X_i^{\max} - X_i^{\min}) \quad (10)$$

Here, NP shows the number of particles, ( $i=1, 2, \dots, NP$ )

### 3) Update the solution vector

In PSO algorithm particles follow the fittest member of the swarm and move toward historically good areas of the provided space. Each particle tries to modify its position using. In order to modify the solutions vector, each individual is associated with some velocity,  $v$ . Starting from some random value, velocity is updated in each iteration by the following equation[13].

$$v_{ij}^{t+1} = wv_{ij}^t + c_1 R_1 (Pbest^t - X^t) + c_2 R_2 (Gbest^t - X^t) \quad (11)$$

$v_{ij}^t$  is velocity of  $j$ th member of  $i$ th particle at iteration number  $t$  which is bounded in its min-max limits[18]

$$v_j^{\min} \leq v_{ij} \leq v_j^{\max}$$

Here, **Gbest** is the global best position in the problem space. **Pbest** is the best known individual position of a particle.  $R_1$  &  $R_2$  are the random numbers generated between 0 and 1.

On the other hand,  $C_1$  &  $C_2$  can vary in range of 0-4 but these are adjusted such as sum of  $C_1$  and  $C_2$  should be 4.  $w$  is inertia-weight which is given as below [12].

$$w = w^{\max} - \frac{(w^{\max} - w^{\min}) * \text{iteration}}{\text{max iteration}} \quad (12)$$

The position vector of swarms is updated by adding the velocity 'v' in the current solution vector as given below[18].

$$X^{t+1} = X^t + v^{t+1} \quad (13)$$

## IV. SIMULATION STUDY & RESULTS

### a) System under study

The proposed algorithms are implemented and tested on a standard test bed of IEEE- 30 bus 6-generators system. IEEE 30 bus power system consists of 48 branches, 6 generating units (generator buses) and 22 load-buses. Here, **Bus-1** is considered as *slack bus*, on the other hand generators are connected on bus number: 2,5,8,11,13 and remaining others are PQ-buses. Table-1 shows the fuel cost coefficient and of the system under study.

### b) Optimal solution obtained

In this paper, programs have been developed using MATLAB-2013 to demonstrate the effectiveness of Cuckoo search (CS) and Particle Swarm Optimization (PSO) for the optimal active power dispatch problem with and without valve point function on IEEE 30 bus system. Table-2 shows the values of parameters in algorithms for cuckoo search (CS) and particle swarm optimization (PSO).

TABLE-I Fuel Cost Coefficients of System

Unit	a	b	c	d	e
1	0.0015	1.8	40	200	0.035
2	0.0030	1.8	60	140	0.040
5	0.0012	2.1	100	160	0.038
8	0.0080	2.0	25	100	0.042
11	0.0010	2.0	125	180	0.037
13	0.0625	1.0	80	120	0.025

TABLE-II Parameters set for algorithms of CS and PSO

S. No.	Parameter	Value
1	No. of Cuckoo Nests (n)	30
2	Discovery rate of Cuckoo Eggs (pa)	1/4 <sup>th</sup>
3	No. of Particles in PSO (N)	30
4	No. of Variables in CS & PSO (D)	06
5	Penalty factor in CS & PSO (k)	10
6	Max Iterations for CS	500
7	Max Iterations for PSO	300
8	Constriction Factor in MPSO	0.5

TABLE-III Solutions for economic power dispatch with and without valve-point effect

S. No.	Parameter	Solutions for without valve-point effect			Solutions for with valve-point effect		
		Load Flow	CS	PSO	Load Flow	CS	PSO
1	Pg1	104.62	137.547	120.727	104.62	137.137	142.977
2	Pg2	80.00	54.039	64.445	80.00	60.745	75.273
3	Pg5	50.00	40.234	49.618	50.00	36.998	18.462
4	Pg8	20.00	31.580	12.835	20.00	19.224	13.878
5	Pg11	20.00	16.989	29.998	20.00	26.885	29.612
6	Pg13	20.00	12.700	15.741	20.00	12.072	13.180
7	Total Gen. (MW)	294.62	294.93	294.36	294.615	294.187	294.384
8	<b>Cost of Gen. (\$/h)</b>	<b>1034.524</b>	<b>1029.543</b>	<b>1024.069</b>	<b>1097.086</b>	<b>1056.725</b>	<b>1042.878</b>

TABLE-IV Optimal setting of generators for problem of dynamic economic power dispatch by PSO

Time (Hr)	Load (MW)	Pg1 (MW)	Pg2 (MW)	Pg5 (MW)	Pg8 (MW)	Pg11 (MW)	Pg13 (MW)	Total Gen (MW)	Total Cost (\$/h)
1	166	84.48	34.85	15.32	14.36	10.06	16.79	176.38	793.96
2	196	82.28	39.20	40.56	18.44	10.85	14.85	206.42	850.61
3	229	82.64	72.92	38.54	18.14	10.44	16.66	239.34	926.47
4	267	118.83	67.46	40.46	21.00	14.10	14.59	277.38	1010.29
5	283.4	121.54	60.88	48.00	21.81	27.32	13.59	295.37	1053.36
6	272	114.84	62.96	42.20	18.64	26.21	17.26	282.14	1030.09
7	243	93.19	57.24	32.23	23.62	27.75	19.31	253.24	972.15
8	213	88.62	45.89	36.67	19.55	17.88	14.44	223.02	903.05
9	192	80.04	35.02	37.17	22.85	12.51	14.75	201.14	850.53
10	161	80.47	31.01	24.46	10.46	10.15	12.56	172.19	790.08
11	147	61.90	27.46	15.84	23.02	10.85	18.68	160.36	786.56
12	160	80.47	31.01	24.46	10.46	10.15	12.56	172.19	790.08
13	170	82.79	31.08	15.80	15.59	12.38	18.99	180.99	827.60
14	185	72.37	27.67	37.09	25.23	18.33	14.55	194.14	847.33
15	208	81.08	68.91	24.28	15.70	12.77	15.51	217.46	891.97
16	232	88.49	65.77	29.53	11.79	29.30	17.52	243.44	944.92
17	246	106.32	59.85	32.09	19.90	25.23	13.06	256.20	987.36
18	241	105.38	75.40	26.31	18.31	12.07	14.30	252.11	977.93
19	236	100.68	72.04	24.37	15.16	18.00	16.01	245.85	960.72
20	225	106.90	51.66	29.33	12.45	22.29	12.61	235.74	929.98
21	204	88.09	41.09	33.61	10.55	22.32	18.55	214.59	892.78
22	182	90.69	36.476	16.64	11.29	25.24	12.00	192.91	844.86
23	161	80.47	31.01	24.46	10.46	10.15	12.56	172.19	790.08
24	131	57.90	23.46	15.84	13.02	12.85	10.68	140.36	712.56

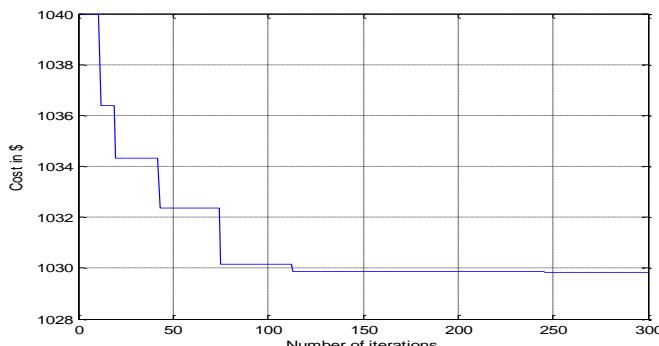


Figure.2 Fitness curve for economic power dispatch without valve-point effect by PSO technique

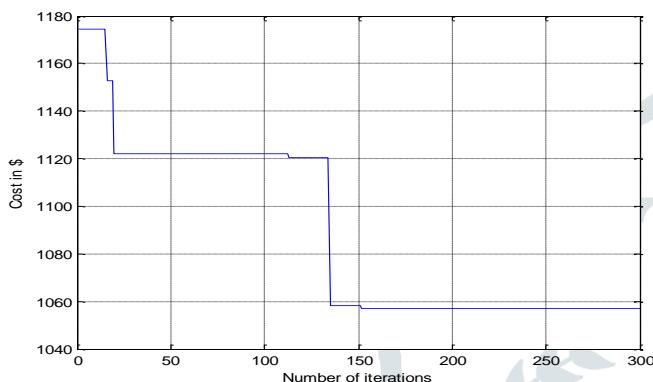


Figure.3 Fitness curve for economic power dispatch with valve-point effect by PSO technique

## V. CONCLUSION

This paper demonstrated the performance of PSO in solving dynamic economic load dispatch problem considering valve point effect. Proposed approach is simulated and tested on standard IEEE 30 bus 6 generators system. For case of economic load dispatch (ELD) with valve point effect, best solution was obtained by PSO technique; it minimized generation cost by **4.94%** as compared to initial load flow solutions. On other hand Cuckoo search method minimized fuel cost by **3.68%** for the same case. The simulation results and comparative analysis of performance show the effectiveness of Cuckoo search method and PSO techniques in handling of non-smooth function of optimal active power dispatch problem.

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