



Finite Element Analysis of convective Heat Transfer flow of Ethylene Glycol based SWCNT and MWCNT Rotating Nanofluids in a Vertical Channel with Variable Viscosity, Activation energy, Heat Generating Sources and Hall Effects

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Abstract :An attempt has been made to analyse the combined effect of variable viscosity, activation energy, thermal radiation on convective heat and mass transfer flow of Ethylene glycol based Swcnt and Mwcnt nanofluids through porous medium in a vertical channel in the presence of heat generating sources. The governing equations of the flow, heat and mass transfer of nanofluids have been executed by Finite element technique. The velocity, temperature and nanoconcentration have been analysed for different parametric variations through graphs. The skin friction, rate of heat and mass transfer on the channel walls are numerically evaluated. The observation of the velocities depreciate, temperature enhances with increase in G/EC . Increase in Hall parameter(m)/ viscosity parameter(B)/ radiation(R_d) enhances u , w , θ . Velocity, temperature reduce, transverse velocity(w) enhances with higher values of rotation parameter (R)/ heat source parameter(Q)/nanoparticle volume fraction(ϕ). The nanoconcentration(C) decays with increase in activation energy(E_1)/Soret parameter(S_r).

Keywords : Egbased Swcnt and Mwcnt nanofluids, Vertical channel, activation energy, Soret effect, Hall effect, Rotation, Thermal radiation, Heat sources.

1. INTRODUCTION:

The carbon nanotubes (CNT's) have become one of the most effective materials, owing to their ability to enhance the thermal characteristics of the fluid, high electrical conductivity, unique optical transmission, and high tensile strength. They can also increase the entropy generation Berrehal [4]. Shafiq et al [13] CNT'S are rolled-up graphene sheets arranged in a cylindrical shape. They are of two types single walled (SWCNT's) and multi-walled (MWCNT's). It was observed that the boundary layer separation could be delayed if suction effects on the CNT's nanoparticle volume fraction are provided Anuar [1]. Naganthran et al [11], CNT's have higher thermal conductivity. Shamshuddin et al [14] have studied the dynamics of ethylene glycol conveying Mwcnts and Ethylene glycol conveying Swcnts: Significant joule heating and thermal radiation. Vijayalakshmi [20] has explored the effect of thermal radiation on non-Darcy hydromagnetic convective heat and mass transfer flow of a water-Swcnt's nanofluid in a cylindrical annulus with thermo-diffusion and chemical reaction. Several authors (Shamshuddin et al[15], Srinivasa Rao and Shamshuddin [17]) have examined the influence of heat sources on Conceptive heat transfer flow.

The vertical channel is an often encountered configuration in thermal engineering equipment, as an example, collectors of solar power, cooling devices of digital and micro-digital equipments and many others. The radiation effect on a hydromagnetic convective flow in a vertical channel was studied by Gupta and Gupta [8]. Datta and Jana [5] have studied the effect of wall conductance on a hydromagnetic convection of a radiation gas in a vertical channel. The combined forced and free convective flow in a vertical channel with viscous dissipation and isothermal-isoflux boundary conditions have been studied by Barletta [3].

Sulochana and Ramakrishna [18] have analyse effect of dissipation, thermal radiation, radiation absorbtion on convective heat and mass transfer flow in a non-uniformly heated vertical channel. Arundhati et el [2] have discussed thermal radiation and thermo-diffusion effect on convective heat and mass transfer flow of a rotating nanofluid in a vertical channel. Sreedevi et al [16] & Kiran Kumar et al [9] have analyse effect of dissipation and radiation on convective heat transfer flow of a rotating cu-water nano-fluid in a vertical channel.

The model with potential reactants to produce a chemical reaction minimizing the energy in the chemical system is focused nowadays in the industrial manufacturing of extrusion of plastic, aerodynamics with rubber sheets crystal growing, geothermal or oil reservoir engineering and so on (Dhramini et al. [6]). The Arrhenius activation terminology was first indicated by Svante Arrhenius around 1889. One significant measure in free convection boundary layer flows taking into account heat mass transfer together is the specific chemical reactions with finite Arrhenius activation energy. It is more significant to put on the theoretical attempts to predict the advantages of the activation energy inflows mentioned above instead of the experimental works

in these areas (Maleque [10], Netai and Dulal [12]). Suvarna [19] has discussed finite element approach of hydromagnetic heat and mass transfer flow of rotating fluid in a channel with activation energy. Recently Gopi [7] has extended this work to include the effect of heat generating sources on hydromagnetic convective heat transfer flow of rotating Swcnt and Mwcnt nanofluids in a vertical channel with inconstant viscosity.

In this paper we investigate the combined influence of variable viscosity, activation energy, thermal radiation on convective heat and mass transfer flow of Ethylene glycol based Swcnt and Mwcnt nanofluids through porous medium in a vertical channel in the presence of heat generating sources. The non-linear, coupled equations governing the flow, heat and mass transfer of nanofluids have been solved by Finite element technique with quadratic interpolation functions. The behaviour of the velocity, temperature and concentration have been discussed for different parametric variations. The skin friction, rate of heat and mass transfer on the channel walls are numerically evaluated for different variations.

2. FORMULATION OF THE PROBLEM:

We consider the steady, three-dimensional flow of a nanofluid consisting of a Ethylene glycol based Swcnt and Mwcnt nanofluids in a vertical porous channel with thermal radiation. A uniform magnetic field of strength H_0 is applied normal to the plate. It is assumed that there is no applied voltage which implies the absence of an electric field. The flow is assumed to be in the x-direction which is taken along the plane in an upward direction and z-axis is normal to the plate. It is assumed that the whole system is rotating with a constant angular velocity vector $\bar{\Omega}$ about the y-axis. The fluid is assumed to be gray, absorbing, emitting but not scattering medium. The radiation heat flux in the x-direction is considered negligible in comparison with that in the y-direction. Due to the fully developed assumption, the flow variables are functions of y only. Figure.1 shows that the problem under consideration and the co-ordinate system.

In the present problem, the following assumptions have been made: The conservation equation of current density $\nabla \cdot \bar{J} = 0$ gives $J_y = \text{constant}$.

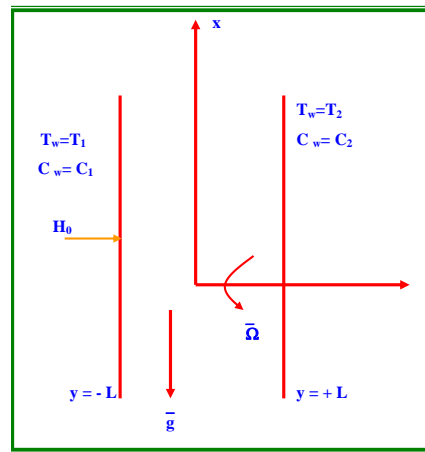


Figure 1 . Schematic diagram of the problem

Under the abovementioned assumptions, the equation of momentum and thermal energy respectively under Rosseland approximation can be written in dimensional form as:

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \tag{2.1}$$

$$\rho_{nf} (v \frac{\partial u}{\partial y} - 2\Omega w) = \frac{\partial}{\partial y} (\mu_{nf}(T) \frac{\partial u}{\partial y}) + (\rho_f \beta_T)_{nf} g(T - T_2) - (\frac{\mu_{nf}}{k_p})u - \frac{\sigma_{nf} B_o^2}{(1+m^2)}(u + mw) \tag{2.2}$$

$$\rho_{nf} (v \frac{\partial w}{\partial y} + 2\Omega u) = \frac{\partial}{\partial y} (\mu_{nf}(T) \frac{\partial w}{\partial y}) - (\frac{\mu_{nf}}{k_p})w + \frac{\sigma_{nf} B_o^2}{(1+m^2)}(mu - w) \tag{2.3}$$

$$(\rho C_p)_{nf} (v \frac{\partial T}{\partial y}) = k_{nf} \frac{\partial^2 T}{\partial y^2} - \frac{\partial(q_R)}{\partial y} + Q_H(T - T_2) + \tag{2.4}$$

$$+ 2\mu_{nf} [(\frac{\partial u}{\partial y})^2 + (\frac{\partial w}{\partial y})^2] + \frac{\sigma_{nf} \mu_e H_o^2}{1+m^2} (u^2 + w^2)$$

$$u \frac{\partial C}{\partial y} = D_B \frac{\partial^2 C}{\partial y^2} + \frac{D_T}{T_m} (\frac{\partial^2 T}{\partial y^2}) - kc(C - C_2) (\frac{T}{T_2})^n \text{Exp}(-\frac{E_a}{KT}) \tag{2.5}$$

The boundary conditions are:

$$\begin{aligned} u(\pm L) &= 0, & w(\pm L) &= 0, \\ T(-L) &= T_1, & T(+L) &= T_2, \\ C'(-L) &= C_1, & C'(+L) &= C_2 \end{aligned} \tag{2.6}$$

The properties of the nanofluids are defined as follows:

$$\begin{aligned} \mu_{nf} &= \mu_f / (1 - \phi)^{2.5} & \alpha_{nf} &= \frac{k_{nf}}{(\rho C_p)_{nf}} & \rho_{nf} &= (1 - \phi)\rho_f + \phi\rho_s \\ (\rho C_p)_{nf} &= (1 - \phi)(\rho C_p)_f + \phi(\rho C_p)_s & (\rho\beta)_{nf} &= (1 - \phi)(\rho\beta)_f + \phi(\rho\beta)_s \\ k_{nf} &= \frac{k_f(k_s + 2k_f - 2\phi(k_f - k_s))}{(k_s + 2k_f + 2\phi(k_f - k_s))}, & \sigma_{nf} &= (\sigma_f + \frac{3(\sigma_f - \sigma_s)\phi}{(\sigma_s + 2\sigma_f)}), \end{aligned} \tag{2.7}$$

where the subscripts nf, f and s represent the thermophysical properties of the nanofluid, base fluid and the nanosolid particles respectively and ϕ is the solid volume fraction of the nanoparticles. The thermophysical properties of the nanofluid are given in Table 1.

Table – 1 : Physical Properties of nanofluids

Physical properties	Fluid phase (Ethylene Glycol)	Swcnt	Mwcn
C _p (j/kg K)	2430	425	796
ρ(kg m ³)	1115	2600	1600
k(W/m K)	0.253	6600	3000
βx10 ⁻⁵ 1/k)	5.7	27	44
σ	10.7	1	1

We consider the solution of equation(2.1) as:

$$v = -v_0 \tag{2.8}$$

The dynamic viscosity of the nanofluids is assumed to be temperature dependent as follows:

$$\mu_{nf}(T) = \mu_f \text{Exp}(-m(T - T_2)) \tag{2.9}$$

where μ_{nf} is the nanofluid viscosity at the ambient temperature T_0 , m is the viscosity variation parameter which depends on the particular fluid.

We introduce the following dimensionless variables:

$$\begin{aligned} y' &= \frac{y}{L}, u' = \frac{u}{v_0}, w' = \frac{v}{v_0}, \theta = \frac{T - T_2}{T_1 - T_2}, C = \frac{C' - C_2}{C_1 - C_2}, G = \frac{\beta g(T_1 - T_2)L^2}{\mu_f v_0}, B = m(T_1 - T_2), \\ S &= \frac{v_0 L}{\mu_f}, M = \frac{\sigma_f \mu_e^2 H_0^2 L^2}{\rho_f \mu_f}, Q = \frac{Q_H L^2}{k_f}, Rd = \frac{4\sigma^* T_0^3}{\beta_R k_f}, So = \frac{D_B K_T (C_1 - C_2)}{T_m (T_1 - T_2)}, \gamma = \frac{k_c L^2}{D_B} \end{aligned} \tag{2.10}$$

Equations(2.2)-(2.4) in the non-dimensional form under Rosseland approximation are

$$\begin{aligned} 0 &= \left(\frac{\partial^2 u}{\partial y^2} - B \frac{\partial u}{\partial y} \frac{\partial \theta}{\partial y} \right) + \text{Exp}(B\theta) \left[A_1 A_3 \left(-S \frac{\partial u}{\partial z} + 2Rw \right) + \right. \\ &\quad \left. + A_1 A_4 G(\theta) - A_1 A_6 \frac{M^2}{1 + m^2} (u + mw) \right] \end{aligned} \tag{2.11}$$

$$0 = \left(\frac{\partial^2 w}{\partial y^2} - B \frac{\partial w}{\partial y} \frac{\partial \theta}{\partial y} \right) + \text{Exp}(B\theta) \left[A_1 A_3 \left(S \frac{\partial w}{\partial y} - 2Ru \right) - A_1 A_6 \frac{M^2}{1 + m^2} (mu - w) \right] \tag{2.12}$$

$$\begin{aligned} 0 &= \left(A_2 + \frac{4Rd}{3} \right) \frac{\partial^2 \theta}{\partial y^2} + S \text{Pr} A_5 \left(\frac{\partial \theta}{\partial y} \right) - Q \text{Pr}(\theta) + Ec \text{Pr} \text{Exp}(-B\theta) \left[\left(\frac{\partial u}{\partial y} \right)^2 + \left(\frac{\partial w}{\partial y} \right)^2 \right] + \\ &\quad + Ec \text{Pr} \frac{A_6 M^2}{1 + m^2} (u^2 + w^2) \end{aligned} \tag{2.13}$$

$$0 = \frac{\partial^2 C}{\partial y^2} + SSc \frac{\partial C}{\partial y} - \gamma C(1 + n\delta\theta) \text{Exp}\left(-\frac{E_1}{1 + \delta\theta}\right) + ScSo \frac{\partial^2 \theta}{\partial y^2} \tag{2.14}$$

Where

$$G = \frac{\beta_T g(T_1 - T_0)L^3}{v^2} \text{ (Grashof number), } B = m(T_1 - T_0) \text{ (Viscosity parameter)}$$

$$M^2 = \frac{\sigma_f \mu_e^2 H_0^2}{L} \text{ (Magnetic parameter), } Rd = \frac{4\sigma^* T_0^3}{\beta_R k_f} \text{ (Radiation parameter)}$$

$$R = \frac{\Omega L}{v}, m = \omega_e \tau_e \text{ (Rotation parameter), } m = \omega_e \tau_e \text{ (Hall parameter),}$$

$$Q = \frac{Q_H v}{Lk_f} \text{ (Heat source parameter), } \text{Pr} = \frac{\mu_f C_p}{k_f} \text{ (Prandtl number),}$$

$$Sc = \frac{v}{D_B} \text{ (Schmidt number), } \gamma = \frac{k_c v}{L} \text{ (Chemical reaction parameter),}$$

$$Sr = \frac{D_T(T_1 - T_2)}{T_m(C_1 - C_2)} \text{ (Soret parameter), } \theta_w = \frac{T}{T_2}, \delta = \theta_w - 1, \text{ (Temperature difference ratio), } E_1 = \frac{E_a}{KT_2} \text{ (Activation energy}$$

$$\text{parameter), } A_1 = (1 - \phi)^{2.5} \quad A_2 = \frac{k_{nf}}{k_f}, \quad A_3 = 1 - \phi + \phi \left(\frac{\rho_s}{\rho_f} \right), \quad A_4 = 1 - \phi + \phi \left(\frac{(\rho\beta)_s}{(\rho\beta)_f} \right), \quad A_5 = 1 - \phi + \phi \left(\frac{(\rho C_p)_s}{(\rho C_p)_f} \right),$$

$$A_6 = \left(1 + \frac{3(1 - \sigma)\phi}{(\sigma + 2)} \right), \quad \sigma = \frac{\sigma_s}{\sigma_f}$$

The boundary conditions (2.5) reduce to

$$u(\pm 1) = 0, w(\pm 1) = 0, \theta(-1) = 1, \theta(+1) = 0, C(-1) = 1, C(+1) = 0 \tag{2.15}$$

3. METHOD OF SOLUTION

The equations (2.11 - 2.14) are highly nonlinear nature and cant resolved exactly. Using Galerkin finite element analysis with quadratic interpolation polynominal the governing equation have been executed to explore the impact of the governing parameters G/M/B/ Rd/Ec/A11/B11/E1δ and γ on velocity, temperature and nanoconcentration.

4. COMPARISON:

In absence ofporous medium (K=0) and Hall effect (m=0) the results are good agreement with Gopi [7].

Parameter	Swcnt-Water nanofluid				Mwcnt-Water nanofluid				
	Gopi [7]		Present Results		Gopi [7]		Present Results		
	Nu(+1)	Sh(+1)	Nu(+1)	Sh(+1)	Nu(+1)	Sh(+1)	Nu(+1)	Sh(+1)	
R	0.25	0.498652	0.348847	0.498655	0.348845	0.497092	0.349132	0.497096	0.349133
	0.50	0.498651	0.348849	0.498650	0.348852	0.497092	0.349130	0.497099	0.349132
	1.00	0.498649	0.348852	0.498651	0.348855	0.497122	0.349128	0.497121	0.349129
Rd	0.5	0.498655	0.348846	0.498657	0.348849	0.497276	0.349135	0.497263	0.349131
	1.5	0.499252	0.348737	0.499250	0.348739	0.498381	0.349043	0.498382	0.349049
	5.0	0.499604	0.348672	0.499600	0.348675	0.499134	0.348915	0.499133	0.348916
Ec	0.05	0.498655	0.348846	0.498652	0.348847	0.497076	0.349135	0.497079	0.349139
	0.1	0.498673	0.348843	0.498669	0.348845	0.497144	0.349381	0.497142	0.349388
	0.12	0.498706	0.348837	0.498707	0.348839	0.497169	0.349632	0.497163	0.349627
Q	2	0.499236	0.348742	0.499238	0.348745	0.498335	0.348907	0.498339	0.348901
	4	0.498655	0.348846	0.498657	0.348849	0.497097	0.349396	0.497100	0.349399
	6	0.498082	0.34895	0.498088	0.34899	0.495818	0.350121	0.495827	0.350117
φ	0.05	0.498656	0.348846	0.498655	0.348842	0.497078	0.349138	0.497067	0.349136
	0.10	0.498601	0.348856	0.498605	0.348855	0.497004	0.349149	0.497001	0.349155
	0.12	0.498547	0.348867	0.498545	0.348869	0.496894	0.349173	0.496898	0.349178

Parameter	Swcnt-Water nanofluid				Mwcnt-Water nanofluid				
	Gopi [7]		Present Results		Gopi [7]		Present Results		
	Sh(-1)	Sh(+1)	Sh(-1)	Sh(+1)	Sh(-1)	Sh(+1)	Sh(-1)	Sh(+1)	
Sr	0.5	0.748156	0.348846	0.748159	0.348841	0.747505	0.349135	0.747527	0.349121
	1.0	0.747883	0.348968	0.747885	0.348969	0.746915	0.349396	0.746911	0.349369
	1.5	0.747613	0.349093	0.747604	0.349099	0.746304	0.349669	0.746313	0.349656
E1	0.1	0.748156	0.348846	0.748166	0.348841	0.747505	0.349135	0.747509	0.349167
	0.2	0.727272	0.356813	0.727274	0.356811	0.726018	0.357372	0.726023	0.357379
	0.3	0.710376	0.363286	0.710380	0.363293	0.701005	0.367008	0.701002	0.367011
δ	0.2	0.748156	0.348846	0.748155	0.348841	0.747505	0.349135	0.747503	0.349131
	0.3	0.753602	0.347509	0.753600	0.347511	0.752358	0.348056	0.752359	0.348072
	0.4	0.758337	0.346342	0.758344	0.346344	0.756482	0.347166	0.756497	0.347161

5. RESULTS AND DISCUSSION:

In this analysis an attempt has been made to investigate the effect of Hall currents, variable viscosity, activation energy on convective heat transfer flow of ethylene based Swcnt and Mwcnt nanofluid through a porous medium in a vertical channel in the presence of heat generating sources. The non-linear, coupled equations have been executed numerically for different variations. The velocity, temperature and nanoconcentrations have been displayed through different graphs.

Figs. 2(a)-2(c) exhibit the effect of Grashof number (G) on flow variables (u, w, θ). It is found from the profiles that increase in G results in an enhancement in velocity components and temperature in both Swcnt and Mwcnt-Eg nanofluids.

Figs. 3(a)-3(c) represents u, w , and θ with magnetic parameter (M). Higher the Lorentz force, smaller the velocity components and larger the temperature in the flow region. This force tends to lessen the motion of the fluid for higher values of M , as a consequence the velocity reduces.

The effect of porous medium on flow variables can be seen from figs. 4(a)-4(c). Increase in inverse Darcy parameter (K) leads to a depreciation in u and enhancement in w . This is due to the fact that increase in the obstruction of the fluid motion with increase in the inverse Darcy parameter leads to a reduction in u and w . Fig. 4(c), the temperature distribution increases with increase in values of K as a result of growth in the thickness of thermal boundary layer owing to Darcy drag developed by the porous medium.

The effect of variable viscosity (B) is exhibited in figs. 5(a)-5(c). All the flow variables experience augmentation with rising values of viscosity parameter (B) in both types of nanofluids. This may be due to the fact that increase in B leads to the thickening of the momentum and thermal boundary layers.

The effect of Hall currents (m) on u, w and θ is demonstrated in figs. 6(a)-6(c). From the profiles we notice that the momentum and thermal boundary layers becomes thicker for higher values of m which results in an enhancement velocity components and temperature in the flow region in both types of nanofluids. From the profiles we find that the values of velocity components (u, w) in Eg-Swcnt nanofluid are lesser than those in Eg based Mwcnt nanofluid while opposite behaviour is noticed in the case of temperature distribution.

Figs. 7(a)-7(c) indicate the effect of rotation parameter (R) on u, w and θ . Higher the Coriolis force, smaller the axial velocity, temperature and larger the transverse velocity (w). This indicates that the increase in rotation parameter enhances the growth of the momentum boundary layer and decays the thermal boundary layer thickness in Eg based Swcnt and Mwcnt nanofluids.

Figs. 8(a)-8(c) represent the effect of thermal radiation (R_d) on flow variables u, w and θ . With increase in radiation parameter (R_d), the thickness of momentum and thermal boundary layers grow which results in an augmentation in both the velocity components and thermal radiations. This may be due to the fact that increase in Ec leads to growth of the thermal boundary layer in both types of nanofluids. From the profiles we find that the values of velocity components (u, w) in Swcnt-Eg nanofluid are smaller than those in Mwcnt-Eg nanofluid. While opposite behaviour is observed in the case of temperature in the flow region.

From figs. 9(a)-9(c) we notice a reduction in axial velocity u , enhancement in transverse velocity (w) and temperature (θ) with higher dissipative force (Ec). From the profiles we find that the values of f', g and θ in Swcnt-Eg nanofluid are smaller than those Mwcnt-Eg nanofluid.

Figs. 10(a)-10(c) demonstrates the variation of u, w and θ with heat source Q . In the presence of heat generating source ($Q > 0$), the axial velocity and the temperature depreciate and transverse velocity (w) upsurges in the flow region. Thus the thickness of thermal boundary layer becomes thinner with increasing values of Heat generating source parameter (Q). From the profiles we find that the values of axial velocity u and temperature in Swcnt-Eg nanofluid are greater than those in Mwcnt-Eg nanofluid. In the case of secondary velocity (w) in Swcnt-Eg nanofluid are lesser than those in Mwcnt-Eg nanofluid for $Q \leq 0.1$ and for higher $Q \geq 0.3$ the values of w in Swcnt-Eg nanofluid are greater than those in Mwcnt-Eg nanofluid.

The effect of nano particle volume fraction (ϕ) on u, w and θ can be seen from figs. 11(a)-11(c). The axial velocity and temperature decrease while the transverse velocity (w) augments with rising values of nano particle volume fraction (ϕ). When the volume of the nanoparticle value fraction increases the thermal conductivity grows and hence enhances the momentum boundary layer thickness. This is due to the fact that with increase in ϕ , the thermal boundary layer becomes thinner in the boundary layer. From the graphs we find that the values of u, w and θ in Swcnt-Eg nanofluid are relatively greater than those in Mwcnt-Eg nanofluid. In the case of secondary velocity (w), its values in Swcnt-Eg nanofluid are relatively smaller than those in Mwcnt-Eg nanofluid.

Figs. 12(a)-12(c) depicts the effect of Prandtl number (Pr) on flow variables. From the profiles we notice that lesser the thermal diffusivity, smaller the axial velocity, temperature and larger the transverse velocity. From the profiles we find that the values of w, θ in Swcnt-Eg nanofluid are relatively greater than those in Mwcnt-Eg nanofluid. In the case of secondary velocity (w) we find that for $Pr \leq 0.62$, the values of w in Swcnt-Eg nanofluid are lesser than those in Mwcnt-Eg nanofluid and for higher $Pr \geq 1.62$, an opposite behaviour is observed in the values of w .

Figs. 13(i)-(ii)(a)-13(c) represents the nanoconcentration (C) with Schmidt number (Sc), Sorret parameter (Sr), chemical reaction parameter (γ). From fig. 13(a) we find that lesser the molecular diffusivity, smaller the concentration. Higher the thermo-diffusivity effects larger the concentration in the flow field (fig. 13(b)). From 13(c) we notice a depreciation in chemical reaction case ($\gamma > 0$). The variation of nanoconcentration (C) with different parameters $Sc, Sr, \gamma, E_1, \delta$ and n shows that the values of concentration C in Swcnt-Eg nanofluid are relatively greater than those in Mwcnt-Eg nanofluid with variation in Sc , while for variations in Sr, γ and E_1 the values of concentration in Swcnt-Eg nanofluid are relatively smaller than those in Mwcnt-Eg nanofluids and for variations in Sc, δ and n , a reverse behaviour is noticed in C .

Figs. 13(i)-(ii)(a)-14(c) exhibit the variation of nano concentration (C) with activation energy parameter (E_1), temperature difference ratio (δ_1) and index number n . From fig. 13(a) we notice a growth in nano concentration with higher values of E_1 . For larger values of δ_1 and n , the concentration experiences a depreciation in the flow field.

From the above analysis, we find that the values of the axial velocity in Swcnt-Eg are relatively greater than those in Mwcnt-Eg nanofluid variation in $G/R_d/E_c/Q/\phi$ and Pr , while an opposite trend is observed in f' with rising values of $M/K/B/m/R$

The values of the transverse velocity in Swcnt-Eg are relatively greater than those in Mwcnt with increasing values $K/B/m/Rd/Ec/Q/Pr$ while reversed effect is noticed with increasing values of $G/M/R/\phi$. The values of temperature(θ) in Swcnt are always greater than those values in Mwcnt for all parametric variations.

The shear stress components (τ_x, τ_z) and rate of heat transfer (Nu) at the walls $\eta = \pm 1$ have been presented in table 2 for different parametric variations. It is found that the stress components and Nusselt number augment at both the walls with rising values of Grashof number(G) in Swcnt&Mwcnt nanofluids. Higher the Lorentz force, larger the stress components and smaller the Nusselt number at $\eta = \pm 1$ in Swcnt nanofluid while in Mwcnt nanofluid τ_x reduces, Nu enhances at $\eta = \pm 1$. τ_z enhances at $\eta = -1$ and reduces at $\eta = +1$. Increase in porous parameter (K) reduces τ_x, τ_z at $\eta = \pm 1$, Nu reduces at $\eta = -1$, τ_z enhances at $\eta = +1$, In Swcnt nanofluid case while in Mwcnt nanofluid case, τ_x, Nu reduces at $\eta = \pm 1$, τ_z enhances at $\eta = -1$ and reduces at $\eta = +1$. Both stress components and Nusselt number experiences an enhancement at $\eta = \pm 1$ in both Swcnt and Mwcnt nanofluids with higher values of Hall parameter(m). With respect to rotation parameter (R), τ_x reduces, τ_z and Nu enhances in Swcnt at $\eta = +1$ while in Mwcnt case τ_x, Nu decay, τ_z grows at $\eta = \pm 1$ with higher values of R. With rising values of viscosity parameter B, we notice an augmentation in τ_x, τ_z and at $\eta = \pm 1$ in Swcnt nanofluid case while in Mwcnt nanofluid τ_x, Nu decays, τ_y grows at both the walls. In the presence of heat generating source ($Q > 0$), stress components depreciate at $\eta = \pm 1$, in both Swcnt and Mwcnt nanofluids. The rate of heat transfer upsurges in Swcnt case and decays in Mwcnt case at both the walls. Higher the thermal radiation, larger the stress components at $\eta = \pm 1$ in both Swcnt and Mwcnt nanofluids. The Nusselt number reduces in Swcnt nanofluid and enhances in Mwcnt nanofluid at $\eta = \pm 1$ with rising values of Rd.

Higher the dissipative energy (Ec), larger τ_x , smaller Nu at $\eta = \pm 1$ in Swcnt case while in case τ_y, Nu grows at $\eta = \pm 1$. The stress component τ_x reduces at $\eta = -1$ and enhances at $\eta = +1$ in both types of nanofluids. With rising values of nanoparticle volume fraction (ϕ), τ_x, τ_z decay at $\eta = \pm 1$ in both types of nanofluids. Nu enhances in Swcnt case and reduces in Mwcnt case at $\eta = \pm 1$. With respect to Prandtl number(Pr), τ_x, τ_z decay, Nu grows at $\eta = \pm 1$ in Swcnt case while in Mwcnt case τ_x, τ_z, Nu decay at $\eta = -1$ and $\eta = +1$, τ_x, τ_y grow and Nu decays with increase in Ec. From the above analysis we find that the value of stress components at the left wall $\eta = -1$ in Swcnt nanofluid are relatively smaller than those in Mwcnt nanofluid for all parametric variations.

With higher values of $G/K/B/R/Q/Rd/Ec/\phi/Pr$, the values of τ_x, τ_y in Swcnt case are smaller than those in Mwcnt case. For increase in magnetic parameter(M) and Hall parameter (m) values of τ_x, τ_y in Swcnt nanofluid are relatively greater than those in Mwcnt nanofluid. The values of the rate of heat transfer at the left wall $\eta = -1$ in Swcnt case are much higher than those in Mwcnt case while at $\eta = +1$ an opposite effect is observed in the behaviour of Nu for all parametric variations.

The rate of mass transfer (Sherwood number) at $\eta = \pm 1$ are presented in table 3 for different values of $Sc, Sr, \gamma, E1, \delta$ & n . Lesser the molecular diffusivity, larger the Sh at $\eta = -1$ and smaller Sh at $\eta = +1$, while an opposite trend is noticed in Sh with higher thermos-diffusion effect. The rate of mass transfer at $\eta = -1$ increases while at $\eta = +1$ decays in the degenerating chemical reaction case. Increase in the activation energy parameter (E1) reduces Sh at $\eta = -1$ and enhances Sh at $\eta = +1$. For higher values of temperature difference ratio(δ)/index number(n), we notice augmentation in Sh at $\eta = -1$ and reduction at $\eta = +1$. From the tabular values we find that the Sherwood number at $\eta = -1$ in Swcnt nanofluid are much smaller than in Mwcnt nanofluid while a reverse trend is noticed in Sh at $\eta = +1$.

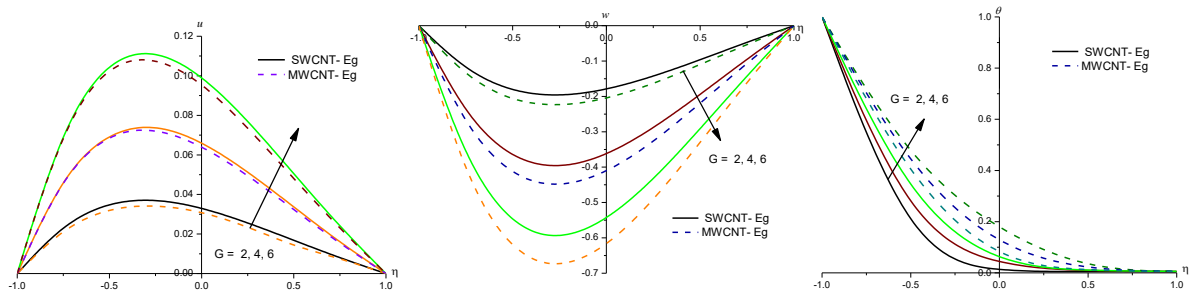


Fig.2 : Variation of [a] Axial velocity (u), [b] Secondary velocity(w), [c] Temperature(θ), with G
 $M=1.0, K=0.10, B=0.2, m=0.2, R=2, Rd=2, Ec=0.5, Q=0.1, \phi=0.1, Pr=0.62$

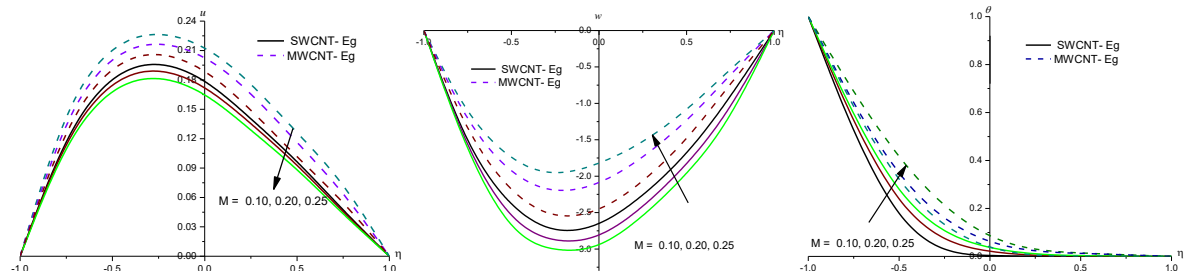


Fig.3 : Variation of [a] Axial velocity (u), [b] Secondary velocity(w), [c] Temperature(θ), with M
 $G=2, K=0.10, B=0.2, m=0.2, R=2, Rd=2, Ec=0.5, Q=0.1, \phi=0.1, Pr=0.62$

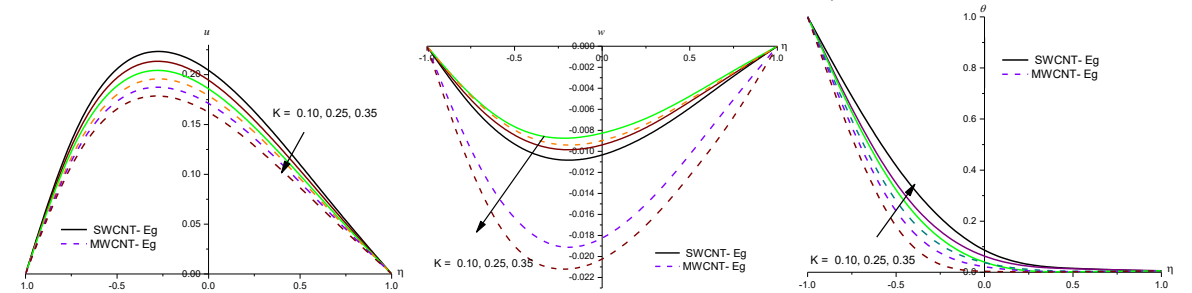


Fig.4 : Variation of [a] Axial velocity (u), [b] Secondary velocity(w), [c] Temperature(θ), with K
 $G=2, M=1.0, B=0.2, m=0.2, R=2, Rd=2, Ec=0.5, Q=0.1, \phi=0.1, Pr=0.62$

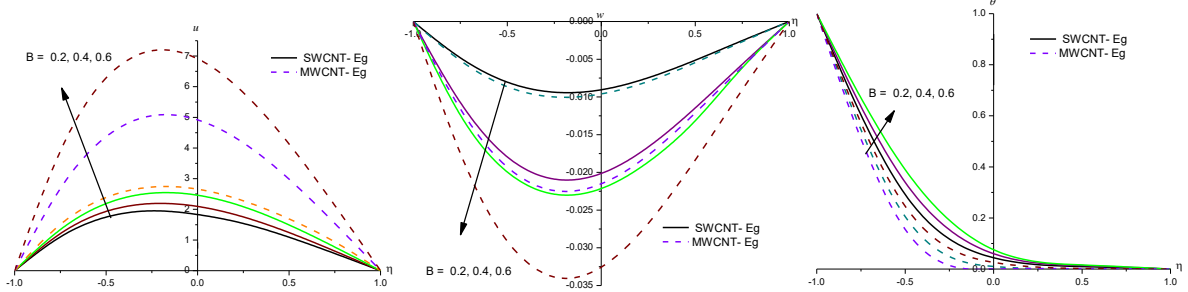


Fig.5 :Variation of [a] Axial velocity (u), [b] Secondary velocity(w), [c] Temperature(θ), with B
 $G=2, M=1.0, K=0.10, m=0.2, R=2, Rd=2, Ec=0.5, Q=0.1, \phi=0.1, Pr=0.62$

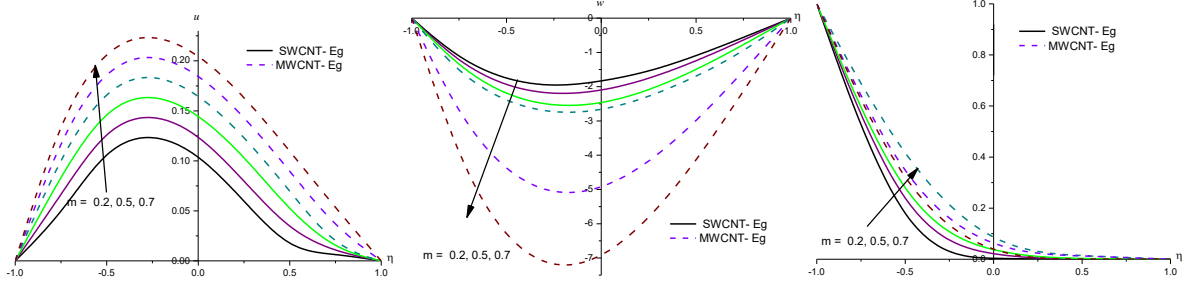


Fig.6 :Variation of [a] Axial velocity (u), [b] Secondary velocity(w), [c] Temperature(θ), with m
 $G=2, M=1.0, K=0.10, B=0.2, R=2, Rd=2, Ec=0.5, Q=0.1, \phi=0.1, Pr=0.62$

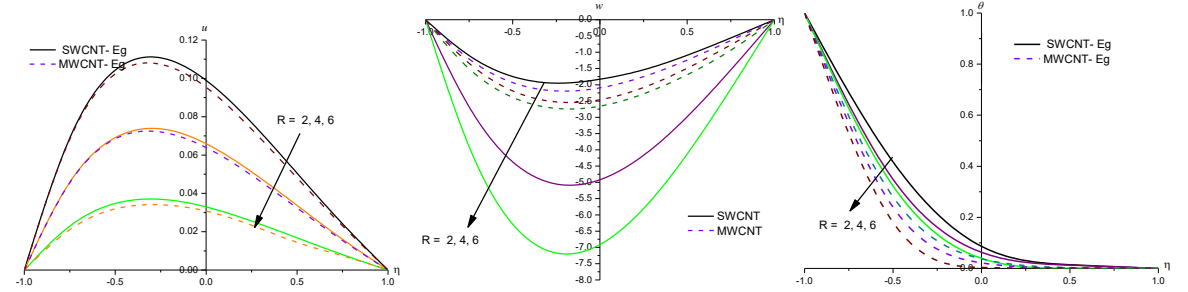


Fig.7 :Variation of [a] Axial velocity (u), [b] Secondary velocity(w), [c] Temperature(θ), with R
 $G=2, M=1.0, K=0.10, B=0.2, m=0.2, Rd=2, Ec=0.5, Q=0.1, \phi=0.1, Pr=0.62$

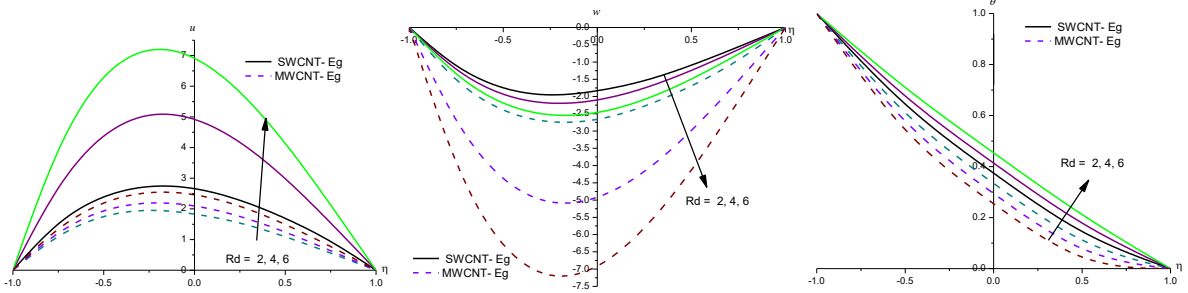


Fig.8 :Variation of [a] Axial velocity (u), [b] Secondary velocity(w), [c] Temperature(θ), with Rd
 $G=2, M=1.0, K=0.10, B=0.2, m=0.2, R=2, Ec=0.5, Q=0.1, \phi=0.1, Pr=0.62$

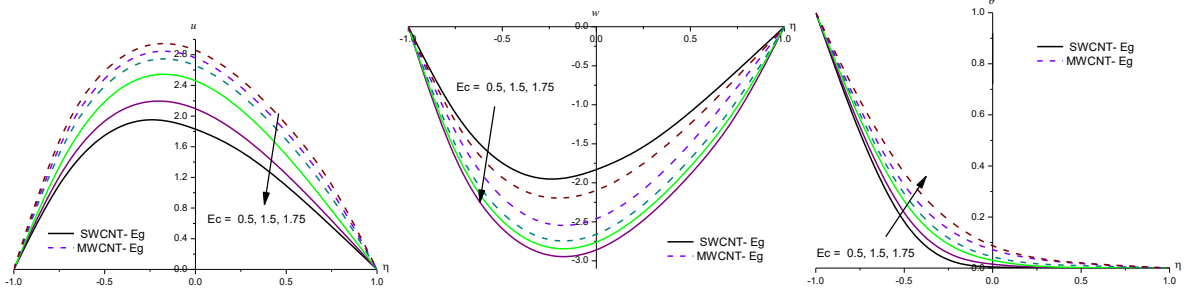


Fig.9 :Variation of [a] Axial velocity (u), [b] Secondary velocity(w), [c] Temperature(θ), with Ec
 $G=2, M=1.0, K=0.10, B=0.2, m=0.2, R=2, Rd=2, Q=0.1, \phi=0.1, Pr=0.62$

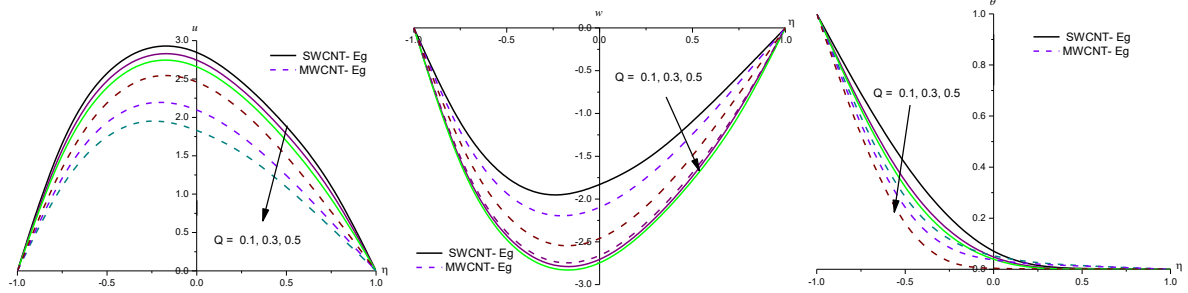


Fig.10 :Variation of [a] Axial velocity (u), [b] Secondary velocity(w), [c] Temperature(θ), with Q
 $G=2, M=1.0, K=0.10, B=0.2, m=0.2, R=2, Rd=2, Ec=0.5, \phi=0.1, Pr=0.62$

Fig.10 :Variation of [a] Axial velocity (u), [b] Secondary velocity(w), [c] Temperature(θ), with Q
 $G=2, M=1.0, K=0.10, B=0.2, m=0.2, R=2, Rd=2, Ec=0.5, \phi=0.1, Pr=0.62$

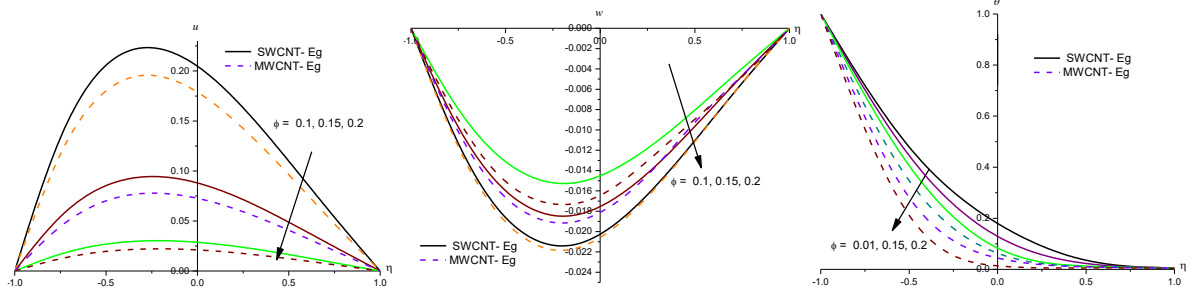


Fig.11 :Variation of [a] Axial velocity (u), [b] Secondary velocity(w), [c] Temperature(θ), with ϕ
 $G=2, M=1.0, K=0.10, B=0.2, m=0.2, R=2, Rd=2, Ec=0.5, Q=0.1, Pr=0.62$

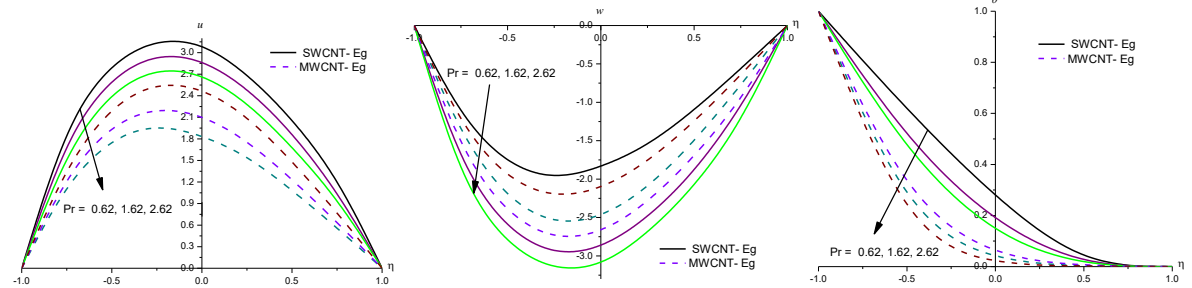


Fig.12 :Variation of [a] Axial velocity (u), [b] Secondary velocity(w), [c] Temperature(θ), with Pr
 $G=2, M=1.0, K=0.10, B=0.2, m=0.2, R=2, Rd=2, Ec=0.5, Q=0.1, \phi=0.1$

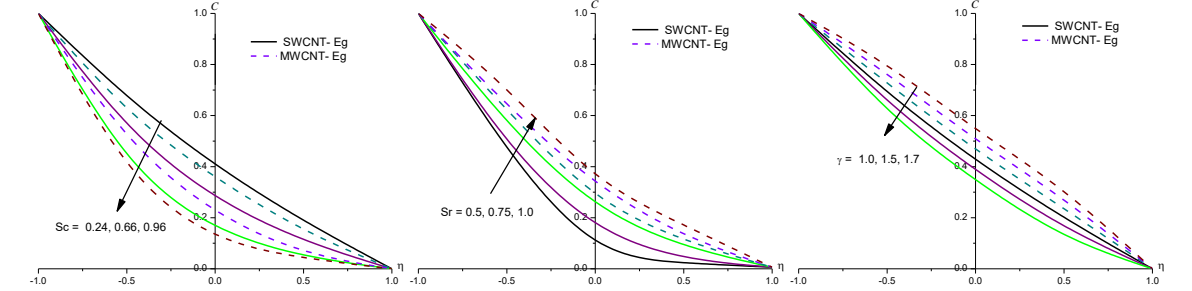


Fig.13(i) : Variation of Nanoconcentration(C) with $E1, \delta, n$

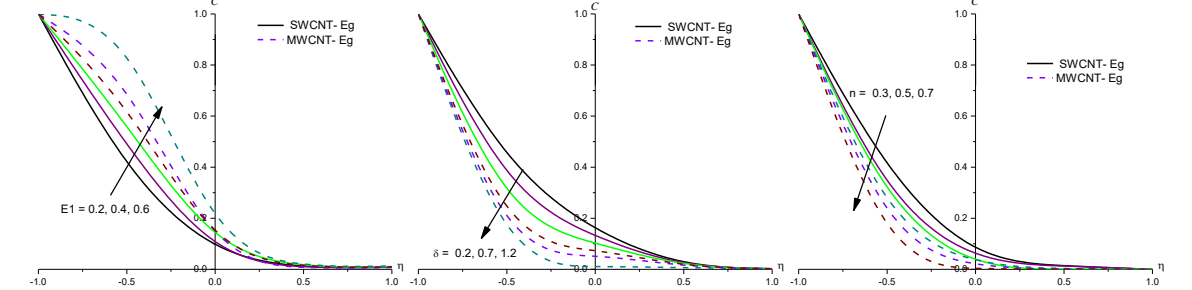


Fig.13(ii) : Variation of Nanoconcentration(C) with Sc, Sr, γ

Table 2 :Shear Stress(τ_x, τ_z) and Nusselt number(Nu) with SWCNT-EG & MWCNT-EG on the walls at $\eta = -1$

Parameter		EG-SWCNT			EG-MWCNT		
		$\tau_x(-1)$	$\tau_z(-1)$	$Nu(-1)$	$\tau_x(-1)$	$\tau_z(-1)$	$Nu(-1)$
G	0.2	0.13833	-0.0056748	0.501032	0.139516	-0.0058577	0.502264
	0.4	0.27665	-0.0117252	0.501042	0.279032	-0.0117156	0.502267
	0.6	0.41498	-0.0175878	0.501132	0.418548	-0.0175734	0.502269
M	0.10	1.33914	-0.0301075	0.501031	1.440054	-0.0342246	0.502263
	0.20	1.35355	-0.0397172	0.501027	1.424544	-0.0422908	0.502266
	0.25	1.38328	-0.0586263	0.501022	1.395165	-0.0585782	0.502288
m	0.2	1.10033	-0.4524364	0.501033	1.133135	-0.4840233	0.502261
	0.5	0.78185	-0.5128166	0.501031	0.320932	-0.5459234	0.502253
	0.7	0.61469	-0.5695869	0.501027	0.647827	-0.5919594	0.502264
K	0.10	1.49484	-0.0698632	0.501028	1.49461	-0.0716344	0.502257
	0.25	1.43612	-0.0649837	0.501029	1.44259	-0.0645927	0.502253
	0.35	1.38328	-0.0586263	0.501032	1.39516	-0.0585782	0.502258
B	0.2	1.38395	-0.0567745	0.500088	1.39636	-0.0586535	0.500189
	0.4	1.38382	-0.0586599	0.500107	1.39633	-0.0586526	0.500095
	0.6	1.38381	-0.0587592	0.500126	1.39622	-0.0586505	0.500273
R	2	1.38339	-0.0567461	0.501029	1.39536	-0.0585782	0.502258
	4	1.37261	-0.1186266	0.501032	1.39544	-0.0585782	0.502248

	6	1.38328	-0.1586263	0.501043	1.39516	-0.0585782	0.502258
Q	0.1	1.38373	-0.0557615	0.500468	1.39589	-0.0586241	0.501027
	0.3	1.38375	-0.0586546	0.500271	1.39614	-0.0586402	0.500595
	0.5	1.38378	-0.0586276	0.500191	1.39625	-0.0586468	0.500418
	2	1.38339	-0.0567461	0.501029	1.39516	-0.0585782	0.502258
Rd	4	1.37262	-0.1186266	0.501023	1.39519	-0.0585788	0.502245
	6	1.38329	-0.1586266	0.501021	1.39522	-0.0585789	0.502232
	0.5	1.38339	-0.0567461	0.501029	1.39516	-0.0585782	0.502258
Ec	1.5	1.21642	-0.0483892	0.501035	1.28027	-0.0510397	0.502268
	1.7	1.05968	-0.0394935	0.501044	1.16149	-0.0439422	0.502277
	0.05	1.38395	-0.0567748	0.500103	1.39636	-0.0586534	0.500226
φ	0.15	1.38373	-0.0586547	0.500269	1.39615	-0.0586404	0.500579
	0.20	1.38364	-0.0587485	0.500435	1.39593	-0.0586268	0.500955
	0.62	1.38395	-0.0567748	0.500103	1.39636	-0.0586534	0.500226
Pr	1.62	1.38373	-0.0586547	0.500269	1.39615	-0.0586404	0.500359
	2.62	1.38364	-0.0585485	0.500435	1.39593	-0.0586268	0.500955

Table 3 :Shear Stress(τ_x, τ_z) and Nusselt number(Nu) with SWCNT-EG & MWCNT-EG on the walls at $\eta = +1$

Parameter	EG-SWCNT			EG-MWCNT			
	$\tau_x(+1)$	$\tau_z(+1)$	Nu(+1)	$\tau_x(+1)$	$\tau_z(+1)$	Nu(+1)	
G	0.2	0.138339	-0.0056748	0.501032	0.139516	-0.00585778	0.502264
	0.4	0.27665	-0.0117252	0.501032	0.279032	-0.0117156	0.502264
	0.6	0.41498	-0.0175878	0.501032	0.418548	-0.0175734	0.502264
M	0.10	1.33914	-0.0301075	0.501031	1.44005	-0.0342246	0.502263
	0.20	1.35355	-0.0397172	0.50103	1.42454	-0.0422908	0.50226
	0.25	1.38328	-0.0586263	0.501029	1.39516	-0.0585782	0.502258
m	0.2	1.10033	-0.4524344	0.50103	1.13313	-0.48402	0.502261
	0.5	0.78185	-0.5128164	0.501031	0.820932	-0.545924	0.502263
	0.7	0.61469	-0.4695844	0.501032	0.647827	-0.501959	0.502264
K	0.10	1.49484	-0.0698632	0.501028	1.49461	-0.0716344	0.502257
	0.25	1.43612	-0.0649837	0.501029	1.44259	-0.0645927	0.502257
	0.35	1.38328	-0.0586263	0.501029	1.39516	-0.0585782	0.502258
B	0.2	1.38395	-0.0567745	0.500088	1.39636	-0.0586535	0.500189
	0.4	1.38382	-0.0586599	0.500107	1.39633	-0.058652	0.500231
	0.6	1.38381	-0.0586592	0.500126	1.39631	-0.0586505	0.500273
R	2	1.38339	-0.0567414	0.501029	1.39516	-0.0585782	0.502258
	4	1.37261	-0.1186264	0.501029	1.39516	-0.0585782	0.502258
	6	1.38328	-0.0586263	0.501029	1.39516	-0.0585782	0.502258
Q	0.1	1.38373	-0.0567615	0.500468	1.39589	-0.0586241	0.501027
	0.3	1.38373	-0.0586546	0.500271	1.39614	-0.0586402	0.500595
	0.5	1.38378	-0.0586576	0.500191	1.39625	-0.0586468	0.500418
Rd	2	1.38339	-0.0567414	0.501029	1.39516	-0.0585782	0.502258
	4	1.37262	-0.1186264	0.501023	1.39517	-0.0585788	0.502245
	6	1.38329	-0.0586266	0.501021	1.39518	-0.0585789	0.502242
Ec	0.5	1.38339	-0.0567414	0.501029	1.39516	-0.0585782	0.502258
	1.5	1.21642	-0.0483892	0.501035	1.28027	-0.0510397	0.502268
	1.75	1.05968	-0.0394935	0.50104	1.16149	-0.0439422	0.502277
φ	0.1	1.38395	-0.0567748	0.500103	1.39636	-0.058654	0.500226
	0.15	1.38373	-0.0586547	0.500269	1.39615	-0.0586404	0.50059
	0.2	1.38364	-0.0586485	0.500435	1.39593	-0.0586268	0.500955
Pr	0.62	1.38395	-0.0567748	0.500103	1.39636	-0.058654	0.500226
	1.62	1.38373	-0.0586547	0.500269	1.39615	-0.0586404	0.50059
	2.62	1.38364	-0.0586485	0.500435	1.39593	-0.0586268	0.500955

Table 4 :Shewood number (Sh)with SWCNT-EG & MWCNT-EG on the walls at $\eta = \pm 1$

Parameter	EG-SWCNT		EG-MWCNT		
	Sh(-1)	Sh(+1)	Sh(-1)	Sh(+1)	
Sc	0.25	0.771065	0.337335	0.770768	0.337464
	0.66	1.24332	0.166168	1.24251	0.166416
	0.96	1.57684	0.0990546	1.57567	0.0993372
Sr	0.5	0.748592	0.348651	0.748455	0.348712
	0.75	0.748535	0.348676	0.74833	0.348767
	1.0	0.748479	0.348701	0.748206	0.348822
γ	1.0	0.748479	0.348701	0.748206	0.348822

	1.5	0.809158	0.327131	0.808891	0.327247
	1.7	0.832659	0.319016	0.832395	0.31913
E1	0.2	0.738104	0.352653	0.73783	0.352775
	0.4	0.719661	0.359704	0.719384	0.359828
	0.6	0.703947	0.365731	0.703668	0.365855
δ	0.2	0.748479	0.348701	0.748206	0.348822
	0.7	0.760513	0.345739	0.760238	0.345861
	1.2	0.77168	0.342987	0.771402	0.34311
n	0.3	0.75032	0.348259	0.750047	0.34838
	0.5	0.753997	0.347378	0.753723	0.347499
	0.7	0.757667	0.346500	0.757392	0.346621

6. CONCLUSIONS:

The effect of activation energy, variable viscosity, Hall effects on convective heat and mass transfer flow of Eg based Swcnt and Mwcnt nanofluids have been investigated by solving the governing equations by Finite element method. The findings of this analysis are : Increase in Grashof number(G)/Eckert number(E_c) results in an enhancement in velocity components and temperature in both Swcnt and Mwcnt nanofluids.

- 1) Higher the Lorentz force(M)/porous permeability(K), smaller the velocity components and larger the temperature in the flow region.
- 2) All the flow variables experience augmentation with rising values of Hall parameter (m)/viscosity parameter (B)/radiation(R_d) in both types of nanofluids.
- 3) The axial velocity and temperature decrease while the transverse velocity (w) augments with rising values of nano particle volume fraction (ϕ)/Heat source (Q)/rotation(R).
- 4) The nanoconcentration (C) reduces with Sc , Chemical reaction parameter (γ) / temperature difference ratio(δ) and enhances with Soret parameter (S_r)/activation energy parameter(E_1).
- 5) τ_x reduces, τ_z and Nu enhance in Swcnt at $\eta=+1$ while in Mwcnt case τ_x , Nu decay, τ_z grows at $\eta=\pm 1$ with higher values of R .
- 6) With rising values of viscosity parameter(B), τ_x , τ_z grow at $\eta=\pm 1$ in Swcnt nanofluid case while in Mwcnt nanofluid, τ_x , Nu decay, τ_z grows at both the walls.
- 7) Higher the thermal radiation, larger the stress components at $\eta=\pm 1$ in both Swcnt and Mwcnt nanofluids. Higher the dissipative energy (E_c), larger τ_x , smaller Nu at $\eta=\pm 1$ in Swcnt case while in Mwcnt case τ_y , Nu grows at $\eta=\pm 1$.
- 8) With rising values of nanoparticle volume fraction (ϕ), τ_x , τ_z decay at $\eta=\pm 1$ in both types of nanofluids. Nu enhances in Swcnt case and reduces in Mwcnt case at $\eta=\pm 1$.
- 9) Higher thermo-diffusion effects, smaller Sh at $\eta=-1$ and larger at $\eta=+1$. The rate of mass transfer at $\eta=-1$ increases while at $\eta=+1$, it decays in the degenerating chemical reaction case.
- 10) Increase in the activation energy parameter (E_1) reduces Sh at $\eta=-1$ and enhances Sh at $\eta=+1$. For higher values of temperature difference ratio(δ)/index number(n), Sh surges at $\eta=-1$ and reduces at $\eta=+1$.

7. REFERENCES

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