



## Structural Design of Reinforced Concrete Shear wall

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**Abstract** -Shear walls are uniquely designed structural walls constructed into buildings to resist lateral forces that are created by the plane of the wall due to wind, earthquakes and other forces. The term "shear wall" is somewhat misleading because such walls deal with similar flexural members. They are typically used in large high-rise buildings and have unlimited use in preventing buildings from completely collapsing due to seismic forces. It is always advisable to incorporate them in areas that are likely to experience high intensity earthquakes or strong winds. Wind walls are designed as simple concrete walls.

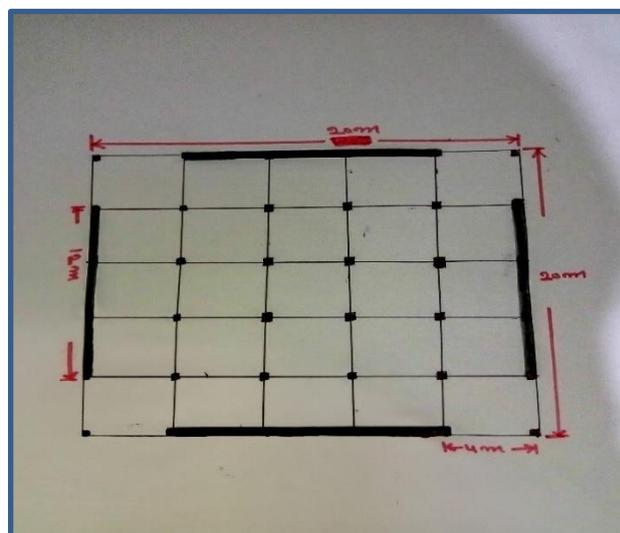
**Key Words:** Reinforced concrete shear wall, Axial force, Bending moment, Shear force, Base Moment, Base Shear, Shear strength.

### 1. INTRODUCTION

A shear wall is a structural element in a reinforced concrete frame structure that resists lateral forces such as wind forces. Shear walls are generally used in high-rise buildings exposed to cross wind and seismic forces. In reinforced concrete frame structures, the effects of wind forces increase with increasing height of the structure. Good practice guidelines limit horizontal movement or rocking.

### 2. Problem Statement

10-storey building has plan dimensions as shown in Fig. 1. Two shear walls are to be provided in each direction to resist the seismic forces. The axial load on each shearwall is 16000kN due to both dead and live loads. The height between floors is 3.5m. dead load per unit area of the floor, which consists of floor slab, finishes. etc., is 4.5kN/m<sup>2</sup> and the weight of partitions on floor is 3kN/m<sup>2</sup>. The intensity of live load on each floor is 3.5kN/m<sup>2</sup> and on roof is 1.5kN/m<sup>2</sup>. The soil below the foundation is hard and the building is located in Rishikesh.



### 3. Solution

Seismic weight of the building

According to the provisions of the code, the percentage of design load to be considered for earthquake force calculation is 25% for floors and live load for roof is not considered.

Hence, the effective weight at each floor will be

$$= 4.5 + 3.0 + 0.25 \times 3.5 = 8.375\text{kN/m}^2$$

and that at the roof = 4.5kN/m<sup>2</sup>

Weight of 60 beams, each 4 m span, on each floor and roof  
 $= 0.3 \times 0.6 \times (4 \times 60) \times 25$

$$= 1080\text{kN}$$

Weight of 36 columns at each floor

$$= 0.3 \times 0.6 \times 2.4 \times 36 \times 25$$

$$= 388.8\text{kN}$$

Weight of columns at roof = 0.5x388.8= 194.4kN

Plan area of building is 20 m × 20 m = 400 m<sup>2</sup> Equivalent load at roof level = 4.5×400 + 1080 + 194.4  
 $= 3074.4\text{kN}$

Equivalent load at each floor = 8.375×400 + 1080 + 388.8  
 $= 4818.8\text{kN}$

Seismic weight of the building,  $W = 3074.4 + 4818.8 \times 9$   
 $= 46443.6\text{kN}$

#### 3.1 Base shear

The fundamental natural period of oscillation T for buildings with shear walls is given by T =

$$\frac{0.09h}{\sqrt{d}}$$

$$= (0.09 \times 35) / (20)^{1/2} \text{ (d, the plan dimension = 20m)}$$

Building is situated in Rishikesh, i.e., in Zone IV. Zone factor Z = 0.24, importance factor I = 1, response reduction factor R = 4.0 for 5% damping and type I soil, average response acceleration coefficient  $\frac{S_a}{g} = 1.81$  Design horizontal seismic

coefficient  $A_h = \frac{Z}{2} \times \frac{I}{R} \times \frac{S_a}{g}$   
 $= \frac{0.24 \times 1 \times 1.81}{2 \times 4} = 0.0543$

Base shear  $V_b = A_h \times W = 0.0543 \times 46443.6 = 2521.887\text{kN}$

Lateral loads and shear forces at different floor level are given in Table 1.

**Table 1 Calculation of lateral loads and shear**

Mass No.	W(KN)	H(m)	W <sub>i</sub> h <sub>i</sub> <sup>2</sup>	W <sub>i</sub> h <sub>i</sub> <sup>2</sup> / ∑ W <sub>i</sub> h <sub>i</sub> <sup>2</sup>	Q <sub>i</sub> (KN)	V <sub>i</sub> (KN)
1	3074.4	35	3766140	0.8291312	461.29	464.29
2	4818.8	31.5	4781454.3	0.23222469	585.65	1046.94
3	4818.8	28	377939.2	0.18348618	462.74	1509.68
4	4818.8	24.5	2892484.7	0.104816	354.28	1863.96
5	4818.8	21	2125090.8	0.10321097	260.29	2124.25
6	4818.8	17.5	1475757.5	0.07167429	180.76	2305.01
7	4818.8	14	944484.8	0.04587154	115.69	2420.07
8	4818.8	10.5	531272.7	0.02580274	65.071	2485.77
9	4818.8	7	236121.2	0.01146789	28.93	2514.701
10	4818.8	3.5	59030.3	0.00286697	7.24	2521.94
$\sum W_i h_i^2 =$			20589775.5			

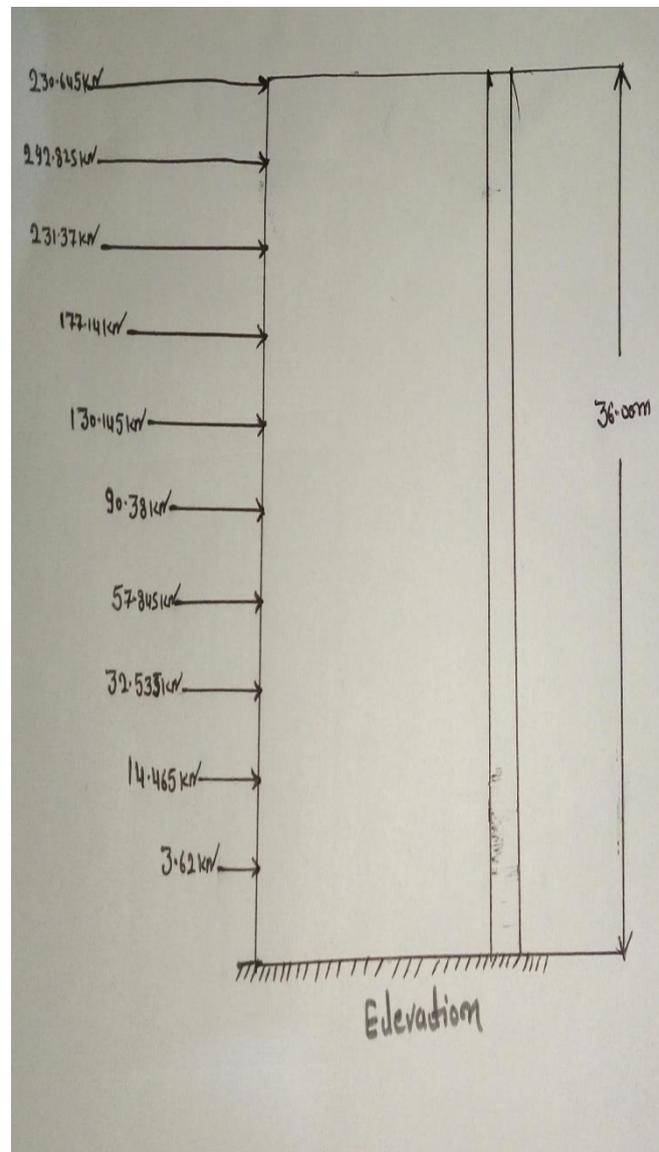
### 3.2 Bending moment and shear force

Two shear walls are arranged in each direction to resist seismic forces. Therefore, the lateral forces acting on one shear wall will be half of the calculated shears and are as shown in Fig. 2.

**Figure 2. Lateral Forces on shear wall**

The shear wall will be designed as a cantilever fixed at the base and free at the top.

Maximum shear force at base  $V = 1260.97\text{kN}$  Maximum bending moment at base,



$$M = (7.24 \times 3.5) + (28.93 \times 7) + (65.071 \times 1.5) + (115.6 \times 14) + (180.76 \times 17.5) + (260.29 \times 21) + (354.28 \times 24.5) + (462.74 \times 28) + (585.65.73 \times 31.5) + (461.29 \times 35)$$

$$M = 67388.5905 \text{ kNm}$$

### 3.3 Loads and material properties

Typical shear wall stress results obtained from the above section of the analysis and are as follows:

Taking partial safety factor 1.5

$$\text{Factored shear force, } V_u = 1.5 \times 1260.97 = 1891.455 \text{ kN}$$

$$\text{Factored bending moment, } M_u = 1.5 \times 67388.5905 = 101082.88 \text{ kNm}$$

$$\text{Factored axial load, } P_u = 1.5 \times 16000 = 24000 \text{ kN}$$

$$\text{Axial force on boundary element} = 2400 \text{ kN}$$

The material properties for reinforced concrete shear wall and reinforcing steel are assumed as follows: Concrete grade M30,  $f_{ck} = 30 \text{ MPa}$ , Reinforcement grade HYSD Fe 415

## 4. General requirements for a shear wall

Thickness of Wall,  $t_w = 300 \text{ mm}$  (Minimum thickness, as per Clause 10.1.2, IS 13920:2016 shall be 150 mm)

Length of wall,  $L_w = 14000 \text{ mm}$

Since wall thickness  $> 200 \text{ mm}$ , vertical as well as horizontal reinforcement shall be provided in two layers or in two curtains in the shear wall (Clause 10.17(b), IS 13920:2016)

Maximum diameter or reinforcement  $< (t_w)/10$  (Clause 10.1.8, IS 13920:2016)

The maximum diameter of the reinforcement should therefore be 30 mm. As 30 mm size bars are not available on the market, the maximum practical diameter of the reinforcing bar must be 28 mm.

Maximum spacing of reinforcement shall not exceed the smaller of the following:

- $L_w/5 = 14000/5 = 2800 \text{ mm}$
- $3t_w = 3 \times 300 = 900 \text{ mm}$
- 450 mm

(Clause 10.1.9, IS 13920:2016)

Hence, maximum spacing of reinforcement  $\leq 450 \text{ mm}$  Minimum in-plane reinforcement in the longitudinal and transverse directions in the shear wall shall be 0.25% of the respective gross sectional area of the wall.

(Clause 10.1.6, IS 13920:2016)

### 4.1 Shear strength requirements

$$\text{Let the nominal shear stress in the wall} = \tau_v = \frac{V_u}{d_w} \quad (\text{Clause 10.2.1, IS: 13920-2016})$$

Where,

$d_w$  = effective depth of the wall section For rectangular wall sections,

$$d_w = 0.8 \times L_w \quad (\text{Clause 10.2.1, IS: 13920-2016})$$

$$\therefore d_w = 0.8 \times 12000 = 9600 \text{ mm}$$

$$\therefore \tau_v = (1891.45 \times 1000) / (300 \times 9600)$$

$$= 0.656 \text{ MPa}$$

For M30 grade concrete  $\tau_{cmax} = 3.5 \text{ MPa}$  [Table-20, IS 456:2000]

Since  $\tau_v < \tau_{cmax}$ , wall section is adequate for shear.

Assume the minimum 0.25% steel in the wall in the vertical as well as in the horizontal direction

For  $p_t = 0.25\%$ ,  $\tau_c = 0.37 \text{ MPa}$  [Table 19, IS 456:2000]

Since  $\tau_v > \tau_c$ ,

Shear reinforcement is required.

### 4.2 Horizontal shear reinforcement

Provide horizontal shear reinforcement as per 10.2.3 section c of IS 13920:2016

Assume 2-legged 12 mm diameter horizontally aligned closed stirrups along the height of the shear wall,

Spacing of stirrups along the height of shear wall

$$\therefore \text{Spacing of stirrups} = S_v = \frac{0.87 \times f_y \times A_{sh} \times d_w}{V_{us}}$$

$$\therefore S_v = (0.87 \times 415 \times 2 \times 113 \times 9600) / [(1891.45 \times 1000) - (0.37 \times 300 \times 9600)]$$

$$\therefore S_v = 950 \text{ mm c/c}$$

Minimum horizontal reinforcement =  $(A_{sh})_{min}$

= 0.0025 of gross sectional area of the wall in elevation (Clause 10.1.6, IS 13920:2016)

$$\therefore (A_{sh})_{min} = 0.0025 \times 300 \times 1000 = 750 \text{ mm}^2$$

Hence, provide 2-legged 12 mm diameter horizontally aligned closed stirrups at 950 mm c/c along the entire height of the shear wall.

### 4.3 Vertical shear reinforcement

According to Clause 10.1.6 of IS 13920:2016, the vertical reinforcement, which shall be uniformly distributed in the wall section, shall not be less than the horizontal reinforcement.

Assume 2-legged 12 mm diameter vertically oriented stirrups.

$$\text{Spacing of stirrups} = S_v = \frac{0.87 \times f_y \times A_h \times d_w}{V_{us}}$$

$$\therefore S_v = (0.87 \times 415 \times 2 \times 113 \times 9600) / [(1891.45 \times 1000) - (0.37 \times 300 \times 9600)]$$

$$\therefore S_v = 950 \text{ mm c/c}$$

Minimum vertical reinforcement = 0.0025 of gross sectional area of the wall in plan  
(Clause 10.1.6, IS 13920:2016)

$$\therefore (A_{sv}) = 0.0025 \times 300 \times 12000 = 9000 \text{ mm}^2$$

Hence, provide 2-legged 12 mm diameter vertically aligned closed stirrups at 950 mm c/c along the entire length of the shear wall.  
 $A_{sv} > A_{sh}$ , hence ok.

### 4.4 Check for flexural strength

With reference to Annex 'A' and Clause 10.3.1 of IS 13920:2016

$$x_u / L_w = \frac{(\Phi + \lambda)}{(2\Phi + 0.36)}$$

$$x_u' / L_w = \frac{(0.0035)}{0.0035 + \left( \frac{0.87 f_y}{E_s} \right)}$$

$$\Phi = \frac{(0.87 f_y \times \rho)}{f_{ck}}$$

$$\lambda = \frac{(P_u)}{f_{ck} \times t_w \times l_w}$$

$$\rho = \text{vertical reinforcement ratio} = \frac{A_{st}}{t_w \times l_w}$$

$$= [(2 \times 113 \times 12000) / 950] / (300 \times 12000) = 0.0007928$$

$$\Phi = (0.87 \times 415 \times 0.0007928) / 30 = 0.00954$$

$$\lambda = (24000 \times 10000) / (30 \times 300 \times 12000) = 0.223$$

$$x_u / L_w = (0.00954 + 0.223) / (2 \times 0.00954 + 0.36) = 0.6134$$

$$x_u' / L_w = \frac{(0.0035)}{0.0035 + \left( \frac{0.87 \times 415}{2 \times 10^5} \right)} = 0.6597$$

Since  $x_u' / L_w > x_u / L_w$ , Eq.(a) of Annex "A" (Clause 10.3.1) IS 13920:2016, is applicable.

### 4.5 Moment of resistance of Rectangular Shear wall section

A-1 bearing moment of a slender rectangular shear wall section with uniform vertical reinforcement can be estimated as follows:

$$\therefore \frac{M_{uv}}{f_{ck} \times t_w \times l_w^2} =$$

$$\Phi \left[ \left( 1 + \frac{\lambda}{\Phi} \right) \left( \frac{1}{2} - 0.416 \frac{x_u}{l_w} \right) - \left( \frac{x_u}{l_w} \right)^2 \left( 0.168 + \frac{\beta^2}{3} \right) \right]$$

$$\beta = \left( \frac{0.87 \times 415}{0.0035 \times 2 \times 10^5} \right) = 0.5158 \quad \& \quad \frac{\beta^2}{3} = 0.088678$$

$$\therefore \frac{M_{uv}}{f_{ck} \times t_w \times l_w^2} = \{0.00954 \times [(24.375) \times (0.2448) - 0.09657]\}$$

$$\therefore \frac{M_{uv}}{f_{ck} \times t_w \times l_w^2} = 0.05600$$

$$\therefore M_{uv} = 0.05600 \times 30 \times 300 \times 12000^2$$

$$= 72576.0 \text{ kNm}$$

Balance moment to be resisted by the edge reinforcement in each shear wall

$$= (101082.88 - 72576.0)$$

$$= 28506.88 \text{ kNm}$$

#### 4.6 Check on boundary elements

To check the necessity of providing boundary elements in the shear wall (Figure 3).

Gross area of wall section,  $A_g = 12000 \times 300$   
 $= 3600000 \text{ mm}^2$

$I_{xx} = (300 \times 12000^3) / 12 = 43.2 \times 10^{12} \text{ mm}^4$

Combined stress at edge of wall:

$$\therefore \sigma = \frac{P}{A} \pm \frac{M}{I} y$$

$$\therefore \sigma = (24000 \times 10^3) / (12000 \times 300) \pm [(101082.88 \times 10^6) / (43.2 \times 10^{12})] \times (12000 / 2)$$

$$\therefore \sigma = 6.67 \pm 14.0392$$

Maximum stress  $= \sigma_{\max} = 20.70 \text{ MPa}$

According to clause 9.4.1 of IS 13920:2016, if the extreme compressive stress of fibers in the wall due to factored gravity load plus factored earthquake exceeds  $0.2 f_{ck} = 0.2 \times 30$

$$= 6 < 20.70 \text{ MPa}$$

Therefore, boundary elements are required in the shear wall. Provide a 1400mm long by 500mm wide boundary element at each edge of the shear wall, Figure 1.

#### 4.7 Design of boundary elements

The bounding element is essentially considered a column. Vertical reinforcement in edge members shall not be less than 0.80% nor more than 6%. (Clause 9.4.4, IS 13920 1993)

Adopt 3% vertical reinforcement in the boundary elements.  $A_{sc \text{ provided}} = 0.03 \times 1400 \times 500 = 21000 \text{ mm}^2$

Axial compression load on the boundary element due to seismic forces

$$= (M_u - M_{uv}) / C_w \text{ (Clause 9.4.2, IS 13920:1993)}$$

$M_u$  = Factored design moment on the entire shear wall section = 278862.64 kNm

$M_{uv}$  = Moment of resistance provided by the distributed vertical reinforcement across the wall section  
 $= 171735.56 \text{ kNm}$

$C_w$  = center to center distance between the boundary elements along the two vertical edges of the shear wall  
 $= 12.6 \text{ m}$

Axial compressive load  $= (101082.88 - 28506.88) / 12.6$

$$= 5760 \text{ kN}$$

Required axial load capacity of boundary element = axial load due to gravity effects + axial load due to seismic forces = 2400 + 5760  
 $= 8160 \text{ kN}$

As per clause 9.4.2, IS 13920:1993, the boundary element shall be assumed to behave as an axially loaded short column.

If the design strength of an axially loaded short column  $= P_{ud}$ , then

$$0.4 f_{ck} A_c + 0.674 f_y A_{sc}$$

$$P_{ud} = 0.447 f_{ck} A_g + (f_c - 0.447 f_{ck}) A_{sc} f_c = 0.790 f_y \text{ (for Fe415 steel)}$$

$$P_{ud} = 0.447 \times 30 \times 1400 \times 500 + (0.790 \times 415 -$$

$$0.447 \times 30) \times 21000$$

$$= 15990.24 \text{ kN} > 8160.15 \text{ kN, Hence ok}$$

Area of steel for each boundary element = 21000 mm<sup>2</sup> Provide 10 nos 40Φ + 12 nos 32Φ in each element

$A_{sc \text{ provided}} = 22217.34 \text{ mm}^2 > 21000 \text{ mm}^2$  Hence, Ok

As per (Clause 9.4.5, IS 13920:1993), boundary elements shall be provided with special confining reinforcement throughout their height.

$$\text{Area of special confining reinforcement } A_{sh} = 0.18 S_h \frac{f_{ck}}{f_y} \times \left( \frac{A_g}{A_k} - 1 \right)$$

(Clause 7.4.8, IS 13920:1993)

Assume 12 mm diameter closed hoops as confining reinforcement with a clear cover of 40 mm

The gross area of the boundary element section  $A_g = 1400 \times 500 = 700000 \text{ mm}^2$

The size of the core  $= A_k = (1400 - 40 - 40) \times (500 - 40 - 40) = 1320 \times 420 \text{ mm}$

Since both dimension of the core is greater than 300mm, a cross tie will have to be used.

If the cross-tie is placed at mid-length of the longer dimension of the core then,  $h = 1320 / 2 = 660 \text{ mm}$  and for shorter dimension,  $h = 420 / 2 = 210 \text{ mm}$ .

The spacing of the confining hoops,  $S$ , shall not exceed the smaller of

$$1. \frac{1}{4} \text{ Minimum member dimension, i.e. } \frac{1}{4} \times 500 = 125 \text{ mm}$$

$$2. 100 \text{ mm.}$$

The spacing however, need not be less than 100mm. (Clause 7.4.6 of IS 13920:1993)

Hence adopt 100mm spacing of the confining hoops  $S = 100 \text{ mm}$

$$A_{sh} = 0.18 \times 100 \times 660 \times \frac{30}{415} \times \left( \frac{1400 \times 500}{1320 \times 420} - 1 \right) = 225.55 \text{ mm}^2 >$$

$$113.09 \text{ mm}^2 \text{ (Area of 12 mm diameter bar)}$$

Hence, 12 mm diameter confining reinforcement is insufficient.

Adopt 20 mm diameter confining hoops at a spacing of 100mm c/c along the entire height of the boundary element  $A_{sh}$

provided =  $314 \text{ mm}^2 > 225.55 \text{ mm}^2$ .

Hence, ok.

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